# PHYSICS 12



Punjab Textbook Board, Lahore

## Chapter 12

### **ELECTROSTATICS**

### **Learning Objectives**

At the end of this chapter the students will be able to:

- Understand and describe Coulomb's law.
- Describe that a charge has a field of force around it.
- Understand fields of like and unlike charges.
- Appreciate the principle of inkjet printers and photostat copier as an application of electrostatic phenomena.
- Explain the electric intensity in a free space and in other media.
- 6. State and prove Gauss's law.
- Appreciate the applications of Gauss's law.
- Explain electric potential at a point in terms of work done in bringing a unit positive charge from infinity to that point.
- Relate electric field strength and potential gradient.
- Find expression for potential at a point due to a point charge.
- 11. Describe and derive the value of electric charge by Millikan's method.
- Calculate the capacitance of parallel plate capacitor.
- Recognize the effect of dielectric on the capacitance of parallel plate capacitor.
- Understand and describe electric polarization of dielectric.
- 15. Know the process of charging and discharging of a capacitor through a resistance and calculate the time constant.
- Find energy expression of a charged capacitor.

he study of electric charges at rest under the action of electric forces is known as electrostatics. An electric force is the force which holds the positive and negative charges that make up atoms and molecules. The human body is composed entirely of atoms and molecules, thus we owe our existence to the electric force.

A lightning flash

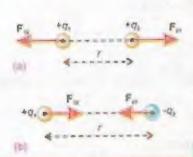


Fig. 13.1 (a) Reputsive forces between like charges and (b) attractive forces between unlike charges

### 12.1 COULOMB'S LAW

We know that there are two kinds of charges, namely, positive and negative charges. The charge on an electron is assumed to be negative and charge on a proton is positive. Moreover, we also learnt that like charges repel each other and unlike charges attract each other. Now we investigate the quantitative nature of these forces. The first measurement of the force between electric charges was made in 1874 AD by Charles Coulomb, a French military engineer. On the basis of these measurements, he deduced a law known as Coulomb's law. It states that

The force between two point charges is directly proportional to the product of the magnitudes of charges and inversely proportional to the square of the distance between them.

It is mathematically expressed as

$$F \propto \frac{q_1 q_2}{r^2}$$
 or  $F = k \frac{q_1 q_2}{r^2}$  ...... (12.1)

where F is the magnitude of the mutual force that acts on each of the two point charges  $q_1$ ,  $q_2$  and r is the distance between them. The force F always acts along the line joining the two point charges (Fig. 12.1), k is the constant of proportionality, its value depends upon the nature of medium between the two charges and system of units in which F, q and r are measured. If the medium between the two point charges is free space and the system of units is SI, then k is represented as

$$k = \frac{1}{4\pi\varepsilon_0} \qquad (12.2)$$

where ε, is an electrical constant, known as permittivity of free space. In SI units, its value is 8.85 × 10<sup>-12</sup> Nm<sup>-1</sup>C<sup>-2</sup>. Substituting the value of ε, the constant

$$k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}$$

Thus Coulomb's force in free space is

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$
 (12.3)

As stated earlier, Coulombs' force is mutual force, it means that if q, exerts a force on  $q_z$ , then  $q_z$  also exerts an equal and opposite force on  $q_z$ , if we denote the force exerted on  $q_z$  by  $q_z$  as  $F_{zz}$  and that on charge  $q_z$  due to  $q_z$  as  $F_{zz}$ , then

The magnitude of both these two forces is the same and is given by Eq. 12.3. To represent the direction of these forces we introduce unit vectors. If  $\hat{\mathbf{r}}_{2}$ , is the unit vector directed from  $q_1$  to  $q_2$  and  $\hat{\mathbf{r}}_{3}$  is the unit vector directed from  $q_3$  to  $q_4$ , then

and

$$\mathbf{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{\mathbf{r}}_{12} \dots 12.5 \text{ (b)}$$

The forces  $F_{21}$  and  $F_{12}$  are shown in Fig. 12.2 (a & b). It can be seen that  $\hat{r}_{21} = -\hat{r}_{121}$  so Eqs. 12.5 (a & b) show that

The sign of the charges in Eqs. 12.5 (a & b) determine whether the forces are attractive or repulsive.

We shall now consider the effect of medium between the two charges upon the Coulomb's force. If the medium is an insulator, it is usually referred as dielectric. It has been found that the presence of a dielectric always reduces the electrostatic force as compared with that in free space by a certain factor which is a constant for the given dielectric. This constant is known as relative permittivity and is represented by  $\varepsilon$ . The values of relative permittivity of different dielectrics are given in Table 12.1.

Thus the Coulomb's force in a medium of relative permittivity ε, is given by

$$F = \frac{1}{4\pi\varepsilon_0\varepsilon_r} \frac{q_t q_2}{r^2} \tag{12.6}$$

It can be seen in the table that a, for air is 1,0006. This value is so close to one that with negligible error, the Eq. 12.3 gives the electric force in air.

**Example 12.1:** Charges  $q_r = 100 \,\mu\text{C}$  and  $q_z = 50 \,\mu\text{C}$  are located in xy-plane at positions  $r_r = 3.0$  j and  $r_z = 4.0$  i respectively,

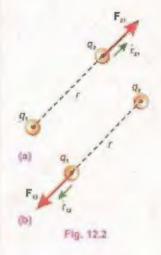


Table 2.1	
Material	21
Vacuum	1
Air (1 atm)	1,0008
Ammonia (liquid)	22-25
Bakelile	5-18
Benzene	2.284
Germanium	18
Glass	4.8-10
Mica	3-7.5
Paraffined paper	- 2
Plexiglas	3,40
Rubber	2.94
Teflon	2.1
Transformer oil	2.1
Water (distilled)	78.5

where the distances are measured in metres. Calculate the force on q (Fig. 12.3)

Solution: 
$$q_s = 100 \,\mu\text{C}$$
,  $q_s = 50 \,\mu\text{C}$ 

Position vector of q, relative to q,

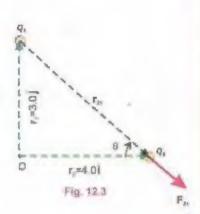
$$\begin{aligned} &= \mathbf{r}_{2} = \mathbf{r}_{2} - \mathbf{r}_{1} = 4 \cdot 1 - 3 \cdot \mathbf{j} \\ &r = \text{magnitude of } \mathbf{r}_{2} = \sqrt{(4 \, \text{m})^{2} + (-3 \, \text{m})^{2}} = 5 \, \text{m} \\ &\tilde{\mathbf{r}}_{2} = \frac{4 \cdot 1 - 3 \cdot \mathbf{j}}{5} \\ &\mathbf{F}_{2} = \frac{1}{4 \pi \epsilon_{0}} \frac{q_{1} q_{2}}{r^{2}} \, \tilde{\mathbf{r}}_{2} , \\ &9 \times 10^{9} \, \text{Nm}^{2} \text{C}^{-2} \times 100 \times 10^{-6} \, \text{C} \times 50 \times 10^{-6} \, \text{C} \times 4 \cdot 1 \end{aligned}$$

$$= \frac{9 \times 10^{9} \text{ Nm}^{2}\text{C}^{-2} \times 100 \times 10^{-6} \text{ C} \times 50 \times 10^{-6}\text{C}}{(5 \text{ m})^{2}} \times \frac{4 \text{ i} - 3 \text{ j}}{5}$$

$$= 1.44 \text{ i} - 1.08 \text{ j}$$

Magnitude of 
$$F_{21} = F = \sqrt{(1.44)^2 + (-1.08)^2} = 1.8 \text{ N}$$

Direction of 
$$F_{zz} = \tan^{-1} \left( \frac{-1.08}{1.44} \right) = -37^{\circ}$$
 with x - axis



### 12.2 FIELDS OF FORCE

Newton's universal gravitational law and Coulomb's law enable us to calculate the magnitude as well as the directions of the gravitational and electric forces, respectively. However one may question, (a) What are the origins of these forces? (b) How are these forces transmitted from one mass to another or from one charge to another?

The answer to (a) is still unknown; the existence of these forces is accepted as it is. That is why they are called basic forces of nature.

To describe the mechanism by which electric force is transmitted, Michael Faraday (1791-1867) introduced the concept of an electric field. According to his theory, it is the intrinsic property of nature that an electric field exists in the space around an electric charge. This electric field is considered to be a force field that exerts a force on other charges placed in that field. For example, a charge q produces an electric field in the space surrounding it. This

field exists whether the other charges are present in space or not. However, the presence of field cannot be tested until another charge  $q_o$  is brought into the field. Thus the field of charge q interacts with  $q_o$  to produce an electrical force. The interaction between q and  $q_o$  is accomplished in two steps: (a) the charge q produces a field and (b) the field interacts with charge  $q_o$  to produce a force  $\mathbf{F}$  on  $q_o$ . These two steps are illustrated in Fig. 12.4.

In this figure the density of dots is proportional to the strength of the field at the various points. We may define electric field strength or electric field intensity E at any point in the field as

$$\mathsf{E} = \frac{\mathsf{F}}{q_a} \tag{12.7}$$

where F is the force experienced by a positive test charge  $q_s$  placed at the point. The test charge  $q_s$  has to be very small so that it may not distort the field which it has to measure.

Since electric field intensity is force per unit charge, it is measured in newton per coulomb in SI units. It is a vector quantity and its direction is the same as that of the force F.

The force experienced by a test charge  $q_a$  placed in the field of a charge q in vacuum is given by Eq. (12.3). Eq. 12.7 can be used to evaluate electric intensity due to a point charge q at a point distant r from it. Place a positive test charge q, at this point. The Coulomb's force that this charge will experience due to q is

$$F = \frac{1}{4\pi\varepsilon_o} \frac{qq_o}{r^2} \hat{r} \qquad (12.8)$$

where  $\bar{r}$  is a unit vector directed from the point charge q to the test point where q, has been placed, i.e., the point where the electric intensity is to be evaluated. By Eq. 12.7

$$E = \frac{F}{q_0} = \frac{1}{4\pi\epsilon_0} \frac{qq_0}{r^2} \hat{\mathbf{r}} \times \frac{f}{q_0} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{\mathbf{r}} \qquad (12.9)$$

**Example 12.2:** Two positive point charges  $q_{\rm s}$  = 16.0  $\mu$ C and  $q_{\rm s}$  = 4.0  $\mu$ C are separated by a distance of 3.0 m, as shown in Fig. 12.5. Find the spot on the line joining the two charges where electric field is zero.

Solution: Between the charges, the two field contribution has opposite directions, and electric field would be zero at a

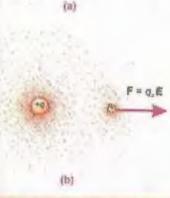


Fig. 12.4 (a) Dots surrounding the positive charge indicate the presence of the electric field. The density of the dots is proportional to the strength of the electric field at different points. (b) Interaction of the field with the charge q,

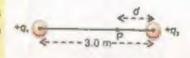
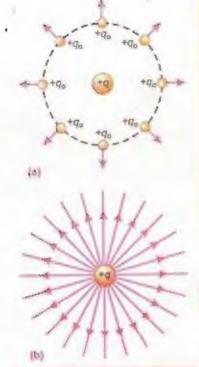


Fig. 12.5



placed grywhere in the vicinity of a positive point charge \*q. experiences a repulsive force directed radially outward from the electric field lines are directed radially outward from the positive point charge \*q.



Fig. 12.3 The electric field lines are directed radially inward towards a negative point charge -q.

point P, where the magnitude of E, equals that of E<sub>2</sub>. In the Fig. 12.5, let the distance of P from  $q_2$  be d.

A1P. 
$$E_1 = E_2$$
, which implies that,  

$$\frac{1}{4\pi\epsilon_o} \frac{q_i}{(3.0 - d)^2} = \frac{1}{4\pi\epsilon_o} \frac{q_2}{d^2}$$
or 
$$\frac{16.0 \times 10^{-6} \text{ C}}{9 + d^2 - 6d} = \frac{4.0 \times 10^{-6} \text{ C}}{d^2}$$

or  $d^2+2d-3=0$ , which gives  $d=+1 \text{ m}_a-3 \text{ m}$ 

There are two possible values of d, the negative value corresponds to a location off to the right of both the charges where magnitudes of E, and E, are equal but directions are same. In this case E, and E, do not cancel at this spot. The positive value corresponds to the location shown in figure and is the zero field location, hence, d=+1.0 m.

### 12.3 ELECTRIC FIELD LINES

A visual representation of the electric field can be obtained in terms of electric field lines; an idea proposed by Michael Faraday. Electric field lines can be thought of a "map" that provides information about the direction and strength of the electric field at various places. As electric field lines provide information about the electric force exerted on a charge, the lines are commonly called "lines of force".

To introduce electric field lines, we place positive test charges each of magnitude q, at different places but at equal distances from a positive charge +q as shown in the figure. Each test charge will experience a repulsive force, as indicated by arrows in Fig. 12.6(a). Therefore, the electric field created by the charge +q is directed radially outward. Fig. 12.6 (b) shows corresponding field lines which show the field direction. Fig. 12.7 shows the electric field lines in the vicinity of a negative charge -q. In this case the lines are directed radially "inward", because the force on a positive test charge is now of attraction, indicating the electric field points inward.

Figures 12.6 and 12.7 represent two dimensional pictures of the field lines. However, electric field lines emerge from the charges in three dimensions, and an infinite number of lines could be drawn.

The electric field lines "map" also provides information about

the strength of the electric field. As we notice in Figs. 12.6 and 12.7 that field lines are closer to each other near the charges where the field is strong while they continuously spread out indicating a continuous decrease in the field strength.

"The number of lines per unit area passing perpendicularly through an area is proportional to the magnitude of the electric field".

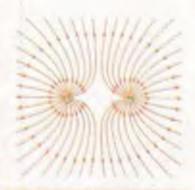
The electric field lines are curved in case of two identical separated charges. Fig.12.8 shows the pattern of lines associated with two identical positive point charges of equal magnitude. It reveals that the lines in the region between two like charges seem to repel each other. The behaviour of two identical negatively charges will be exactly the same. The middle region shows the presence of a zero field spot or neutral zone.

The Fig. 12.9 shows the electric field pattern of two opposite charges of same magnitudes. The field lines start from positive charge and end on a negative charge. The electric field at points such as 1, 2, 3 is the resultant of fields created by the two charges at these points. The directions of the resultant intensities is given by the tangents drawn to the field lines at these points.

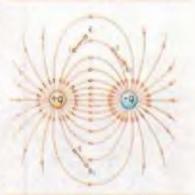
In the regions where the field lines are parallel and equally spaced, the same number of lines pass per unit area and therefore, field is uniform on all points. Fig. 12.10 shows the field lines between the plates of a parallel plate capacitor. The field is uniform in the middle region where field lines are equally spaced.

We are now in a position to summarize the properties of electric field lines.

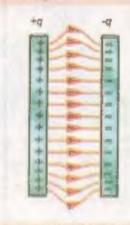
- Electric field lines originate from positive charges and end on negative charges.
- The tangent to a field line at any point gives the direction of the electric field at that point.
- The lines are closer where the field is strong and the lines are farther apart where the field is weak.
- 4) No two lines cross each other. This is because E has only one direction at any given point. If the lines cross, E could have more than one direction.



The electric field lines for two identical positive point charges.



Altractive forces between unlike charges

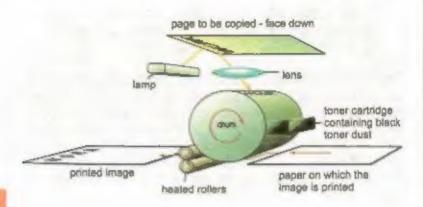


parallel plate capacitor the electric field lines are parallel and evenly spaced, indicating that the electric field there has the same magnitude and direction at all points.

### 12.4 APPLICATIONS OF ELECTROSTATICS

### (i) Xerography (Photocopier)

Fig.12.11 illustrates a photocopy machine. The copying



#### For Your Information



This computer Image shows the electric field lines generated by the fish at the top of the picture. Through the electric field, the presence of other fish can be detected, such as the one silhouetted at the bottom.

The basics of photocopying. The lamp transfers an image of the page to the drum, which leaves a static charge. The drum collects toner dust and transfers it to the page. The toner is meltad onto the page.

process is called xerography, from the Greek word "xeros" and "graphos", meaning "dry writing". The heart of machine is a drum which is an aluminium cylinder coated with a layer of selenium. Aluminium is an excellent conductor. On the other hand, selenium is an insulator in the dark and becomes a conductor when exposed to light; it is a photoconductor. As a result, if a positive charge is sprinkled over the selenium it will remain there as long as it remains in dark. If the drum is exposed to light, the electrons from aluminium pass through the conducting selenium and neutralize the positive charge.

If the drum is exposed to an image of the document to be copied, the dark and light areas of the document produce corresponding areas on the drum. The dark areas retain their positive charge, but light areas become conducting, lose their positive charge and become neutral.

In this way, a positive charge image of the document remains on the selenium surface. Then a special dry, black powder called "toner" is given a negative charge and spread over the drum, where it sticks to the positive charged areas.

The toner from the drum is transferred on to a sheet of paper on which the document is to be copied. Heated pressure

rollers then melt the toner into the paper which is also given an excess positive charge to produce the permanent impression of the document.

### (iii) Inkjet Printers

An inkjet printer (Fig. 12.12 a) is a type of printer which uses electric charge in its operation. While shuttling back and forth across the paper, the inkjet printer "ejects" a thin stream of ink. The ink is forced out of a small nozzle and breaks up into extremely small droplets. During their flight, the droplets pass through two electrical components, a "charging electrode" and the "deflection plates" (a parallel plate capacitor). When the printhead moves over regions of the paper which are not to be inked, the charging electrode is left on and gives the ink droplets a net charge. The deflection plates divert such charged drops into a gutter and in this way such drops are not able to reach the paper. Whenever ink is to be placed on the paper, the charging control, responding to computer, turns off the charging electrode. The uncharged droplets fly straight through the deflection plates and strike the paper. Schematic diagram of such a printer is shown by Fig. 12.12 (b).

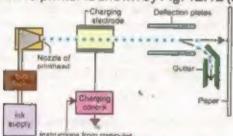


Fig. 12.12 to An inkiel printhead ejects a steady flow of ink droplets. The charging electrodes are used to charge the droplets that are not needed on the paper. Charged droplets are deflected into a gutter by the deflection pistes, while uncharged droplets the streight onto the paper.

Inkjet printers can also produce coloured copies.

### 12.5 ELECTRIC FLUX

When we place an element of area in an electric field, some of the lines of force pass through it (Fig. 12.13 a).

The number of the field lines passing through a certain element of area is known as electric flux through that area. It is usually denoted by Greek letter Φ. For example the flux Φ through the area A in Fig. 12.13 (a) is 4 while the flux through B is 2.

In order to give a quantitative meaning to flux, the field lines are drawn such that the number of field lines passing through



Fig. 12.12 (a) An Initial printer,

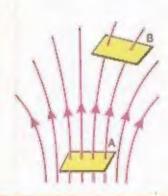


Fig. 12.13 (a) Electric flux through a surface normal to E.

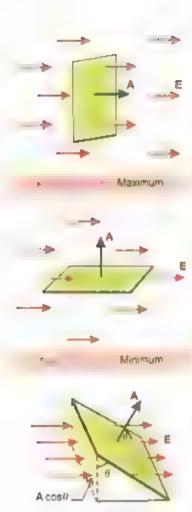


Fig. 12 13 (d)

a unit area held perpendicular to field lines at a point represent the intensity E of the field at that point. Suppose at a given point the value of E is 4NC. This means that if 1m² area is held perpendicular to field lines at this point. 4 field lines will pass through it. In order to establish relation between electric flux Φ, electric intensity E and area A we consider the Fig.12.13 (b,c,d) which shows the three dimensional representation of the electric field lines due to a uniform electric field of intensity E.

In Fig 12 13 (b) area is held perpendicular to the field lines, then EA lines pass through it. The flux **Q**, in this case is

$$\Phi_{\bullet} = EA \tag{12.10}$$

where A denotes that the area is held perpendicular to field lines in Fig. 12.13 (c), area A is held parallel to field lines and, as is obvious πρ knes cross this area, so that flux Φ, in this case is

$$\Phi_{\bullet} = EA_{\bullet} = 0$$
 ........ (12.11)

where A indicates that A is held parallel to the field lines. Fig 12 13 (d) shows the case when A is no ther perpendicular nor parallel to field lines but is inclined at angle 8 with the lines in this case we have to find the projection of the area which is perpendicular to the field lines. The area of this projection, (Fig. 12 13 d) is A cos 8. The flex Φ in this case is

$$\Phi_{\bullet} = EA\cos\theta$$

Usually the element of area is represented by a vector area A whose magnitude is equal to the surface area A of the element and whose direction is direction of normal to the area. The electric flux  $\Phi$ , through a patch of flat surface in terms of E and A is then given by

where  $\theta$  is the angle between the field lines and the normal to the area

Electric flux, being a scalar product, is a scalar quantity. Its SI unit is Nm<sup>2</sup>C.

### 12.6 ELECTRIC FLUX THROUGH A SURFACE ENCLOSING A CHARGE

Let us calculate the electric flux through a closed surface, in shape of a sphere of radius r due to a point charge q

praced at the centre of sphere as shown in Fig. 12.14. To apply the formula  $\Phi_{\bullet} = E$  A for the computation of electric flux, the surface area should be flat. For this reason the total surface area of the sphere is divided into n small patches with areas of magnitudes  $\Delta A_{i}$ ,  $\Delta A_{i}$ ,  $\Delta A_{i}$ , ....,  $\Delta A_{i}$ , if n is very large, each patch would be a flat element of area. The corresponding vector areas are  $\Delta A_{i}$ ,  $\Delta A_{i}$ ,  $\Delta A_{i}$ , ....,  $\Delta A_{i}$ , respectively. The direction of each vector area is along perpendicular drawn outward to the corresponding patch. The electric intensities at the centres of vector areas  $\Delta A_{i}$ ,  $\Delta A_{i}$ , ....,  $\Delta A_{i}$  are  $E_{i}$ ,  $E_{i}$ , .......  $E_{i}$  respectively.

According to Eq 12.12, the total flux passing through the closed surface is

$$\Phi_{a} = E_{a} \Delta A_{a} + E_{b} \Delta A_{a} + E_{b} \Delta A_{a} + E_{b} \Delta A_{a}$$
 (12.13)

The direction of electric intensity and vector area is same at each patch. Moreover, because of spherical symmetry at the surface of sphere,

$$|\mathbf{E}| = \mathbf{E}_{1}| = |\mathbf{E}_{3}| = |\mathbf{E}_{3}| = E = \frac{1}{4\pi\varepsilon_{0}} \frac{q}{r^{2}}$$

$$|\mathbf{\Phi}_{4}| = E\Delta A_{1} + E\Delta A_{3} + E\Delta A_{3} + \dots + E\Delta A_{n}$$

$$= E \times \langle \Delta A_{1} + \Delta A_{1} + \Delta A_{3} + \dots + \Delta A_{n} \rangle$$

$$= E \times (\text{total spherical surface area})$$

$$= \frac{1}{4\pi\varepsilon_{0}} \frac{q}{r^{2}} \times 4\pi r^{2}$$

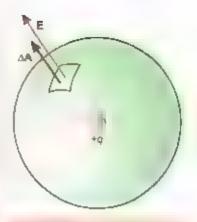
$$|\mathbf{\Phi}_{4}| = \frac{q}{\varepsilon_{0}}$$

$$|\mathbf{\Phi}_{5}| = \frac{q}{\varepsilon_{0}}$$
(12.15)

Now magine that a closed surface S is enclosing this sphere it can be seen in Fig 12.15 that the flux through the closed surface S is the same as that through the sphere. So we can conclude that total flux through a closed surface does not depend upon the shape or geometry of the closed surface. It depends upon the medium and the charge enclosed.

#### 12.7 GAUSS'S LAW

Suppose point charges  $q_n q_n q_n \dots q_n$  are arbitrarily distributed in an arbitrary shaped closed surface as shown in Fig. 12.16. Using dealgiven in previous section, the electric flux passing through the closed surface is



F 7 / The total electric flux through the surface of the sphere due to in charge q at its centre is q. c.

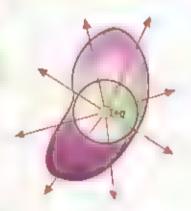


Fig. 12.15

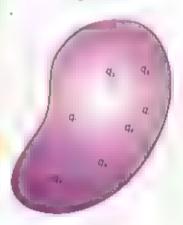


Fig. 12.16

$$\Phi_{a} = \frac{q_{1}}{\varepsilon_{0}} + \frac{q_{2}}{\varepsilon_{0}} + \frac{q_{3}}{\varepsilon_{0}} + \dots + \frac{q_{n}}{\varepsilon_{0}}$$

$$\Phi_{e} = \frac{1}{\varepsilon_{0}} \times (q_{1} + q_{2} + q_{3} + \dots + q_{n})$$

 $\Phi_{e} = \frac{1}{\epsilon_{\sigma}} \times (q_{1} + q_{2} + q_{3} + \cdots + q_{n})$   $\Phi_{e} = \frac{1}{\epsilon_{\sigma}} \times (\text{total charge enclosed by closed surface})$ 

$$\Phi_{\bullet} = \frac{1}{\epsilon_{0}} \times Q$$
 ...... (12 16)

where  $Q = q_1 + q_2 + q_3 + \dots + q_n$ , is the total charge enclosed by closed surface. Eq. 12.16 is mathematical expression of Gauss's law which can be stated as,

> "The flux through any closed surface is 1/s, times the total charge enclosed in it".

### 12.8 APPLICATIONS OF GAUSS'S LAW

Gauss's law is applied to calculate the electric intensity due to different charge configurations. In all such cases, an maginary closed surface is considered which passes through the point at which the electric intensity is to be evaluated. This closed surface is known as Gaussian surface. Its choice is such that the flux through it can be easily evaluated. Next the charge enclosed by Gaussian surface is calculated and finally the electric intensity is computed by applying Gauss's law Eq 12 16. We will illustrate this procedure by considering some examples.



Suppose that a hollow conducting sphere of radius R is given a positive charge g. We wish to calculate the field intensity first at a point inside the sphere

Now imagine a sphere of radius R < R to be inscribed within the hollow charged sphere as shown in Fig. 12.17. The surface of this sphere is the Gaussian surface. Let Φ be flux through this closed surface. It can be seen in the figure that the charge enclosed by the Gaussian surfaces is zero Applying Gaussian law, we have

$$\Phi_{\bullet} = \frac{q}{E_{o}} = 0$$

Φ.=E.A=0 as A≠0, therefore, Since

Thus the interior of a hollow charged metal sphere is a field free region. As a consequence, any apparatus placed within a metal enclosure is "shielded" from electric fields.



Suppose we have a plane sheet of infinite extent on which positive charges are uniformly distributed. The uniform surface charge density is, say, or A finite part of this sheet is shown in Fig. 12.18. To calculate the electric intensity E at a point P close to the sheet imagine a closed Gaussian surface in the form of a cylinder passing through the sheet, whose one flat face contains point P. From symmetry we can conclude that E points at right angle to the end faces and away from the plane. Since E is parallel to the curved surface of the cylinder, so there is no contribution to flux from the curved wall of the cylinder. While It will be, EA + EA = 2 EA, through the two flat end faces of the closed cylindrical surface, where A is the surface area of the flat faces (Fig. 12.18). As the charge enclosed by the closed surface is of A, therefore, according to Gauss's law,

$$\Phi_{*} = \frac{1}{\epsilon_{o}} \times \text{charge enclosed by closed surface}$$

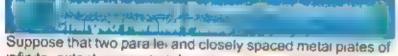
$$\Phi_{*} = \frac{1}{\epsilon_{o}} \times \sigma A. \qquad (12.17)$$

Therefore, 
$$2EA = \frac{1}{\epsilon_o} \times dA$$

or 
$$E = \frac{\sigma}{2c_o}$$
 (12.18)

In vector form, 
$$\mathbf{E} = \frac{\sigma}{2\nu_0}\hat{\mathbf{r}}$$
 (12.19)

where r is a unit vector normal to the sheet directed away from it



Suppose that two parallel and closely spaced metal plates of infinite extent separated by vacuum are given opposite charges. Under these conditions the charges are essentially concentrated on the inner surfaces of the plates. The field lines which originate on positive charges on the inner face of one plate terminate on negative charges on the inner face of the other plate (Fig. 12.19). Thus the charges



To etiminate stray electric field interference circuits of sensitive electronics devices such as TV and Computers are often enclosed within metal boxes.

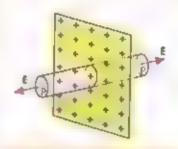
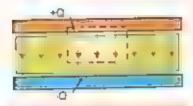


Fig. 14, 18. The closed surface is in the form of a cylinder whose one lace contains the point P at which electric intensity has to be determined.



f g 12 \*9 The lines of force between the plates are normal to the plates and are directed from the positive plate towards the negative one



P Dotted rectangle represents the cross section of Gaussian box with its top inside the upper metal place and its bottom in the diefactric between the plates.

are uniformly distributed on the inner surface of the plate in a form of sheet of charges of surface density  $\sigma = q/A$ , where A is the area of plate and q is the amount of charge on either of the plates

Imagine now a Gaussian surface in the form of a hollow box with its top inside the upper metal plate and its bottom in the space between the plates as shown in Fig 12.20. As the field lines are parallel to the sides of the box, therefore, the flux through the sides is zero. The field lines are uniformly distributed on the lower bottom face and are directed normally to it. If A is the area of this face and E the electric intensity at its site, the flux through it would be EA. There is no flux through the upper end of the box because there is no field inside the metal prate. Thus the total flux  $\Phi$ , through the Gaussian surface is EA. The charge enclosed by the Gaussian surface is  $\sigma$ A. Applying Gauss's law

$$\Phi_{\nu} = \frac{1}{\epsilon_{0}} \times \sigma A$$
or
$$EA = \frac{1}{\epsilon_{0}} \times \sigma A$$
or
$$E = \frac{\sigma}{\epsilon_{0}} \qquad (12.20)$$

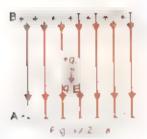
The field intensity is the same at all points between the plates. The direction of field is from positive to negative plate because a unit positive charge anywhere between the plates would be repelled from positive and attracted to negative plate and these forces are in the same direction. In vector form

$$\mathbf{E} = \frac{\sigma}{\varepsilon_0} \hat{\mathbf{f}}$$
 (12.21)

where ris a unit vector directed from positive to negative plate

### 12.9 ELECTRIC POTENTIAL

Let us consider a positive charge q, which is allowed to move in an electric field produced between two oppositely charged parallel plates as shown in Fig. 12.21 (a). The positive charge will move from plate B to A and will gain K.E. If it is to be moved from A to B, an external force is needed to make the charge move against the electric field and will gain P.E. Let us impose a condition that as the charge is moved from A to B, it is moved keeping electrostatic equilibrium. Let it moves with uniform velocity. This condition could be achieved by applying a force F equal and opposite to q,E at every point along its path



as shown in Fig. 12.21 (b). The work done by the external force against the electric field increases electrical potential energy of the charge that is moved.

Let  $W_{\rm ag}$  be the work done by the force in carrying the positive charge  $q_a$  from A to B while keeping the charge in equilibrium. The change in its potential energy  $\Delta U = W_{\rm ag}$ 

or 
$$U_a - U_A = W_{AB}$$
 (12.22)

where  $U_{\star}$  and  $U_{e}$ , are defined to be the potential energies at points A and B, respectively.

To describe electric field we introduce the idea of electric potential difference. The potential difference between two points A and B in an electric field is defined as the work done in carrying a unit positive charge from A to B while keeping the charge in equilibrium, that is,

$$\Delta V = V_0 - V_A - \frac{W_{AB}}{Q_0} = \frac{\Delta U}{Q_0}$$
 (12 23)

where V<sub>s</sub> and V<sub>s</sub> are defined electric potentials at point A and B respectively. Electric potential energy difference and electric potential difference between the points A and B are related as

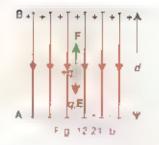
$$\Delta U = q_o \Delta V = W_{AB} \qquad (12.24)$$

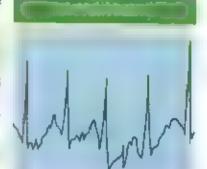
Thus the potential difference between the two points can be defined as the difference of the potential energy per unit charge.

As the unit of PE is joule, Eq. 12.23 shows that the unit of potential difference is joule per coulomb, it is called volt such that,

That is, a potential difference of 1 volt exists between two points if work done in moving a unit positive charge from one point to other, keeping equilibrium, is one joule.

In order to give a concept of electric potential at a point in an electric field, we must have a reference to which we assign zero electric potential. This point is usually taken at infinity. Thus in Eq. 12.23, if we take A to be at infinity and choose  $V_a = 0$ , the electric potential at B will be  $V_a = W_{xx}/q$ , or dropping the subscripts.





An ECG records the "voitage" between points on human skin generated by electrical process in the heart. This ECG is made in running position providing information about the heart's performance under stress.

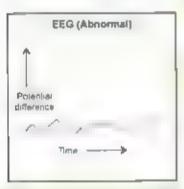


TE VERY TO LOW MANNEY

Time

Polenbar

difference



or

In a ectroencepha ography the potential differences created by the ejectrical activity of the brain are used for diagnosing abnormal bahaviour

which states that the electric potential at any point in an electric field is equal to work done in bringing a unit positive charge from infinity to that point keeping it in equilibrium, it is to be noted that potential at a point is still potential difference between the potential at that point and potential at infinity. Both potential and potential differences are scalar quantities because both Wand q<sub>a</sub> are scalars.

#### Electric Field as Potential Gra

In this section we will establish a relation between electric intensity and potential difference. As a special case, let us consider the situation shown in Fig. 12.21 (b). The electric field between the two charged plates is uniform, let its value be E. The potential difference between A and B is given by the equation.

$$V_a V_{\lambda} = \frac{W_{AB}}{Q_0} \tag{12.27}$$

where  $W_{sq} = Fd - \cdot q.Ed$  (the negative sign is needed because F must be applied opposite to q.E so as to keep it in equilibrium). With this, Eq. 12.27 becomes

$$V_{\theta} \cdot V_{A} = -\frac{Q_{\alpha}Ed}{Q_{\phi}} = -Ed$$

$$E = -\frac{(V_{B} \cdot V_{A})}{d} = -\frac{\Delta V}{d}$$
 (12.28)

If the plates A & B are separated by infinitesimally small distance  $\Delta r$ , the Eq. 12 28 is modified as

$$E = \frac{\Delta V}{\Delta r} \tag{12.29}$$

The quantity  $\frac{\Delta V}{\Delta r}$  gives the maximum value of the rate of change of potential with distance because the charge has been moved along a field line along which the distance  $\Delta r$  between the two plates is minimum. It is known as potential gradient. Thus the electric intensity is equal to the negative of the gradient of potential. The negative sign indicates that the direction of E is along the decreasing potential.

The unit of electric intensity from Eq. 12.29 is volt/metre which is equal to NC 1 as shown below:

### Charge

Let us derive an expression for the potential at a certain point in the field of a positive point charge q. This can be accomplished by bringing a unit positive charge from infinity to that point keeping the charge in equilibrium. The target can be achieved using Eq. 12.29 in the form  $\Delta V = -E \Delta r$ , provided electric intensity E remains constant. However in this case E varies inversely as square of distance from the point charge, it no more remains constant so we use basic principles to compute the electric potential at a point. The field is radial as shown in Fig. 12.22.

Let us take two points A and B, infinitesimally close to each other, so that E remains a most constant between them. The distance of points A and B from q are  $r_s$  and  $r_s$  respectively and distance of midpoint of space interval between A and B is r from q. Then according to Fig. 12.22.

$$r_{\theta} = r_{A} + \Delta r \tag{12.30}$$

$$\Delta r = r_a - r_a \tag{12.31}$$

As r represents mid point of interval between A and B so

$$r = \frac{r_A + r_B}{2}$$
 ....... (12.32)

The magnitude of electric intensity at this point is.

$$\mathcal{E} = \frac{1}{4\pi\epsilon_0} \frac{\mathbf{q}}{r^2} \qquad \dots \tag{12.33}$$

As the points A and B are very close then, as a first approximation, we can take the arithmetic mean to be equal o geometric mean which gives

$$\frac{r}{r_A} = \frac{r_B}{r}$$

$$r^2 = r_B r_B \tag{12.34}$$

Thus, Eq. 12.33 can be written as

Therefore,

$$E = \frac{1}{4\pi\epsilon_o} \frac{q}{r_A r_B}$$
 ...... (12.35)

Now if a unit positive charge is moved from B to A, the work tone is equal to the potential difference between A and B.

$$V_A - V_B = -E(r_A - r_B)$$





Fish and other sea creatures produce electric fields in a vallety of ways. Sharks have special agains called the ampoliae of cure rain; that are more seasive to electric field and can defect potential difference of the order of randoot and can locale their prey very precisely.

$$V_{a} - V_{a} = E(r_{a} - r_{a})$$
 (12.36)

Substituting value of E from Eq. 12.35,

$$V_{A}-V_{B}=\frac{q}{4\pi\varepsilon_{D}}\left(\frac{r_{B}-r_{A}}{r_{A}r_{B}}\right) \dots (12.37)$$

$$V_A - V_B = \frac{q}{4\pi\epsilon_0} \left( \frac{1}{r_A} - \frac{1}{r_B} \right) \dots$$
 (12.38)

To calculate absolute potential or potential at A, point B is assumed to be infinity point so that  $V_{\rm e}=0$  and hence

$$\frac{1}{r_{a}} = \frac{1}{r_{a}} = \frac{1}{r_{a}} = 0$$

$$V_{A} = \frac{1}{4\pi\epsilon_{a}} \frac{q}{r_{A}}$$
 (12.39)

The general expression for electric potential  $V_n$  at a distance r from q is.

$$V_{r} = \frac{1}{4\pi\varepsilon_{0}} \frac{q}{r} \tag{12.40}$$

Example 12.3: Two opposite point charges each of magnitude q are separated by a distance 2d. What is the electric potential at a point P mid-way between them?

Solution:

This gives,

$$V' = \frac{1}{4\pi\epsilon_o} \frac{q}{d} \quad \text{&} \quad V = -\frac{1}{4\pi\epsilon_o} \frac{q}{d}$$

$$V = V' + V' = \frac{1}{4\pi\epsilon_o} \frac{q}{d} \cdot \frac{1}{4\pi\epsilon_o} \frac{q}{d} = 0$$

So potential at P due to opposite charges is zero

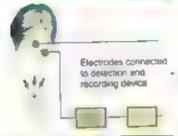
### 12.10 ELECTRON VOLT

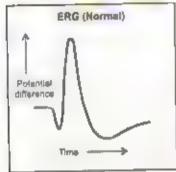
Referring Fig. 12.21 we know that when a particle of charge q moves from point A with potential  $V_s$  to a point 8 with potential  $V_s$  keeping electrostatic equilibrium, the change in potential energy  $\Delta U$  of particle is.

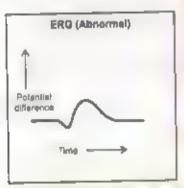
$$\Delta U = q(V_0 - V_A) = q \Delta V \qquad \dots (12.41)$$

If no external force acts on the charge to maintain equilibrium this charge in PE appears in the form of charge in KE Suppose charge carried by the particle is  $q = e = 1.6 \times 10$  °C









The electrical activity of the retina of the eye generates the potential differences used in electroretinography.

Thus, in this case, the energy acquired by the charge will be

$$\Delta K.E = q\Delta V = e\Delta V = (1.6 \times 10^{-10}C)(\Delta V)$$

Moreover assume that ∆V = 1 volt\_hence

$$\Delta K.E = q \Delta V = (1.6 \times 10^{-15} C) \times (1 \text{ volt})$$

$$\Delta K.E = (1.6 \times 10^{-16}) \times (C \times V) = 1.6 \times 10^{-16} J$$

The amount of energy equal to 1.6 x 10<sup>19</sup> J is called one electron-volt and is denoted by 1eV. It is defined as "the amount of energy acquired or lost by an electron as it traverses a potential difference of one volt". Thus,

Example 12.4: A particle carrying a charge of 2e falls through a potential difference of 3 0V. Calculate the energy acquired by it.

Solution: q = 2e  $\Delta V = 3.0 V$ 

The energy acquired by the particle is

$$\Delta K.E = q \Delta V = (2e)(3.0 \text{ V}) = 6.0 \text{ eV}$$

### 12.11 ELECTRIC AND GRAVITATIONAL FORCES (A COMPARISON)

In chapter 4, we pointed out that gravitational force is a conservative force, that is, work done in such a field is independent of path. It can also be proved that Coulomb's electrostatic force is also conservative force. The electric

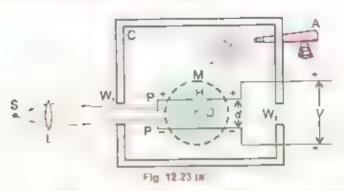
force between two charges  $F = \frac{q_1 q_2}{4\pi\epsilon_0 r^2}$ , is similar in form to

the gravitational force between the two point masses.  $F = G \frac{m_1 m_2}{r^2}$  Both forces vary inversely with the square of the

fact that the gravitational force is a very weak force as compared to electrostatic force. As regards their qualitative aspect, the electrostatic force could be attractive or repulsive while, on the other hand, gravitational force is only attractive. Another difference to be noted is that the electrostatic force is medium dependant and can be shielded while gravitational.

### 12.12 CHARGE ON AN ELECTRON BY MILLIKAN'S METHOD

to 1909, R.A Millikan devised a technique that resulted in precise measurement of the charge on an electron.



A schematic diagram of the Millikan oil drop experiment is shown in Fig. 12.23 (a). Two parallel plates PP, are placed inside a container C, to avoid disturbances due to air currents. The separation between the plates is d. The upper plate P has a small hole H, as shown in the figure. A voltage V is applied to the plates due to which the electric field E is setup between the plates. The magnitude of its value is E = V/d An atomizer A is used for spraying oil drops into the container through a nozzie. The oil drop gets charged because of friction between walls of atomizer and oil drops These oil drops are very small, and are actually in the form of mist. Some of these drops happen to pass through the hole in the upper plate. The space between the plates is illuminated. by the light coming from the source S through the lens L and window W, The path of motion of these drops can be carefully observed by a microscope M.

A given droplet between the two plates could be suspended in air if the gravitational force  $F_0 = mg$  acting on the drop is equal to the electrical force  $F_1 = qE$  as shown in Fig. 12.23(b). The  $F_1$  can be adjusted equal to  $F_2$  by adjusting the voltage. In this case, we can write,

If V is the value of pild between the plates for this setting, then



Fig. 12.71 in On grop parameted by the gray a pray rouse a 2 fre Coulomb force.

or

$$E = \frac{V}{d}$$
, we may write  $q \frac{V}{d} = mg$ 

$$q \frac{mgd}{V}$$
(12.44)

in order to determine the mass m of the droplet, the electric field between the plates is switched off. The droplet falls under the action of gravity through air. It attains terminal speed v almost at the instant the electric field is switched off. Its terminal speed v, is determined by timing the fall of the droplet over a measured distance. Since the drag force F due to air acting upon the droplet when it is falling with constant terminal speed is equal to its weight. Hence, using Stokes's law.

$$F = 6\pi\eta r v_s = mg$$

where r is the radius of the droplet and  $\eta$  is the coefficient of viscosity for air. If  $\rho$  is the density of the droplet, then

$$m = \frac{4}{3}\pi r^3 \rho$$
 ...... (12.45)

Hence, 
$$\frac{4}{3}\pi r^3 \rho g = 6\pi \eta r V_1$$
or 
$$r^2 = \frac{9\pi V_1}{2\rho g}$$

Knowing the value of r, the mass m can be calculated by using Eq. (12.45). This value of m is substituted in Eq. 12.44 to get the value of charge q on the droplet.

Mill kan measured the charge on many drops and found that each charge was an integral multiple of a minimum value of charge equal to 1.6 x 10  $^{\circ}$  C. He therefore, concluded that this minimum value of the charge is the charge on an electron.

**Example 12.5:** In Millikan oil drop experiment, an oil drop of mass 4.9 x 10.1 kg is balanced and held stationary by the electric field between two parallel plates. If the potential difference between the plates is 750 V and the spacing between them is 5.0 mm calculate the charge on the droplet. Assume  $g = 9.8 \, \mathrm{ms}^{-2}$ 

#### Solution:

Mass of drop = m = 4.9 x 10 18 kg

Potential difference = V = 750 V

Spacing between plates =  $d = 5.0 \text{ mm} = 5.0 \text{ x } 10^{3} \text{ m}$ 

For the droplet of the charge q, we have

### 12.13 CAPACITOR

A capacitor is a device that can store charge. It consists of two conductors placed near one another separated by vacuum, air or any other insulator, known as dielectric. Usually the conductors are in the form of parallel plates, and the capacitor is known as parallel plate capacitor. When the plates of such a capacitor are connected to a battery of voltage V (Fig 12.24), it establishes a potential difference of V volts between the two plates and the battery places a charge +Q on the plate connected with its positive terminal and a charge-Q on the other plate connected to its negative terminal let Q be the magnitude of the charge on either of the plates. It is found that

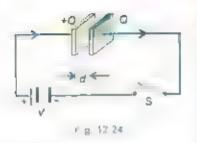
$$Q = V$$
 or  $Q = CV$  or  $C = \frac{Q}{V}$  ..... (12.46)

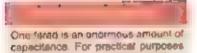
The proportionality constant C is called the capacitance of the capacitor. As we shall see rater, it depends upon the geometry of the plates and the medium between them it is a measure of the ability of capacitor to store charge. The capacitance of a capacitor can be defined as the amount of charge on one plate necessary to raise the potential of that plate by one volt with respect to the other. The SI unit of capacitance is coulombling per volt which because of its frequent use, is commonly called farad (F), after the famous English scientist Faraday.

"The capacitance of a capacitor is one farad if a charge of one coulomb, given to one of the plates of a parallel plate capacitor, produces a potential difference of one volt between them".

### 12.14 CAPACITANCE OF A PARALLEL PLATE CAPACITOR

Consider a parallel prate capacitor consisting of two plane metal plates, each of area A separated by a distance d as shown in Fig. 12.24. The distance d is small so that the electric field E between the plates is uniform and confined





its sub-multiple units are used which

are given below 1 micro-fared = 1µF = 10<sup>4</sup> fared 1 pico-fared = 1 pF = 10<sup>17</sup> fared almost entirely in the region between the plates. Let initially the medium between the plates be air or vacuum. Then according to Eq. 12.46,

$$C_{\rm opc} = \frac{Q}{V} \tag{12.47}$$

where Q is the charge on the capacitor and V is the potential difference between the parallel plates. The magnitude E of electric intensity is related with the distance d by Eq. 12.28 as

$$\mathcal{E} = \frac{V}{d} \tag{12.48}$$

As Q is the charge on either of the plates of area A the surface density of charge on the plates is as

As already shown in section 12.8, the electric intensity between two oppositely charged plates is given by  $E = \frac{\sigma}{\epsilon_{\sigma}}$ . Substituting the value of  $\sigma$ , we have

$$\frac{V}{d} = \frac{Q}{A\epsilon_0}$$
 ...... (12.49)

It gives

If an insulating material, called dielectric, of relative permittivity  $\varepsilon$ , is introduced between the plates, the capacitance of capacitor is enhanced by the factor  $\varepsilon$ . Capacitors commonly have some dielectric medium, thereby  $\varepsilon$ , is also called as dielectric constant.

Following experiment gives the effect of insertion of dielectric between the plates of a capacitor

Consider a charged capacitor whose plates are connected to a voltmeter (Fig. 12.25 a). The deflection of the meter is a measure of the potential difference between the plates. When a dielectric material is inserted between the plates, reading drops indicating a decrease in the potential difference between the plates (Fig. 12.25 b). From the definition, C = Q/V, since V decreases while Q remains constant, the value of Cincreases. Then Eq. 12.50 becomes,

$$C_{\text{max}} = \frac{A\varepsilon_{q}\varepsilon_{r}}{d} \qquad \dots (12.51)$$

### For Your Information



The electric field knee between the plates of a parallel-plate capacitor. Small bits of thread are suspended in oil and become aligned with the electric field. Note that the lines are equally spaced, indicating that the electric field there is uniform.

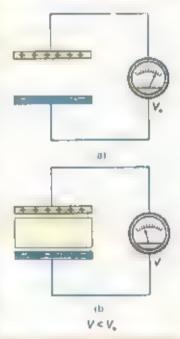


Fig. 12.25 Effect of a dielectric on the capacitance of a capacitor.

Eq.12.50 shows the dependence of a capacitor upon the area of plates, the separation between the plates and medium between them

Dividing Eq.12.51 by Eq.12.50 we get expression for dielectric constant as.

$$\varepsilon_{,=} \stackrel{C_{mad}}{=}$$
 (12.52)

From Eq 12.52 dielectric co-efficient or dielectric constant is defined as

"The ratio of the capacitance of a parallel plate capacitor with an insulating substance as medium between the plates to its capacitance with vacuum (or air) as medium between them".

### 12.15 ELECTRIC POLARIZATION OF DIELECTRICS

The increase in the capacity of a capacitor due to presence of dielectric is due to electric polarization of dielectric.

The dielectric consists of atoms and molecules which are electrically neutral on the average i.e., they contain equaamounts of negative and positive charges. The distribution of these charges in the atoms and molecules is such that the centre of the positive charge coincides with the centre of negative charge. When the molecules of dielectric are subjected to an electric field between the plates of a capacitor, the negative charges (electrons) are attracted towards the positively charged plate of the capacitor and the positive charges (nuclei) towards the negatively charged plate. The electrons in the dielectric (insulator) are not free to move but it is possible that the electrons and nuclei can undergo slight displacement when subjected to an electric field. As a result of this displacement the centre of positive and negative charges now no longer coincide with each other end one end of molecules shows a negative charge and the other end, an equal amount of positive charge but the molecule as a whole is still neutral. Two equal and opposite charges separated by a small distance are said to constitute a dipole. Thus the molecules of the dielectric under the action. of electric field become dipoles and the dielectric is said to be polarized

The effect of the polarization of dielectric is shown in



A collection of capacitors used in various appliances

Fig. 12.26. The positively charged plate attracts the negative end of the molecular dipoles and the negatively charged plate attracts the positive end. Thus the surface of the dielectric which is in contact with the positively charged plate places a layer of negative charges on the plate. Similarly the surface of the dielectric in contact with the negatively charged plate places a layer of positive charges. It effectively decreases the surface density of the charge of on the plates. As the electric intensity E between the plates is  $\frac{\sigma}{\epsilon}$  so E decreases due to

polarization of the dielectric. This results into a decrease of potential difference between the piates due to presence of dielectric as demonstrated by the experiment described in the previous section.

### 12.16 ENERGY STORED IN A CAPACITOR

A capacitor is a device to store charge. Alternatively, it is possible to think of a capacitor as a device for storing electrical energy. After all, the charge on the plate possesses electrical potential energy which arises because work is to be done to deposit charge on the plates. This is due to the fact that with each small increment of charge being deposited during the charging process, the potential difference between the plates increases, and a larger amount of work is needed to bring up next increment of charge.

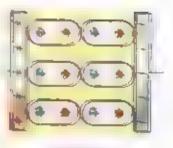
Initially when the capacitor is uncharged, the potential difference between plates is zero and finally it becomes V when q charge is deposited on each plate. Thus, the average

potential difference is 
$$\frac{0+V}{2} = \frac{1}{2}V$$
  
Therefore  $PE = Energy = \frac{1}{2} qV$ 

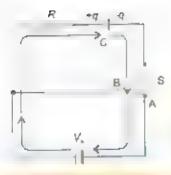
Using the relation q = CV for capacitor we get

Energy = 
$$\frac{1}{2}$$
 CV<sup>2</sup> ........... (12.53)

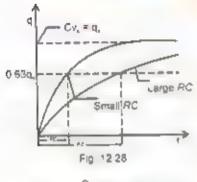
It is also possible to regard the energy as being stored in electric field between the plates, rather than the potential energy of the charges on the plates. Such a view point is useful when electric field strength between the plates instead of charges on the plates causing field is to be considered. This relation can be obtained by substituting V = Ed and  $C = A_{E,E}/d$  in Eq. 12.53,

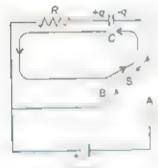


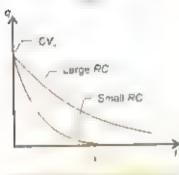
F a 2.26



I Charging a capacitor







Energy = 
$$\frac{1}{2} \left( \frac{A_{E_r} \varepsilon_a}{d} \right) (Ed)^2$$
  
=  $\frac{1}{2} \varepsilon_r \varepsilon_o E^2 \times (Ad)$ 

As (Ad) is volume between the plates so

Energy density 
$$\frac{Energy}{Volume} = \frac{1}{2} \varepsilon_1 \varepsilon_2 \varepsilon_3$$
 (12 54)

This equation is valid for any electric field strength.

### 12.17 CHARGING AND DISCHARGING A CAPACITOR

Many electric circuits consist of both capacitors and resistors Fig 12.27 shows a resistor-capacitor circuit called R.C-circuit. When the switch S is set at terminal A, the R-C combination is connected to a battery of voltage V, which starts charging the capacitor through the resistor R.

The capacitor is not charged immediately, rather charges build up gradually to the equilibrium value of  $q_a = CV_a$ . The growth of charge with time for different resistances is shown in Fig 12.28. According to this graph q=0 at t=0 and increases gradually with time till it reaches its equilibrium value  $q_a = CV_a$ . The voltage V across capacitor at any instant can be obtained by dividing q by C, as V = q/C.

How fast or how slow the capacitor is charging or discharging, depends upon the product of the resistance R and the capacitance C used in the circuit. As the unit of product RC is that of time, so this product is known as time constant and is defined as the time required by the capacitor to deposit 0.63 times the equilibrium charge  $q_{\rm u}$ . The graphs of Fig. 12.28 show that the charge reaches its equilibrium value sooner when the time constant is small.

Fig. 12.29(a) illustrates the discharging of a capacitor through a resistor. In this figure, the switch S is set at point B, so the charge +q on the left plate can flow anti-clockwise through the resistance and neutralize the charge -q on the right plate.

The graphs in Fig. 12 29(b) shows that discharging begins at t=0 when  $q\in CV$ , and decreases gradually to zero. Smaller values of time constant RC ead to a more rapid discharge.

**Example 12.6:** The time constant of a series RC circuit is t = RC. Verify that an ohm times farad is equivalent to second

**Solution:** Ohm's law in terms of potential difference *V*, current *l* and resistance *R* can be written as,

Putting I = q/t, this equation transforms into the equation,

OF.

$$R = \frac{V \times V}{a}$$

According to equation q = CV, C = q/V

Mult plying this equation with above equation gives,

$$RC = \frac{V \times t}{q} \times \frac{q}{V} = t$$

Hence 1 ohm x 1 farad = 1 second

where ohm is the unit of resistance R



And the second second

The charging discharging of a capacitor enables some windshield wipers of cars to be used intermittently during a light drizzle. In this mode of operation the wipers remain off for a while and then turn on briefly. The timing of the on-off cycle is determined by the time constant of a resistor-capacitor combination.

The Coulomb's law states that the force between two point charges is directly proportional to the product of the magnitudes of charges and inversely proportional to the square of the distance between them

- Electric field force per unit charge at a point is called electric field strength or electric field intensity at that point.
- The number of the field lines passing through a certain element of area is known as electric flux through that area, denoted by Φ.
- The electric flux Φ through a vector area A, in the electric field of intensity E is given by
  Φ = E.A = EA cosθ, where θ is the angle between the field lines and the normal to
  surface area.

Gauss's law is stated as "the flux through any closed surface is  $1/\epsilon_{\rm s}$  times the total charge enclosed in it.

- The interior of a hollow charged metal sphere is a field free region.
- The electric intensity between two oppositely charged parallel plates is E =
- The amount of work done in bringing a unit positive charge from infinity to a point against electric field is the electric potential at that point

- Capacitance of a capacitor is a measure of the ability of a capacitor to store charge
- The capacitance of a parallel plate capacitor is  $C_{\infty} = \frac{Q}{V} = \frac{A}{M}$
- The increase in the capacitance of a capacitor due to presence of dielectric is due to electric polarization of the dielectric.



The potential is constant throughout a given region of space is the electrical field zero or non-zero in this region? Explain.

Suppose that you follow an electric field line due to a positive point charge. Do electric field and the potential increase or decrease?

How can you identify that which plate of a capacitor is positively charged?

Describe the force or forces on a positive point charge when placed between parallel plates

with similar and equal charges

with opposite and equal charges

Electric lines of force never cross. Why?

If a point charge q of mass m is released in a non-uniform electric field with field lines pointing in the same direction, will it make a rectilinear motion?

is Einecessarily zero inside a charged rubber balloon if balloon is spherical? Assume that charge is distributed uniformly over the surface.

Is it true that Gauss's law states that the total number of lines of forces crossing any closed surface in the outward direction is proportional to the net positive charge enclosed within surface?

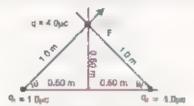
12.9 Do electrons tend to go to region of high potential or of low potential?



12.1 Compare magnitudes of electrical and gravitational forces exerted on an object (mass = 10.0 g, charge = 20.0 μC) by an identical object that is placed 10.0 cm from the first. (G = 6.67 x 10" Nm²kg²)

(Ana: 
$$\frac{F_0}{F_0} = 5.4 \times 10^{14}$$
)

17.7 Calculate vectorally, the net electrostatic force on q as shown in the figure



(Ans: F = 0.058 iN)

- A point charge  $q = -8.0 \times 10^{4}$  C is placed at the origin. Calculate electric field at a point 2.0 m from the origin on the z-axis. [Ans: (-1.8 x10<sup>2</sup> kgNC')]
- Determine the electric field at the position  $\mathbf{r} = (4\hat{\mathbf{i}} + 3\hat{\mathbf{j}})$  m caused by a point charge  $q = 5.0 \times 10^4$  C placed at origin [Ans:  $(1440\hat{\mathbf{i}} + 1080\hat{\mathbf{j}})$  N C']
- Two point charges,  $q_1 = -1.0 \times 10^6$  C and  $q_2 = +4.0 \times 10^6$  C, are separated by a distance of 3.0 m. Find and justify the zero-field location. (Ans: 3.0 m)
- 12.6 Find the electric field strength required to hold suspended a particle of mass 1.0 x10 kg and charge 1.0µc between two plates 10.0 cm apart. (Ans. 9.8 vm.)
- 12.7 A particle having a charge of 20 electrons on it fails through a potential difference of 100 volts. Calculate the energy acquired by it in electron volts (eV). [Ans. (2.0 x 10 eV)]
- In Millikan's experiment, oil droplets are introduced into the space between two flat horizontal plates, 5 00 mm apart. The plate voltage is adjusted to exactly 780V so that the droplet is held stationary. The plate voltage is switched off and the selected droplet is observed to fail a measured distance of 1 50 mm in 11 2 s. Given that the density of the oil used is 900 kg m<sup>3</sup>, and the viscosity of air at laboratory temperature in 1 80 x 10<sup>3</sup> Nm<sup>2</sup>s, calculate.
  - The mass, and The charge on the droplet (Assume  $g = 9.8 \text{ ms}^2$ )

    [Ans: (a) 5.14 x 10<sup>-16</sup> kg, (b) 3.20 x 10<sup>-16</sup> C]
- 12.9 A proton placed in a uniform electric field of 5000 NC \* directed to right is allowed to go a distance of 10.0 cm from A to B. Calculate
  - (a) Potential difference between the two points
  - (b) Work done by the field
  - (c) The change in P.E. of proton
  - (d) The change in K.E. of the proton
  - (e) Its velocity (mass of proton is 1.67 x 10<sup>-17</sup>kg)

(Ans: -500 V, 500 eV, -500 eV, 500 eV, 3 097 x 105 ms1)

- 12.10 Using zero reference point at infinity, determine the amount by which a point charge of 4.0 x 10°C alters the electric potential at a point 1.2 m away, when
  - (a) Charge is positive
- (b) Charge is negative

(Ans: +3.0 x 10° V, -3.0 x 10° V)

12.11 In Bohr's atomic model of hydrogen atom, the electron is in an orbit around the nuclear proton at a distance of 5.29 x 10 " m with a speed of 2.18 x 10 ms ' (e=1.60 x 10 °C, mass of electron ≠ 9.10 x 10 °kg). Find

The electric potential that a proton exerts at this distance

- (b) Total energy of the atom in eV
- (c) The ionization energy for the atom in eV

(Ans: +27.20 V, -13.6 eV, +13.60 eV)

- The electronic flash attachment for a camera contains a capacitor for storing the energy used to produce the flash. In one such unit, the potential difference between the plates of a 750 μF capacitor is 330 V. Determine the energy that is used to produce the flash.

  (Ans: 40.8 J)
- 12 13 A capacitor has a capacitance of 2.5 x 10° F. In the charging process, electrons are removed from one plate and placed on the other one. When the potential difference between the plates is 450 V, how many electrons have been transferred? (e=1.60 x 10°°C) (Ans: 7.0 x 10°°alectrons)

### Chapter 13

### CURRENT ELECTRICITY

### **Learning Objectives**

At the end of this chapter the students will be able to:

- Understand the concept of steady current.
- Describe some sources of current.
- Recognize effects of current.
- Understand and describe Ohm's law.
- Sketch and explain the current-voltage characteristics of a metallic conductor at constant temperature, diode and filament tamp.
- Understand resistivity and explain its dependence upon temperature
- Understand and elaborate conductance and conductivity of conductor
- Solve problems relating the variation of resistance with temperature for one dimension current flow.
  - Know the value of resistance by reading colour code on it
- 1 Know the working and use of rheostat in the potential divider circuit.
  - Describe the characteristics of thermistor
  - Use the energy considerations to distinguish between emf and p.d.
    - Understand the internal resistance of sources and its consequences for external circuits.
  - Describe the conditions for maximum power transfer.
- 15 Know and use the application of Kirchhoff's first law as conservation of charge
  - Know and use the application of Kirchhoff's second law as conservation of energy
  - Describe the function of Wheatstone Bridge to measure the unknown resistance.
- Describe the function of potentiometer to measure and compare potentials without drawing any current from the circuit.

Most practical applications of electricity involve charges in motion or the electric current. Alight bulb glows due to the flow of electric current. The current that flows through the coil of a motor causes its shaft to rotate. Most of the devices in the industry and in our homes.

operate with current. The electric current has become a necessity of our life.

#### 13.1 ELECTRIC CURRENT

An electric current is caused by the motion of electric charge if a net charge  $\Delta Q$  passes through any cross section of a conductor in time  $\Delta t$ , we say that an electric current I has been established through the conductor where

The SI unit of current is ampere and it is a current due to flow of charge at the rate of one coulomb per second

Motion of electric charge which causes an electric current is due to the flow of charge carners. In case of metallic conductors, the charge carners are electrons. The charge carners in electrolyte are positive and negative ions e.g., in a CuSO, solution the charge carriers are Cu<sup>\*\*</sup> and SO <sup>\*\*</sup>, ions. In gases, the charge carriers are electrons and ions.



When sel senses danger if turns itself into a viring battery. Any one who alter key this list is likely in sel a and key the performance between the sea and an if the self is self at a performance to the self is self at a performance.

#### ureat D

Early scientists regarded an electric current as a flow of positive charge from positive to negative terminal of the battery through an external circuit. Later on it was found that a current in metallic conductors is actually due to the flow of negative charge carners called electrons moving in the opposite direction i.e. from negative to positive terminal of the battery but it is a convention to take the direction of current as the direction in which positive charges flow. This current is referred as conventional current. The reason is that it has been found experimentally that positive charge moving in one direction is equivalent in all external effects to a negative charge moving in the opposite direction. As the current is measured by its external effects so a current due to motion of negative charges, after reversing its direction of flow can be substituted by an equivalent current due to flow of positive charges. Thus

The conventional current in a circuit is defined as that equivalent current which passes from a point at higher potential to a point at a lower potential as if it represented a movement of positive charges

White analyzing the electric circuit, we use the direction of the current according to the above mentioned convention

If we wish to refer to the motion of electrons, we use the term electronic current (Fig. 13.1).

#### riducto

In a metal, the valence electrons are not attached to individual atoms but are free to move about within the body. These electrons are known as free electrons. The free electrons are in random motion just like the molecules of a gas in a container and they act as charge carriers in metals. The speed of randomly moving electrons depends upon temperature

If we consider any section of metallic wire, the rate at which the free electrons pass through it from right to left is the same. as the rate at which they pass from left to night (Fig. 13.2 a). As a result the current through the wire is zero. If the ends of the wire are connected to a battery, an electric field E will be set up at every point within the wire (Fig. 13.2 b). The free electrons will now experience a force in the direction opposite to E. As a result of this force the free electrons acquire a motion in the direction of -E. It may be noted that the force experienced by the free electrons does not produce a net acceleration because the electrons keep on colliding with the atoms of the conductor. The overall effect of these collisions is to transfer the energy of accelerating electrons to the lattice with the result that the electrons acquire an average velocity, called the drift velocity in the direction of -E (Fig. 13.2 b). The drift velocity is of the order of 10 'ms', whereas the velocity of free electrons at room temperature due to their thermal motion is several hundred kilometres per second

Thus when an electric field is established in a conductor the free electrons modify their random motion in such a way that they drift slowly in a direction opposite to the field in other words the electrons, in addition to their violent thermal motion acquire a constant drift velocity due to which a net directed motion of charges takes place along the wire and a current begins to flow through it. A steady current is established in a wire when a constant potential difference is maintained across it which generates the requisite electric field E along the wire

Example 13.1: 10 x 10' electrons pass through a conductor in 10 μs. Find the current in ampere flowing through the conductor Electronic charge is 1 6 x 10 °C Solution: Number of electrons = n = 1.0 x 10°

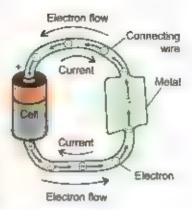
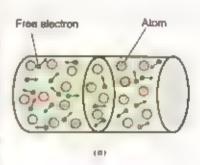
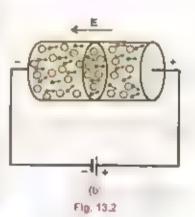


Fig. 13.1





33

Charge on an electron = e = 1.6 x 10° °C

Time = $\Delta I = 1.0$ us

Current / through the conductor is given by

$$I = \frac{\lambda I}{\lambda \hat{\Omega}} = \frac{\lambda I}{Mc}$$

 $I = \frac{1.0 \times 10^7 \times 1.6 \times 10^{-19} \text{C}}{1.0 \times 10^{-6} \text{s}} = 1.6 \times 10^{-6} \text{Cs} = 1.6 \times 10^{-6} \text{A}$ 

### 13.2 SOURCE OF CURRENT

When two conductors at different potentials are joined by a metallic wire current with flow through the wire. The current continues to flow from higher potential to the lower potential until both are at the same potential (Fig. 13.3). After this the current ceases to flow. Thus the current through the wire decreases from a maximum value to zero. In order to have a constant current the potential difference across the conductors or the ends of the wire should be maintained constant. This is achieved by connecting the ends of the wire to the terminals of a device called a source of current (Fig. 13.4).

Every source of current converts some non electrical energy such as chemical, mechanical, heat or solar energy into electrical energy. There are many types of sources of current Afew examples are mentioned below:

Cells (primary as well as secondary) which convert chemical energy into electrical energy

Electric generators which convert mechanical energy into electrical energy

- (III) Thermo-couples which convert heat energy into electrical energy
- Solar cells which convert sunlight directly into electrical energy.

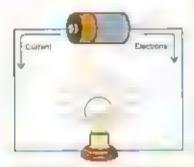
### 13.3 EFFECTS OF CURRENT

The presence of electric current can be detected by the various effects which it produces. The obvious effects of the current are

- (i) Heating effect
- (III) Magnetic effect
- (let) Chemical effect



Conventional current flows from higher to lower potential shrough a wire



 A source of current such as battery maintains a nearly constant potential difference between ends of a conductor



Healing effect of current is used in electric kettle.



Current flows through a metallic wire due to motion of free electrons. During the course of their motion, they collide frequently with the atoms of the metal. At each collision, they lose some of their kinetic energy and give it to atoms with which they collide. Thus as the current flows through the wire, it increases the kinetic energy of the vibrations of the metal atoms. I.e., it generates heat in the wire. It is found that the heat H produced by a current I in the wire of resistance R during a time interval I is given by



The heating effect of current is utilized in electric heaters, kettles, toasters and electric irons etc.

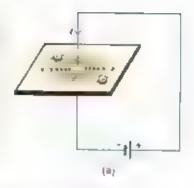


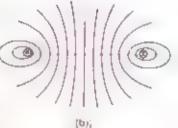
The passage of current is always accompanied by a magnetic field in the surrounding space. The strength of the field depends upon the value of current and the distance from the current element. The pattern of the field produced by a current carrying straight wire a coil and a solenoid is shown in Fig. 13.5 (a, b & c). Magnetic effect is utilized in the detection and measurement of current. All the machines involving electric motors also use the magnetic effect of current.

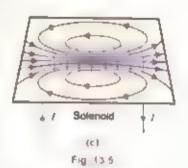


Certain liquids such as dilute sulphunc acid or copper sulphate solution conduct electricity due to some chemical reactions that take place within them. The study of this process is known as electrolysis. The chemical changes produced during the electrolysis of a liquid are due to chemical effects of the current. It depends upon the nature of the liquid and the quantity of electricity passed through the liquid.

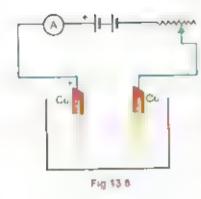
The liquid which conducts current is known as electrolyte. The material in the form of wire or rod or plate which leads the current into or out of the electrolyte is known as electrode. The electrode connected with the positive terminal of the current source is called anode and that connected with negative terminal is known as cathode. The vessel containing the two electrodes and the liquid is known as voltameter. As an example we will consider the electrolysis of copper sulphate solution. The voltameter contains dilute solution of copper sulphate. The anode and cathode are both copper plates.







35



(Fig. 13.6) When copper sulphate is dissolved in water, it dissociates into Cu and SO, ions On passing current through the voltameter Cu moves towards the cathode and the following reaction takes place.

The copper atoms thus formed are deposited at cathode plate. While copper is being deposited at the cathode, the SO, ions move towards the anode. Copper atoms from the anode go into the solution as copper ions which combine with sulphate ions to form copper sulphate.

As the electrolysis proceeds copper is continuously deposited on the cathode-while an equal amount of copper from the anode is dissolved into the solution and the density of copper sulphate solution remains unaltered

This example also illustrates the basic principle of electroplating - a process of coating a thin layer of some expensive metal (gold, silver etc.) on an article of some cheap metal.

## 13.4 OHM'S LAW

We have seen that when a battery is connected across a conductor an electric current begins to flow through it. How much current flows through the conductor when a certain potential difference is set up across its ends? The answer to this question was given by a German Physicist George Simon Ohm. He showed by elaborate experiments that the current through a metallic conductor is directly proportional to the potential difference across its ends. This fact is known as Ohms' law which states that

"The current flowing through a conductor is directly proportional to the potential difference across its ends provided the physical state such as temperature etc. of the conductor remains constant".

Symbolically Ohm's law can be written as

It implies that 
$$V=RI$$
 . (13.2)

where R, the constant of proportionality is called the resistance of the conductor. The value of the resistance depends upon the nature dimensions and the physical state of the conductor. In fact the resistance is a measure of the

opposition to the motion of electrons due to their continuous bumping with the atoms of the lattice. The unit of resistance is ohm. A conductor has a resistance of 1 ohm if a current of 1 ampere flows through it when a potential difference of 1 volt is applied across its ends. The symbol of ohm is  $\Omega$ . If I is measured in amperes, V in volts, then R is measured in ohms i.e.,

$$R(\text{ohms}) = \frac{V(\text{volts})}{I(\text{amperes})}$$
 (13.3)

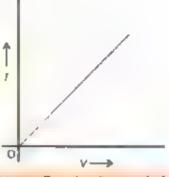
A sample of a conductor is said to obey Ohm's law if its resistance R remains constant that is, the graph of its V versus / is exactly a straight line (Fig. 13.7). A conductor which strictly obeys Ohm's law is called ohmic. However, there are devices, which do not obey Ohms' law i.e., they are non-ohmic. The examples of non-ohmic devices are filament bulbs and semiconductor diodes.

Let us apply a certain potential difference across the terminals of a filament tamp and measure the resulting current passing through it. If we repeat the measurement for different values of potential difference and draw a graph of voltage V versus current I, it will be seen that the graph is not a straight line (Fig. 13.8). It means that a filament is a non-ohmic device. This deviation of I - V graph from straight line is due to the increase in the resistance of the filament with temperature - a topic which is discussed in the next section. As the current passing through the filament is increased from zero, the graph is a straight line in the initial stage because the change in the resistance of the filament with temperature due to small current is not appreciable. As the current is further increased, the resistance of the filament continues to increase due to rise in its temperature.

Another example of non-ohmic device is a semiconductor diode. The current - voltage plot of such a diode is shown in Fig. 13.9. The graph is not a straight line so semi-conductor is also a non-ohmic device.

In an electrical circuit, usually, a number of resistors are connected together. There are two arrangements in which resistors can be connected with each other, one is known as series arrangement and other one as parallel arrangement.

If the resistors are connected end to end such that the same current passes through all of them, they are said to be connected in series as shown in Fig. 13.10(a). There



Current voltage graph of an ohmic material.

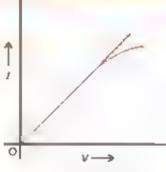


Fig. 13-8

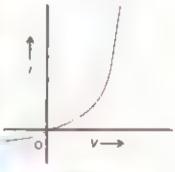


Fig 13.9

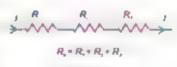
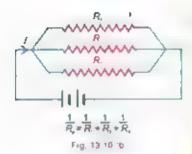


Fig 13 10 (a)

equivalent resistance R, is given by



$$R_{s} = R_{s} + R_{s} + R_{s} + \dots$$
 (13.4)

In parallel arrangement a number of resistors are connected side by side with their ends joined together at two common points as shown in Fig. 13.10(b). The equivalent resistance R<sub>e</sub> of this arrangement is given by

$$\frac{1}{R_a} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$
 (13.5)

# 13.5 RESISTIVITY AND ITS DEPENDENCE UPON TEMPERATURE

It has been experimentally seen that the resistance R of a wire is directly proportional to its length L and inversely proportional to its cross sectional area A Expressing mathematically we have

or 
$$R = \rho \frac{L}{A}$$
 (13.6)

where p is a constant of proportionality known as resistivity of specific resistance of the material of the wire. It may be noted that resistance is the characteristic of a particular wire whereas the resistivity is the property of the material of which the wire is made. From Eq. 13.6 we have

$$\rho = \frac{RA}{L} \qquad (13.7)$$

The above equation gives the definition of resistivity as the resistance of a metre cube of a material. The SI unit of resistivity is ohim-metre (Ω m)

Conductance is another quantity used to describe the electrical properties of materials. In fact conductance is the reciprocal of resistance i.e.,

Conductance = 
$$\frac{1}{\text{resistance}(R)}$$

The SI unit of conductance is inho or siemen

Likewise conductivity, a is the reciprocal of resistivity (e.,

$$\sigma = \frac{1}{\alpha} \tag{13.8}$$

The SI unit of conductivity is ohm 'm' or mh m'. Resistivity of various materials are given in Table 13.1.

it may be noted from Table 13.1 that silver and copper are two best conductors. That is the reason that most electric wires are made of copper.

The resistivity of a substance depends upon the temperature also It can be explained by recalling that the resistance offered by a conductor to the flow of electric current is due to collisions, which the free electrons encounter with atoms of the lattice. As the temperature of the conductor rises, the amplitude of vibration of the atoms in the lattice increases and hence, the probability of their collision with free electrons also increases. One may say that the atoms then offer a bigger target, that is the collision cross-section of the atoms increases with temperature. This makes the collisions between free electrons and the atoms in the lattice more frequent, and hence, the resistance of the conductor increases.

Experimentally the change in resistance of a metallic conductor with temperature is found to be nearly linear over a considerable range of temperature above and below 0 °C (Fig. 13.11). Over such a range the fractional change in resistance per keivin is known as the temperature coefficient of resistance i.e.,

$$\alpha = \frac{R - R}{R_{c}t} \tag{13.9}$$

where  $R_i$  and  $R_i$  are resistances at temperature 0 °C and t °C. As resistivity  $\rho$  depends upon the temperature, Eq. 13.6 gives

R=p,UA and R=p,UA
Substituting the values of R, and R, in Eq. 13.9, we get

as 
$$\alpha = \frac{\rho_1 - \rho_2}{\rho_n t}$$
 (13.10)

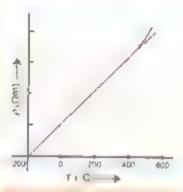
where  $\rho_c$  is the resist-vity of a conductor at 0 °C and  $\rho_c$  is the resist-vity at t °C. Values of temperature co-efficients of resist-vity of some substances are also listed in Table 13.1.

There are some substances like germanium, silicon etc., whose resistance decreases with increase in temperature lie, these substances have negative temperature coefficients.

Example 13.2: 0.75 A current flows through an iron wire when a battery of 1.5 V is connected across its ends. The

Table 13 1

Substance	ρ (Ωm)	n (K*)
Salver	1 52 × 10 <sup>4</sup>	0.00380
Copper	1.54 × 10 <sup>4</sup>	0.00390
Gold	2.27 × 10 <sup>-6</sup>	0.00340
Alumanuam	2 63 × 10 <sup>th</sup>	0.00390
Tungster	5.00 × 10 <sup>4</sup>	0.00460
Impr	11.00 = 10 <sup>-8</sup>	0.00520
Platinum	11.00 × 10 <sup>-4</sup>	0.00520
Constanton	49.00 + 10*	0.00001
Mercury	94 00 × 10 <sup>-4</sup>	0.00091
Nichrome	100.0 × 0 <sup>4</sup>	0.00020
Carbon	35 + 104	-0.0005
Germanum	۵5	-0 05
Stircon	20-2300	-0.07



Vanation of resistivity of Cu with temperature

#### والتوريد والمراوي والمراوي

inspecials can easily check the reliability of a concrete bridge made with carbon fibers. The fibers conduct electrical resistance is increasing over time the fibers are separating because of cracks.

length of the wire is 5.0 m and its cross sectional area is 2.5 × 10° m<sup>2</sup>. Compute the resistivity of iron.

#### Solution:

The resistance R of the wire can be calculated by Eq. 13.2 i.e.,

$$R = \frac{1}{I} = \frac{1.5 \text{ V}}{0.75 \text{ A}} = 2.0 \text{ VA}^{-1} = 2.0 \Omega$$

The resistivity plot iron of which the wire is made is given by

$$\rho = R \frac{A}{L} = \frac{2.0 \,\Omega \times 2.5 \times 10^{-7} \text{m}^2}{50 \,\text{m}} = 1.0 \times 10^{-7} \,\Omega \text{m}$$

**Example 13.3:** A platinum wire has resistance of 10  $\Omega$  at 0°C and 20  $\Omega$  at 273 °C. Find the value of temperature coefficient of resistance of platinum

### Solution:

Temperature coefficient of resistance can be found by

$$\alpha = \frac{R_1 - R_2}{R_0 I} = \frac{20 \Omega - 10 \Omega}{10 \Omega \times 273 K} = \frac{1}{273 K} = 3.66 \times 10^{-3} K^{-1}$$

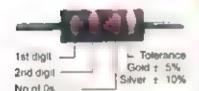
# 13.6 COLOUR CODE FOR CARBON RESISTANCES

Carbon resistors are most common in electronic equipment. They consist of a high-grade ceramic rod or cone (called the substrate) on which is deposited a thin resistive film of carbon. The numerical value of their resistance is indicated by a colour code which consists of bands of different colours printed on the body of the resistor. The colour used in this code and the digits represented by them are given in Table 13.2.

Usually the code consists of four bands (Fig. 13.12). Starting from left to right, the colour bands are interpreted as follows.

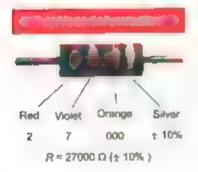
- The first band indicates the first digit in the numerical value of the resistance.
- The second band gives the second digit.
- The third band is decimal multiplier i.e. it gives the number of zeros after the first two digits.
  - The fourth band gives resistance tolerance its colour is either silver or gold. Silver band indicates a tolerance of ± 10%, a gold band shows a tolerance of





Resistor Colour Code

Fig. 13.12



 $\pm$  5 %. If there is no fourth band, tolerance is understood to be + 20%. By tolerance, we mean the possible variation from the marked value. For example, a 1000  $\Omega$  resistor with a tolerance of  $\pm$  10% will have an actual resistance anywhere between 900 $\Omega$  and 1100  $\Omega$ 

## Riverstat

It is a wire wound variable resistance. It consists of a bare

mangarin wire wound over an insulating cylinder. The ends of the wire are connected to two fixed terminals A and B (Fig. 13.13.a). A third terminal C is attached to a skding contact which can also be moved over the wire.

A rheostat can be used as a variable resistor as well as a potential divider. To use it as a variable resistor one of the fixed terminal say A and the sliding terminal C are inserted in the circuit (Fig. 13.13 b). In this way the resistance of the wire between A and the sliding contact C is used. If the sliding contact is shifted away from the terminal A, the length and hence the resistance included in the circuit increases and if the sliding contact is moved towards A, the resistance decreases. Arheostat can also be used as a potential divider

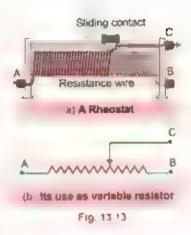
This is illustrated in Fig. 13.14. A potential difference V is applied across the ends A and B of the rheostat with the help of a battery. If R is the resistance of wire AB, the current I passing through it is given by I = V/R.

The potential difference between the portion BC of the wire AB is given by

$$V_{\text{sc}} = \text{current x resistance}$$

$$= \frac{V}{R} \times r = \frac{r}{R} V \qquad (13.11)$$
recurring so of the particle RC of the ware. The

where r is the resistance of the portion BC of the wire. The circuit shown in Fig. 13.14 is known as potential divider. Eq.13.11 shows that this circuit can provide at its output terminals a potential difference varying from zero to the full potential difference of the battery depending on the position of the sliding contact. As the sliding contact C is moved towards the end B, the length and hence the resistance r of the portion BC of the wire decreases which according to Eq. 13.11, decreases  $V_{\rm ac}$ . On the other hand if the sliding contact C is moved towards the end A, the output voltage  $V_{\rm ac}$  increases



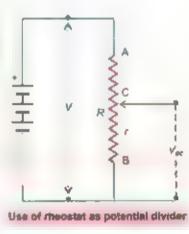


Fig.13.14



A thermistor is a heat sensitive resistor. Most thermistors have negative temperature coefficient of resistance i.e. the resistance of such thermistors decreases when their temperature is increased. Thermistors with positive temperature coefficient are also available.

Thermistors are made by heating under high pressure semiconductor ceramic made from mixtures of metallic oxides of manganese nicket cobalt copper iron etc. These are pressed into desired shapes and then baked at high temperature. Different types of thermistors are shown in Fig. 13,15. They may be in the form of beads, rods or washers.

Thermistors with high negative temperature coefficient are very accurate for measuring low temperatures especially near 10 K. The higher resistance at low temperature enables more accurate measurement possible.

Thermistors have wide applications as temperature sensors i.e., they convert changes of temperature into electrical voltage which is duly processed.

# 13.7 ELECTRICAL POWER AND POWER DISSIPATION IN RESISTORS

Consider a circuit consisting of a battery E connected in series with a resistance R (Fig. 13.16). A steady current I flows through the circuit and a steady potential difference V exists between the terminals A and B of the resistor R. Terminal A, connected to the positive pole of the battery is at a higher potential than the terminal B in this circuit the battery is continuously lifting charge uphill through the potential difference V. Using the meaning of potential difference the work done in moving a charge  $\Delta Q$  up through the potential difference V is given by

Work done = 
$$\Delta W = V \times \Delta Q \dots$$
, (13.12)

This is the energy supplied by the battery. The rate at which the battery is supplying electrical energy is the power output or electrical power of the battery. Using the definition of power we have

Electrical power = 
$$\frac{\text{Energy supplied}}{\text{Time taken}} = V \frac{\Delta C}{\Delta t}$$



Fig. 13 15 Thermistors of different shapes.



A zero-ohm resistor is indicated by a single black colour band around he body of the resistor.

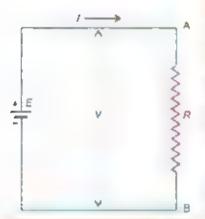


Fig. 11. The power of a battery oppears as the power dissipated in the resistor R

$$I = \frac{\Delta Q}{\Delta t}$$
, so

Electrical power = VxI

(13.12a)

Eq. 13.12a is a general relation for power delivered from a source of current *I* operating on a voltage *V*. In the circuit shown in Fig.13.16 the power supplied by the battery is expended or dissipated in the resistor *R*. The principle of conservation of energy tells us that the power dissipated in the resistor is also given by Eq. 13.12.a.

Alternative equation for calculating power can be found by substituting V=IR, I=V/R in turn in Eq. 13.13

$$P = V \times I = IR \times I = I^{2}R$$

$$P = V \times I = V \times \frac{V}{R} = \frac{V^{2}}{R}$$

Thus we have three equations for calculating the power dissipated in a resistor.

$$P=V\times I, P=I^2R, P=\frac{V^2}{R}$$
 ..... (13.14)

If Vis expressed in volts and /in amperes, the power is expressed in watts.

# 13.8 ELECTROMOTIVE FORCE (EMF) AND POTENTIAL DIFFERENCE

We know that a source of electrical energy say a cell or a battery, when connected across a resistance maintains a steady current through it (Fig. 13.17). The cell continuously supplies energy which is dissipated in the resistance of the circuit. Suppose when a steady current has been established in the circuit, a charge  $\Delta Q$  passes through any cross section of the circuit in time  $\Delta t$ . During the course of motion, this charge enters the cell at its low potential end and leaves at its high potential end. The source must supply energy  $\Delta W$  to the positive charge to force it to go to the point of high potential. The emf E of the source is defined as the energy supplied to unit charge by the cell.

Le 
$$E = \frac{\Delta W}{\Delta Q}$$
 . (13.15)



f g 13.17 Electromotive force of a cell

It may be noted that electromotive force is not a force and we do not measure it in newtons. The unit of emf is joule/coulomb which is volt (V).

The energy supplied by the cell to the charge carners is derived from the conversion of chemical energy into electrical energy inside the cell.

Like other components in a circuit a cell also offers some resistance. This resistance is due to the electroryte present between the two electrodes of the cell and is called the internal resistance r of the cell. Thus a cell of emf. E having an internal resistance r is equivalent to a source of pure emf. E with a resistance r in senes as shown in Fig. 13.18.

Let us consider the performance of a cell of emf E and internal resistance r as shown in Fig. 13.19. A voltmeter of infinite resistance measures the potential difference across the external resistance R or the potential difference V across the terminals of the cell. The current I flowing through the circuit is given by

or E = IR + Ir (13.16)

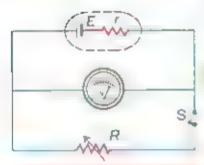
Here IR = V is the terminal potential difference of the cell in the presence of current I. When the switch S is open, no current passes through the resistance. In this case the voltmeter reads the emf E as terminal voltage. Thus terminal voltage in the presence of the current (switch on) would be less than the emf E by Ir.

Let us interpret the Eq. 13-16 on energy considerations. The left side of this equation is the emf. E of the cell which is equal to energy gained by unit charge as it passes through the cell from its negative to positive terminal. The right side of the equation gives an account of the utilization of this energy as the current passes the circuit. It states that, as a unit charge passes through the circuit, a part of this energy equal to I ris dissipated into the cell and the rest of the energy is dissipated into the external resistance R. It is given by potential drop I R. Thus the emf gives the energy supplied to unit charge by the cell and the potential drop across the various elements account for the dissipation of this energy into other forms as the unit charge passes through these elements.

The emf is the "cause" and potential difference is its "effect". The emf is always present even when no current is drawn.



Fig. 1.18 An equivalent circuit of a cell or emil £ and internal resistance r



I'm so The fermed potental offerences face so

through the battery or the cell, but the potential difference across the conductor is zero when no current flows through it.

**Example 13.4:** The potential difference between the terminals of a battery in open circuit is 2.2 V. When it is connected across a resistance of 5.0  $\Omega$  the potential fails to 1.8 V. Calculate the current and the internal resistance of the battery.

#### Solution:

As

Given F-22V, R=5.0Ω, V-18V

We are to calculate / and r

We have V = IR

or  $I = \frac{V}{R} = \frac{18 \text{ V}}{50 \Omega} = 0.36 \text{ A}$ 

Internal resistance rican be calculated by using

E-V+Ir

or 22V=18V+036Axr

or r = 1.11 VA' = 1.11 Ω

## Marining Proper Supplie

In the circuit of Fig. 13.19, as the current I flows through the resistance R, the charges flow from a point of higher potential to a point of lower potential and as such, they loose potential energy. If V is the potential difference across R, the loss of potential energy per second is VI. This loss of energy per second appears in other forms of energy and is known as power delivered to R by current I.

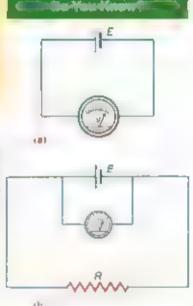
Power delivered to  $R = P_{ad} = VI$ 

$$= l^{2}R \qquad (: V = lR)$$

$$l = \frac{E}{R + l}$$

 $P_{out} = \frac{E^2 R}{(R+r)^2} = \frac{E^2 R}{(R-r)^2 + 4Rr}$  (13.17)

when R = r, the denominator of the expression of  $P_{\rm ext}$  is least and so  $P_{\rm ext}$  is then a maximum. Thus we see that maximum power is delivered to a resistance (load), when the internal resistance of the source equals the load resistance. The



A voltmeter connected across the terminals of a cell measures a the emf of the cell on open circuit, b) the terminal potential difference on a closed circuit.

value of this maximum output power as given by Eq. 13.17 is  $E^2$ 

4R

#### 13.9 KIRCHHOFF'S RULES

Ohm's law and rules of series and parallel combination of resistance are quite useful to analyze simple electrical circuits consisting of more than one resistance. However such a method fails in the case of complex networks consisting of a number of resistors, and a number of voltage sources. Problems of such networks can be solved by a system of analysis, which is based upon two rules, known as Kirchhoff's rules.



It states that the sum of all the currents meeting at a point in the circuit is zero i.e.,

$$\Sigma I = 0$$
 .......... (13.18)

It is a convention that a current flowing towards a point is taken as positive and that flowing away from a point is taken as negative

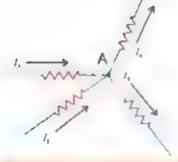
Consider a situation where four wires meet at a point A (Fig. 13.20). The currents flowing into the point A are I, and I<sub>2</sub> and currents flowing away from the point are I<sub>3</sub> and I<sub>4</sub>. According to the convention currents I and I<sub>4</sub> are positive and currents I<sub>3</sub> and I<sub>4</sub> are negative. Applying Eq. 13.18 we have

$$I_1 + I_2 + (-I_3) + (-I_4) = 0$$
  
 $I_1 + I_2 = I_1 + I_4$  ...... (13.19)

Using Eq. 13.19 Kirchhoff's first rule can be stated in other words as

The sum of all the currents flowing towards a point is equal to the sum of all the currents flowing away from the point.

Kirchhoff's first rule which is also known as Kirchhoff's point rule is a manifestation of law of conservation of charge. If there is no sink or source of charge at a point, the total charge flowing towards the point must be equal to the total charge flowing away from it.



7 in 124 According to Kirchhoff's 1° rule I. + I, = I + I,

## Kirchhoff's Second Rule

It states that the algebraic sum of voltage changes in a closed. circuit or a loop must be equal to zero. Consider a closed circuit shown in Fig. 13.21. The direction of the current I flowing through the circuit depends on the cell having the greater emf. Suppose E is greater than E, so the current flows in counter clockwise direction (Fig. 13.21). We know that a steady current is equivalent to a continuous flow of positive charges through the circuit. We also know that a voltage change or potential difference is equal to the work. done on a unit positive charge or energy gained or lost by it in moving from one point to the other. Thus when a positive charge AQ due to the current I in the closed circuit (Fig. 13.21), passes through the cell E, from low (-ve) to high potential (+ye) it gains energy because work is done on it. Using Eq. 13.12 the energy gain is E, ∆Q. When the current passes through the cell E it loses energy equal to - E AQ because here the charge passes from high to low potential. In going through the resistor R, the charge AQ loses energy equal to - / R AQ where / R is potential difference across R The minus sign shows that the charge is passing from high to ow potentia. Similarly the loss of energy white passing through the resistor R. s. IR, AQ. Finally the charge reaches the negative terminal of the cell E from where we started According to the law of conservation of energy the total change in energy of our system is zero. Therefore, we can write

$$E_{i}\Delta Q - iR_{i}\Delta Q - E_{i}\Delta Q - iR_{i}\Delta Q = 0$$
  
or  $E_{i} - iR_{i} - iR_{i} = 0$  . (13.20)

which is Kirchhoff's second rule and it states that

# The algebraic sum of potential changes in a closed circuit is zero.

We have seen that this rule is simply a particular way of stating the law of conservation of energy in electrical problems.

Before applying this rule for the analysis of complex network it is worthwhile to thoroughly understand the rules for finding the potential changes.

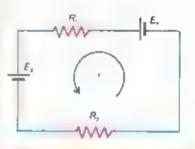


Fig. 1. According to Kirchhoffs 2<sup>M</sup> rule E. IR. E., IR., =0

- (i) If a source of emf is traversed from negative to positive terminal, the potential change is positive, it is negative in the opposite direction.
- If a resistor is traversed in the direction of current, the change in potential is negative, it is positive in the opposite direction.

**Example 13.6:** Calculate the currents in the three resistances of the circuit shown in Fig. 13.22.

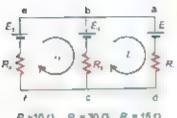
#### Solution:

First we select two loops aboda and ebofe. The choice of loops is quite arbitrary, but it should be such that each resistance is included at least once in the selected loops.

After selecting the loops, suppose a current *I* is flowing in the first loop and *I*<sub>2</sub> in the second loop, all flowing in the same sense. These currents are called loop currents. The actual currents will be calculated with their help. It should be noted that the sense of the current flowing in all loops should essentially be the same. It may be clockwise or anticlockwise. Here we have assumed it to be clockwise (Fig. 13.22).

We now apply Kirchhoff's second rule to obtain the equations required to calculate the currents through the resistances. We first consider the loop abcda. Starting at a point 'a we follow the loop clockwise. The voltage change while crossing the battery E is - E, because the current flows through it from positive to negative. The voltage change across R, is -  $I_rR_r$ . The resistance R, is common to both the loops I and I2 therefore, the currents I and I, simultaneously flow through it. The directions of currents I, and I, as flowing through R, are opposite, so we have to decide that which of these currents is to be assigned a positive sign. The convention regarding the sign of the current is that if we are applying the Kirchhoffs second rule in the first loop, then the current of this loop (  $\sigma/L$ will be assigned a positive sign and all currents, flowing opposite to / have a negative sign. Similarly, while applying Kirchhoffs second rule in the second loop, the current I, will be considered as positive and /, as negative Using this convention the current flowing through  $R_2$  is  $(l-l_2)$  and the voltage change across is - (I, - I2) R, The voltage change across the battery E, is E, Thus the Kirchhoffs second rule as applied to the loop abcda gives

$$-E_1-I_1R_2-(I_1-I_2)R_2+E_3=0$$



Substituting the values, we have

$$-40 \text{ V} - I_1 \times 10 \Omega - (I_1 - I_2) \times 30 \Omega + 60 \text{ V} = 0$$

$$20 \text{ V} - 10 \Omega \times [I_1 + 3(I_1 - I_2)] = 0$$

$$4I_2 - 3I_3 = 2 \text{ V}\Omega^2 = 2 \text{ A} \qquad (13.21)$$

Similarly applying Kirchhoff's second rule to the loop ebcfe.

we get

$$-E_1 - (I_2 - I_1) R_2 - I_2 R_3 + E_1 = 0$$

Substituting the values, we have

$$-60 \text{ V} - (I_2 - I_3) \times 30 \Omega - I_2 \times 15 \Omega + 50 \text{ V} = 0$$

$$-10 \text{ V} - 15 \Omega \times [I_2 + 2(I_2 - I_1)] = 0$$

or 
$$8I_1 - 9I_2 = 2V\Omega^{-1} = 2A$$
 ...... (13.22)

Solving Eq. 13.21 and Eq. 13.22 for I, and I, we get

$$I_1 = \frac{2}{3} \text{ A}$$
 and  $I_2 = \frac{2}{9} \text{ A}$ 

Knowing the values of loop currents I, and I, the actual current flowing through each resistance of the circuit can be determined Fig. 13.22 shows that I, and I, are the actual currents through the resistances R, and R. The actual current through R, is the difference of I, and I, and its direction is along the larger current. Thus

The current through  $R = I = \frac{2}{3} A = 0.66 A$  flowing in the direction of J. I.e., from a to d.

The current through  $R_1 = I_1 - I_2 = \frac{2}{3} A - \frac{2}{9} A = 0.44 A flowing in the direction of <math>I_3$  i.e., from c to b.

The current through  $R_1 = I_2 = \frac{2}{6}A = 0.22$  A flowing in the direction of I, i.e., from f to e

# Solution of Circuit Problems

After solving the above problem we are in a position to apply the same procedure to analyse other direct current complex networks. While using Kirchhoff's rules in other problems, it is worthwhile to follow the approach given below:

- (1) Draw the circuit diagram.
- The choice of loops should be such that each (0)resistance is included at least once in the selected loops.

- (iii) Assume a loop current in each loop, all the loop currents should be in the same sense it may be either clockwise or anticlockwise
- (iv) Write the loop equations for all the selected loops. For writing each loop equation the voltage change across any component is positive if traversed from low to high potential and it is negative if traversed from high to low potential.

Solve these equations for the unknown quantities.

#### 13.9 WHEATSTONE BRIDGE

The Wheatstone bridge circuit shown in Fig. 13.23 consists of four resistances R, R, R, and R, connected in such a way so as to form a mesh ABCDA. A battery is connected between points A and C. A sensitive galvanometer of resistance  $R_{\rm o}$  is connected between points B and D. If the switch S is closed a current will flow through the galvanometer. We are to determine the condition under which no current flows through the galvanometer even after the switch is closed. For this purpose we analyse this circuit using Kirchhoff's second rule. We consider the loops ABDA, BCDB and ADCA, and assume anticlockwise loop currents  $I_{\rm o}$ ,  $I_{\rm o}$ , and  $I_{\rm o}$ , through the loops respectively. The Kirchhoff's second rule as applied to loop ABDA gives.

$$-I_1R_2 - (I_1 - I_2)R_2 - (I_1 - I_2)R_3 = 0$$
 (13.23)

Similarly by applying the Kirchhoffs second rule to loop -BCDB we have

$$-I_{1}R_{1}-(I_{2}-I_{3})R_{4}-(I_{2}-I_{3})R_{4}=0$$
(13.24)

The current flowing through the galvanometer will be zero  $I_1 - I_2 = 0$  or  $I_1 = I_2$ . With this condition Eq. 13.23 and Eq. 13.24 reduce to

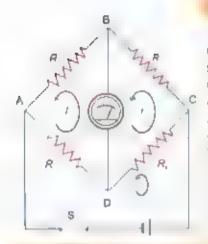
$$-I_iR = (I - I_i)R_i$$
 (13.25)

$$-I_1R_2 = (I_2 - I_3)R_4$$
 (13.26)

Dividing Eq. 13.25 by Eq. 13.26

$$\frac{R_1}{R_2} = \frac{R_3}{R_4}$$
 (13.27)

Thus whenever the condition of Eq. 13.27 is satisfied ino current flows through the galvanometer and it shows no deflection, or conversely when the galvanometer in the Wheatstone bridge circuit shows no deflection, Eq. 13.27 is satisfied.



Mheussione bridge carroit

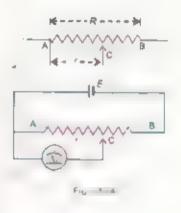
If we connect three resistances  $R_1$ ,  $R_2$  and  $R_3$  of known adjustable values and a fourth resistance  $R_1$ , of unknown value and the resistances  $R_2$ ,  $R_3$  and  $R_3$  are so adjusted that the galvanometer shows no deflection then, from the known resistances  $R_4$ ,  $R_2$  and  $R_3$  the unknown resistance  $R_4$  can be determined by using Eq. 13.27

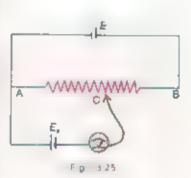
## 13.10 POTENTIOMETER

Potential difference is usually measured by an instrument called a voltmeter. The voltmeter is connected across the two points in a circuit between which potential difference is to be measured. It is necessary that the resistance of the voltmeter be large compared to the circuit resistance across which the voltmeter is connected. Otherwise an appreciable current will flow through the voltmeter which will after the circuit current and the potential difference to be measured. Thus the voltmeter can read the correct potential difference only when it does not draw any current from the circuit across which it is connected. An ideal voltmeter would have an infinite resistance.

However, there are some potential measuring instruments such as digital voltmeter and cathode ray oscilloscope which practically do not draw any current from the circuit because of their large resistance and are thus very accurate potential measuring instruments. But these instruments are very expensive and are difficult to use. A very simple instrument which can measure and compare potential differences accurately is a potentiometer.

A potentiometer consists of a resistor R in the form of a wire on which a terminal C can slide (Fig. 13.24 a). The resistance between A and C can be varied from 0 to R as the sliding contact C is moved from A to B. If a battery of emil E is connected across R (Fig. 13.24 b), the current flowing through it is I = E/R. If we represent the resistance between A and C by r the potential drop between these points will be r/ = r E/R Thus as C is moved from A to B, r varies from 0 to R and the potential drop between A and C changes from 0 to E Such an arrangement also known as potential divider can be used to measure the unknown emf of a source by using the circuit shown in Fig. 13.25. Here R is in the form of a straight wire of uniform area of cross section. A source of potential say a cell whose emf E, is to be measured, is connected between A and the sliding contact C through a gaivanometer. G It should be noted that the positive terminal of E, and that of the potential divider are connected to the same point A. If in





the toop AGCA, the point C and the negative terminal of E, are at the same potential then the two terminals of the galvanometer will be at the same potential and no current will flow through the galvanometer. Therefore, to measure the potential E, the position of C is so adjusted that the galvanometer shows no deflection. Under this condition, the emil E, of the cell is equal to the potential difference between A and C whose value  $E \cap R$  is known. In case of a wire of uniform cross section, the resistance is proportional to the length of the wire. Therefore, the unknown emil is also given by

$$E_{r} - E_{R}^{r} = E_{L}^{r}$$
 (13.28)

where L is the total ength of the wire AB and L is its length from A to C after C has been adjusted for no deflection. As the maximum potential that can be obtained between A and C is E so the unknown emf E should not exceed this value otherwise the null condition will not be obtained it can be seen that the unknown emf E is determined when no current is drawn from it and therefore potentiameter is one of the most accurate methods for measuring potential.

The method for measuring the emf of a cell as described above can be used to compare the emfs E and E, of two cells. The balancing engths  $\ell$ , and  $\ell$  are found separately for the two cells. Then

$$E_i = E \frac{\ell_1}{L}$$
 and  $E_z = E \frac{\ell_2}{L}$ 

Dividing these two equations weight

$$E_z = \frac{r}{r_z}$$
 (13.29)

So the ratio of the emfs is equal to ratio of the balancing lengths.

# SUMMARY

- The electric current is said to be caused by the motion of electric charge.
- The heat energy H produced by a current I in the wire of resistance R during a time interval t is given by H= IRt
- The passage of current is always accompanied by a magnetic field in the surrounding space

- Certain liquids conduct electricity due to some chemical reaction that takes place within them. The study of this process is known as electrolysis.
- The potential difference V across the ends of a conductor is directly proportional to the current / flowing through it provided the physical state such as temperature etc. of the conductor remains constant.
- The fractional change in resistance per kelvin is known as temperature coefficient of resistance.
- A thermistor is a heat sensitive resistor. Most thermistors have negative temperature coefficient of resistance.
- Electrical power  $P = VI = I^2 R = \frac{V^2}{R}$
- The emf E of the source is the energy supplied to unit charge by the cell
- The sum of all the currents meeting at a point in a circuit is zero is the Kirchhoff's first rule
- The algebraic sum of potential changes in a closed circuit is zero is known as Kirchtoff's second rule.

# QUESTIONS

- 13.1 A potential difference is applied across the ends of a copper wire. What is the effect on the drift velocity of free electrons by
  - (i) Increasing the potential difference
  - i, decreasing the length and the temperature of the wire
- 13.2 Do bends in a wire affect its electrical resistance? Explain
- 13.3 What are the resistances of the resistors given in the figures A and B? What is the tolerance of each? Explain what is meant by the tolerance?



- 13.4 Why does the resistance of a conductor rise with temperature?
- 13.5 What are the difficulties in testing whether the filament of a lighted bulb obeys Ohm's law?

- 13 b (is the filament resistance lower or higher in a 500 W 220 V light bulb than in a 100 W, 220 V bulb?
- 13.7 Describe a circuit which will give a continuously variing potential
- 13.8 Explain why the terminal potential difference of a battery decreases when the current drawn from it is increased?
- 13.9 What is Wheatstone bridge? How can it be used to determine an unknown resistance?

# PROBLEMS

- 13.1 How many electrons pass through an electric συίν in one minute if the 300 mA current is passing through it? (Ans: 1.12 x 10<sup>20</sup>)
- 13.2 A charge of 90 C passes through a wire in 1 hour and 15 minutes. What is the current in the wire? (Ans: 20 mA)
- 13.3 Find the equivalent resistance of the circuit (Fig.P.13.3), total current drawn from the source and the current through each resistor.

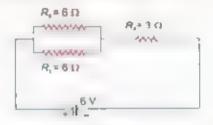
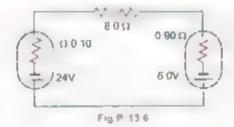


Fig. P. 13.3 (Ans: 6.0 Ω, 1.0 A, 0.5 A, 0.5 A, 1.0 A)

- A rectangular bar of iron is 2.0 cm by 2.0 cm in cross section and 40 cm long Calculate its resistance if the resistivity of iron is 11 x 10 °Ωm (Ans: 1.1 x 10 °Ω)
- The resistance of an iron wire at 0 °C is 1 x 10° Ω. What is the resistance at 500 °C if the temperature coefficient of resistance of iron is 5.2 x 10° K '? (Ans. 3.6 x 10° Ω)
  - Calculate terminal potential difference of each of cells in circuit of Fig. P 13.6



(Ans: 23.8 V, 7.8 V)

Find the current which flows in all the resistances of the circuit of Fig. P 13.7

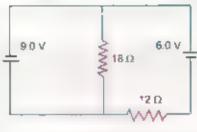
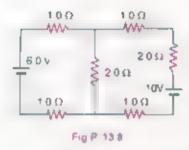


Fig. P. 13.7 (Ans: 1.25 A, 0.5 A)

Find the current and power dissipated in each resistance of the circuit, shown in Fig. P 13.8.



(Ans: 0 8 A, 1 4 A, 2 2 A, 0 64 W, 1 96 W, 3 92 W, & 9 68 W)

# Chapter 14

# **ELECTROMAGNETISM**

## **Learning Objectives**

At the end of this chapter the students will be able to:

- Appreciate that a force might act on a current carrying conductor placed in a magnetic field.
- Define magnetic flux density and the tesla.
- Derive and use the equation  $F = B/L \sin\theta$  with directions
- 4 Understand how the force on a current carrying conductor can be used to measure the magnetic flux density of a magnetic field using a current balance
- 5 Describe and sketch flux patterns due to a long straight wire
- Define magnetic flux and the weber.
- Derive and use the relation Φ = B.A.
- Understand and describe Ampera's law.
- Appreciate the use of Ampere's law to find magnetic flux density inside a solenoid.
- Appreciate that there acts a force on a charged particle when it moves in a uniform magnetic field and in electric field.
- Describe the deflection of beams of charged particles moving in a uniform magnetic field
- 12 Understand and describe method to measure e/m
- 13 Know the basic principle of cathode ray oscilloscope and appreciate its use.
- 14 Derive the expression of torque due to couple acting on a coil
- 15 Know the principle, construction and working of a galvanometer
- 16 Know how a galvanometer is converted into a voltmeter and an ammeter.
- 17 Describe and appreciate the use of AVO meter/multimeter.
- 18 Read through analogue scale and digital display on electrical meters.

lectric current generates magnetic field. At the same time, a changing magnetic field produces electric current. This interplay of electricity and magnetism is widely used in a number of electrical devices and appliances in modern age technology.

# 14.1 MAGNETIC FIELD DUE TO CURRENT IN A LONG STRAIGHT WIRE

Take a straight, thick copper wire and pass it vertically through a hole in a horizontal piece of cardboard. Place small compass needles on the cardboard along a circle with the centre at the wire. All the compass needles will point in the direction of N - S. Now pass a heavy current through the wire. It will be seen that the needles will rotate and will set themselves tangential to the circle (Fig. 14.1 a). On reversing the direction of current, the direction of needles is also reversed. As the current through the wire is stopped, all the needles again point along the N - S direction.

Following conclusions can be drawn from the above mentioned experiment:

- A magnetic field is set up in the region surrounding a current carrying wire
- The lines of force are circular and their direction depends upon the direction of current.
- (III) The magnetic field lasts only as long as the current is flowing through the wire.

The direction of the lines of force can be found by a rule concluded directly from the above experiment which is stated as follows:

If the wire is grasped in fist of right hand with the thumb pointing in the direction of the current, the fingers of the hand will circle the wire in the direction of the magnetic field.

This is known as right hand rule and is illustrated in Fig. 14.1 (b).

# 14.2 FORCE ON A CURRENT CARRYING CONDUCTOR IN A UNIFORM MAGNETIC FIELD

We have seen that a current carrying conductor sets up its own magnetic field. If such a conductor is placed in an external magnetic field, the magnetic field of the conductor will interact with the external magnetic field, as a result of which the conductor may experience a force. To demonstrate

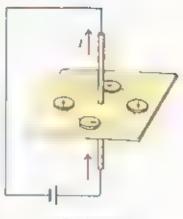


Fig. 14.1 (a)

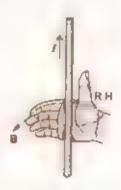
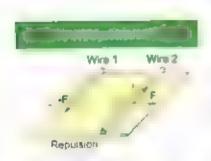


Fig. 14.1 (b)

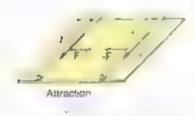
#### Do You Know?

If the middle finger of the right hand points in the direction of the magnetic flext, the thumb in the direction of current, the force on the conductor will be normal to the palm towards the reader.



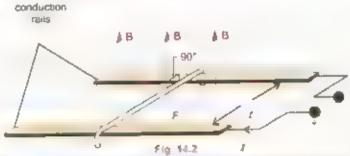


tuck



Two long perellel wires carrying currents and in apposite direction repereach other. The wires attract each other when the currents are in the same direction.

this effect consider a rod of copper, capable of moving on a pair of copper rails. The whole arrangement is placed in between the pole pieces of a horseshoe magnet so that the copper rod is subjected to a magnetic field directed vertically upwards (Fig. 14-2).



When a current is passed through the copper rod from a battery, the rod moves on the rails. The relative directions of the current, magnetic field and the motion of the conductor are shown in Fig. 14.3. It can be seen that the force on a conductor is always at right angles to the plane which contains the rod and the direction of the magnetic field. The magnitude of the force depends upon the following factors.

The force F is directly proportional to sind where a is the angle between the conductor and the field. From this it follows that the force is zero if the rod is placed parallel to the field and is maximum when the conductor is placed at right angles to the field.

The force F is directly proportional to the current / flowing through the conductor. The more the current, greater is the force.

#### Fri

The force F is directly proportional to the length L of the conductor inside the magnetic field

#### FaL

The force F is directly proportional to the strength of the applied magnetic field. The stronger the field, the greater is the force, if we represent the strength of the field by B, then

Fx B

Combining all these factors

Fr ILBsina

where k is constant of proportionality. If we follow SI units, the value of k is 1. Thus in SI units.

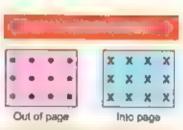
Eq 14.1 provides a definition for the strength of magnetic field. If I = 1 A, L = 1 m and  $\alpha = 90^\circ$ , then F = B. Thus B, the strength of magnetic field which is also known as magnetic induction is defined as the force acting on one metre length of the conductor placed at right angle to the magnetic field when 1 A current is passing through it. In SI units the unit of B is tesia. A magnetic field is said to have a strength of one tesla if it exerts a force of one newton on one metre length of the conductor placed at right angles to the field when a current of one ampere passes through the conductor. Thus

It can be seen that the force on a current carrying conductor is given both in magnitude and direction by the following equation:

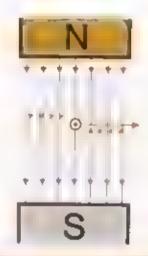
where the vector  $\mathbf{L}$  is in the direction of current flow. The magnitude of the vector  $I(\mathbf{L}) \times \mathbf{B}$  is  $I(\mathbf{L}) \times \mathbf{B} \times \mathbf{I} \times \mathbf{I} \times \mathbf{B} \times \mathbf{I} \times \mathbf{I} \times \mathbf{B} \times \mathbf{I} \times$ 

Consider a straight current carrying conductor held at right angle to a magnetic field such that the current flows out of the plane of paper i.e., towards the reader as shown in Fig. 14.4. It is customary to represent a current flowing towards the reader by a symbol dot (\*) and a current flowing away from him by a cross (x).

In order to find the direction of force, consider the lines of force (Fig. 14.4). The two fields tend to reinforce each other on left hand side of the conductor and cancel each other on the right side of it. The conductor tends to move towards the weaker part of the field i.e., the force on the conductor will be directed towards right in a direction at right angles to both the



Convention to represent direction



The magnotic force on the current placed at sight angle or email ask. Held

conductor and the magnetic field. This rule is often referred as extension of right hand rule. It can be seen that the direction of the force is the same as given by the direction of the vector L x B.

Example 14.1: A 20.0 cm wire carrying a current of 10.0 A is placed in a uniform magnetic field of 0.30 T. If the wire makes an angle of 40° with the direction of magnetic field, find the magnitude of the force acting on the wire.

#### Solution:

Length of the wire = L = 20.0 cm = 0.20 m

Current = / = 10.0A

Strength of magnetic field = B = 0.30 T

Angle = a = 40°

Substituting these values in the equation

F-/BLsina

F= 10 0Ax 0 30 Tx 0 20 m x sin40° = 0 39 N

# 14.3 MAGNETIC FLUX AND FLUX DENSITY

Like electric flux, the magnetic flux  $\Phi_e$  through a plane element of area A in a uniform magnetic field B is given by dot product of B and A (Fig. 14.5)

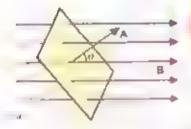
$$\Phi_a = B.A$$

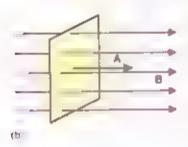
(14.3)

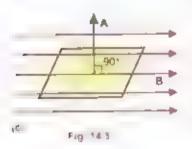
Note that A is a vector whose magnitude is the area of the element and whose direction is along the normal to the surface of the element.  $\theta$  is the angle between the directions of the vectors B and A.

In Fig. 14.5 (b) the field is directed along the normal to the area, so  $\theta$  is zero and the flux is maximum, equal to BA. When the field is parallel to the plane of the area (Fig. 14.5 c), the angle between the field and normal to area is  $90^{\circ}$  i.e.,  $\theta = 90^{\circ}$ , so the flux through the area in this position is zero.

In case of a curved surface placed in a non uniform magnetic field the curved surface is divided into a number of small surface elements, each element being assumed plane and the flux through the whole curved surface is calculated by sum of the contributions from all the elements of the surface From the definition of testal the unit of magnetic flux is NmA' which is called weber (Wb).







According to Eq. 14.3, the magnetic induction **B** is the flux per unit area of a surface perpendicular to **B** hence it is also called as flux density its unit is then Wbm. Therefore, magnetic induction itell the magnetic field strength is measured in terms of Wbm. or NA. in (testa).

**Example 14.2:** The magnetic field in a certain region is given by **B** = (401-18k) Wbm. How much flux passes through a 5.0 cm² area loop in this region if the loop kes flat in the xy- plane?

#### Solution:

Magnetic induction =  $\mathbf{B} = 40\,\hat{\mathbf{i}} - 18\,\hat{\mathbf{k}}$ Area of the loop =  $\mathbf{A} = 5.0 \times 10^{4} \text{m} \cdot \hat{\mathbf{k}}$ Flux =  $\Phi_a = \mathbf{B}$ ,  $\Delta \mathbf{A}$ =  $(40\,\hat{\mathbf{i}} - 18\hat{\mathbf{k}}) \cdot (5.0 \times 10^{4} \text{m} \cdot \hat{\mathbf{k}})$  $\Phi_a = 90 \times 10^{4} \text{Wb}$ 

# 14.4 AMPERE'S LAW AND DETERMINATION OF FLUX DENSITY B

We know that an electric current produces a magnetic field Ampere after carrying out a series of experiments, generalized his results into a law known as Ampere circuitat law by which the magnetic flux density Blat any point due to a current carrying conductor can be easily computed as explained below:

Consider a closed path in the form a circle of radius r enclosing the current carrying wire (Fig 14.6). This closed path is referred as Amperean path. Divide this path into small elements of length like  $\Delta L$ . Let B be the value of flux density at the site of  $\Delta L$ . Determine the value of B. $\Delta L$ . If  $\theta$  is the angle between B and  $\Delta L$ , then

#### B.AL = BAL cos8.

B cos9 represents the component of B along the element of length  $\Delta L$  i.e. Component of B parallel to  $\Delta L$ . Thus B. $\Delta L$  represents the product of the length of the element  $\Delta L$  and the component of B parallel to  $\Delta L$ . Ampere stated that the sum of the quantities B. $\Delta L$  for all path elements into which the complete loop has been divided equals  $\mu_e$  times the total current enclosed by the loop, where  $\mu_e$  is a constant, known



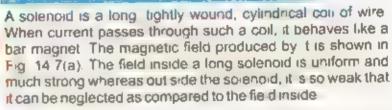
F 14 / Ampère's law to find the magne ic field in the vicinity of this long straight current-carrying wire

as permeability of free space. In SI units its value is  $4\pi \times 10$  WbA m . This can be mathematically expressed as

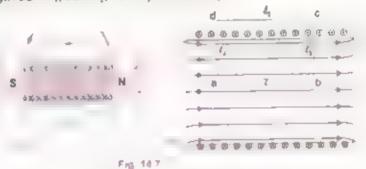
$$(B.\Delta L)_1 + (B.\Delta L)_2 + .... + (B.\Delta L)_n + .... + (B.\Delta L)_n = \mu_0 I$$

or 
$$\sum_{r=1}^{N} (\mathbf{B}.\Delta \mathbf{L})_{r=j,k_{o}} f$$
 ...... (14.4)

where (B.AL), is the value of B.AL along the rith element and N is the total number of elements into which the loop has been divided. This is known as Ampere's circuital law.



The value of magnetic filed **B** can be easily determined by applying Ampere's circuital law. Consider a rectangular loop abod as shown in Fig. 14.7 (b). Divide t into four elements of length  $ab = r_0$ ,  $bc = r_2$ ,  $cd = r_3$  and  $da = r_4$ .



Applying Ampere's law, we have

$$\sum_{i=1}^4 (\mathbf{B}.\Delta \mathbf{L})_{i:} = \mu_{i:} \times \text{current enclosed}$$

 $(\mathbf{B}.\Delta\mathbf{L})_{i}+(\mathbf{B}.\Delta\mathbf{L})_{j}+(\mathbf{B}.\Delta\mathbf{L})_{j}+(\mathbf{B}.\Delta\mathbf{L})_{i}=\mu_{a}\times$  current enclosed

Now we will calculate the value of **B.AL** for each of the elements. First we will consider the element ab = \(\epsilon\) that ies inside the solenoid. Field inside the solenoid is uniform and is parallel to. (Fig. 14.7b), so

For the element cd = r, that lies outside the solenoid, the field **B** sizero, so

Again **B** is perpendicular to  $\ell_2$  and  $\ell_4$  inside the solenoid and is zero outside, so

$$(\mathbf{B}, \Delta \mathbf{L})_a = (\mathbf{B}, \Delta \mathbf{L})_a = 0$$

$$\sum_{i=1}^{4} (\mathbf{B} \cdot \Delta \mathbf{L}) = \mathbf{B} \ell_i = \mu_o \times \text{current enclosed}$$

To find the current enclosed, consider the rectangular surface bounded by the loop abcda.

If n is the number of turns per unit length of the solenoid, the rectangular surface will intercept no turns, each carrying a current / So the current enclosed by the loop is no / Thus Ampere's law gives

$$B = \mu_n \times n i J$$

or B = µ<sub>0</sub>n / ...... (14.5)

The field B is along the axis of the solenoid and its direction is given by right hand grip rule which states "hold the solenoid in the right hand with fingers curling in the direction of the current, the thumb will point in the direction of the field"

Example 14.3: A solehold 15.0 cm long has 300 turns of wire Acutrent of 5.0 Aflows through it. What is the magnitude of magnetic field inside the solehold?

### Solution:

Length of the solehold = L = 15.0 cm = 0.15 m

Total number of turns = N = 300

Current = 1 - 5 0 A

Permeability of free space = μ<sub>n</sub> = 4π x 10. WbA, m.\*

Number of turns per unit length =  $n = \frac{N}{\sqrt{0.15 \text{ m}}}$ 

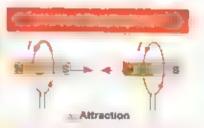
= 2000 turns/m

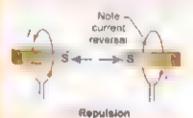
Magnetic field –  $B = \mu_n n I$ 





The current loop can be imagined to be a phantom bat magnet with a north-pole and a south pole.





The "phantom" magnet included for each loop helps to explain the affraction and repulsion between the loops.

# 14.5 FORCE ON A MOVING CHARGE IN A MAGNETIC FIELD

We have seen that a current carrying conductor when placed in a magnetic field expenences a force. The current through the conductor is because of the motion of charges. Actually the magnetic field exerts force on these moving charges due to which the conductor expenences force. We are interested in calculating the force exerted on the moving charges.

Consider the situation as shown in Fig. 14.8 where we see a portion of the wire that is carrying a current / Suppose there are n charge camers per unit volume of the wire, and that each is moving with velocity via shown. We will now find how long it takes for all the charge camers originally in the wire sagment shown to exit through the end area A.

The volume of the wire segment is AL. Because there are n charge carners per unit volume, the number of charge carner in the segment is nAL. If the charge on a charge carner is q, each of it, as it crosses the end area will transport a charge q through it. Assuming the speed of the carriers to be q, the carner entening the left face of the segment takes a time  $\Delta t = L/v$  to reach the right hand face. During this time, all the charge carners originally in the segment namely nAL, will exit through the right hand face. As each charge carner has a charge q, the charge  $\Delta Q$  that exits through the end area in time  $\Delta t = L/v$  is



Then from the definition of the current, the current / through the conductor is

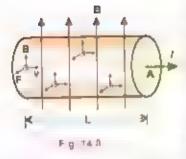
$$I = \frac{\Delta Q}{\Delta t} = \frac{n A L q}{L / v}$$

$$= n A q v \tag{14.6}$$

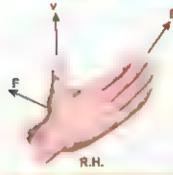
By Eq 14.2, the force on the segment L of a conductor, carrying current / is given by

Substituting the value of the current I.

$$F_{i} = nAgvL \times B$$
 (14.7)







The moving charge experiences a magnetic force F because of the magnetic field B

In Fig. 14.8, it can be seen that the direction of the segment  $\mathbf{L}$  is the same as the direction of the velocity of the charge carriers if  $\hat{\mathbf{L}}$  is a unit vector along the direction of the segment  $\mathbf{L}$  and  $\hat{\mathbf{v}}$ , a unit vector along the velocity vector  $\mathbf{v}$ , then  $\hat{\mathbf{L}} = \hat{\mathbf{v}}$ 

Substituting the value of v L in Eq. 14.7, we have

$$F_{v} = nAq(vL)xB$$

= nALqvxB

n AL is the total number of charge carries in the segment L, so the force experienced by a single charge carrier is

$$F = \frac{F_c}{nAL} = q \times B$$

Thus the force experienced by a single charge carrier moving with velocity v in magnetic field of strength B is

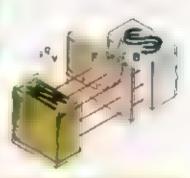
$$F = q(v \times B) \tag{14.8}$$

Although the Eq 14.8 has been derived with reference to charge carrier moving in a conductor but it does not involve any parameter of the conductor so the Eq 14.8 is quite general and it holds for any charge carrier moving in a magnetic field

If an electron is projected in a magnetic field with a velocity  $\mathbf{v}$ , it will experience a force which is given by putting q = -e in Eq. 14.8 where e is the magnitude of the electronic charge.

In case of proton, F is obtained by putting q = +e

Note that in case of proton or a positive charge the direction of the force is given by the direction of the vector  $\mathbf{v} \times \mathbf{B} + \mathbf{e}$ , rotate  $\mathbf{v}$  to coincide with  $\mathbf{B}$  through the smaller angle of rotation and curl the fingers of right hand in the direction of rotation. Thumb will point in the direction of the force. This is illustrated in Fig 14.9 in which the proton enters into a magnetic field, as shown in figure, along the direction of dotted line. It experiences a force in the upward direction as given by the vector  $\mathbf{v} \times \mathbf{B}$ . As a result of this force the proton is deflected upwards as shown in Fig. 14.9. The direction of the force on a moving negative charge will be opposite to that of positive charge. Due to this force, the electron is deflected in the downward direction as it enters into a magnetic field. It



Magnetic force F is perpendicular to both the magnetic field B and the velocity v and causes the particle's trajectory to bend in a vertical plane.

may be noted that the magnitude of the force on a moving charge camer is  $qvB\sin\theta$  where  $\theta$  is the angle between the velocity of the camer and the magnetic field. It is maximum when  $\theta=90^\circ$  i.e., when the charged particle is projected at right angles to the field. It is zero when  $\theta=0^\circ$  i.e., a charged particle projected in the direction of the field experiences no force.

# 14.6 MOTION OF CHARGED PARTICLE IN AN ELECTRIC AND MAGNETIC FIELD

When an electric charge q is placed in an electric field E, It expensions a force Fiparallel to electric field (Fig. 14.10). It is given by

$$F = qE$$

If the charge is free to move then it will accelerate according to Newton's second law as

$$\mathbf{a} = \frac{\mathbf{F} \quad q \, \mathbf{E}}{m \quad m} \tag{14.11}$$

If electric field is uniform, then acceleration is also uniform and hence, the position of the particle at any instant of time can be found by using equations of uniformly accelerated motion.

When a charge particle q is moving with velocity  $\mathbf{v}$  in a region where there is an electric field  $\mathbf{E}$  and magnetic field  $\mathbf{B}$ , the total force  $\mathbf{F}$  is the vector sum of the electric force q  $\mathbf{E}$  and magnetic force q  $(\mathbf{v} \times \mathbf{B})$  that is,

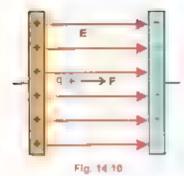
$$F = F_a + F_b$$

$$F = qE + q(vxB)$$
 ........ (14 12)

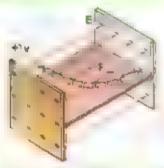
This force F is known as the Lorentz force. It is to be pointed out that only the electric force does work, while no work is done by the magnetic force which is simply a deflecting force.

## 14.7 DETERMINATION OF e/m OF AN ELECTRON

Let a narrow beam of electrons moving with a constant speed vibe projected at right angles to a known uniform magnetic field **B** directed into plane of paper. We have seen that electrons will experience a force.







The electric force if that acts on a positive charge is parallel to the spectric field E and causes the particle's trajectory to bend in a longontal plane.

The direction of the force will be perpendicular to both  $\mathbf{v}$  and  $\mathbf{B}$ . As the electron is experiencing a force that acts at right angle to its velocity, so it will change the direction of the velocity. The magnitude of velocity will remain unchanged. The magnitude of the force is  $evB\sin\theta$ . As  $\theta$  is  $90^\circ$ , so F = evB. As both v and B do not change, the magnitude of F is constant. Thus the electrons are subjected to a constant force evB at right angle to their direction of motion. Under the action of this force, the electrons will move along a circle as shown in Fig. 14.11

The magnetic force F = Bev provides the necessary centripetal force  $\frac{mv^2}{f}$  to the electron of mass m to move along a circular trajectory of radius. Thus we have

$$Bev = \frac{mv^2}{r}$$
or 
$$\frac{\theta}{m} = \frac{v}{Br}$$
 (14.13)

If v and r are known, e/m of the electron is determined. The radius r is measured by making the electronic trajectory visible. This is done by filling a glass tube with a gas such as hydrogen at low pressure. This tube is placed in a region occupied by a uniform magnetic field of known value. As electrons are shot into this tube, they begin to move along a circle under the action of magnetic force. As the electrons move, they collide with atoms of the gas. This excites the atoms due to which they emit light and their path becomes visible as a circular ring of light (Fig. 14.12). The diameter of the ring can be easily measured.

In order to measure the velocity v of the electrons, we should know the potential difference through which the electrons are accelerated before entening into the magnetic field. If V is this potential difference, the energy gained by electrons during their acceleration is Ve. This appears as the kinetic energy of electrons.

$$\frac{1}{2}mv^2 = Ve$$

$$V = \sqrt{\frac{2Ve}{m}}$$

or

Substituting the value of vin Eq. 14.13, we have

$$\frac{\mathbf{e}}{m} = \frac{2V}{B^2 r^2} \qquad \dots \tag{14.14}$$

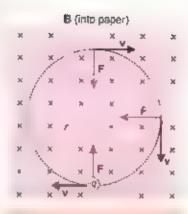


Fig 14.11 An electron is moving perpendicular to a constant magnetic field. The magnetic force F causes the particle to move on a circular path.



Fig. 14.12

Example 14.4: Find the radius of an orbit of an electron moving at a rate of 2.0 x 10<sup>7</sup> ms. the uniform magnetic field of 1.20 x 10<sup>7</sup> T.

#### Solution:

Speed of the electron 
$$= v = 2.0 \times 10^7 \text{ ms}^3$$
  
Magnetic field strength  $= B = 1.20 \times 10^{13} \text{ T}$   
Mass of the electron  $= m = 9.11 \times 10^{19} \text{ C}$   
Charge on electron  $= e = 1.61 \times 10^{19} \text{ C}$ 

The radius of the orbit is

$$r = \frac{mv}{68}$$
=\frac{9.11 \times 10^{-31} \text{ kg} \times 2.0 \times 10^7 \text{ ms}}{1.61 \times 10^{-19} \text{ C} \times 1.20 \times 10^{-3} \text{ T}}
$$r = 9.43 \times 10^{3} \text{ m}$$

**Example 14.5:** Alpha particles ranging in speed from 1000 ms to 2000 ms enter into a velocity selector where the electric intensity is 300 Vm and the magnetic induction 0.20 T. Which particle will move undeviated through the field?

### Solution:

E=300 Vm"=300 NC" , B=0 20 T

Only those particles will be able to pass through the plate for which the electric force eE acting on the particles balances the magnetic force Bevion the particle as shown in the figure

Therefore eE = Bev
Thus, the selected speed is

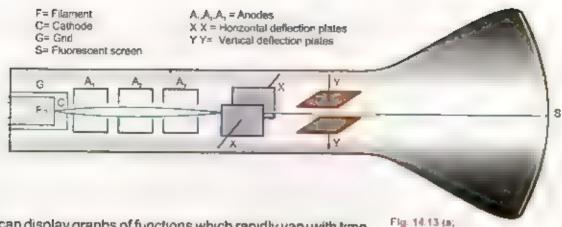
$$v = \frac{E}{B} = \frac{300 \,\text{NC}^{-1}}{0.20 \,\text{NA}^{-1}\text{m}^{-1}} = 1500 \,\text{ms}^{-1}$$

The alpha particles having a speed of 1500 ms will move undeviated through the field

## 14.8 CATHODE RAY OSCILLOSCOPE

Cathode ray oscilloscope (CRO) is a very versatile electronic instrument which is in fact, a high speed graph plotting device. It works by deflecting beam of electrons as they pass through uniform electric field between the two sets of parallel plates as shown in the Fig. 14-13(a). The deflected beam then fails on a fluorescent screen where it makes a visible spot.



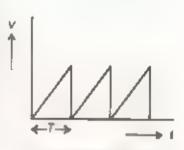


It can display graphs of functions which rapidly vary with time. It is called cathode ray oscilloscope because it traces the desired waveform with a beam of electrons which are also called cathode rays.

The beam of the electrons is provided by an electron gun which consists of an indirectly heated cathode, a gnd and three anodes. The filament F heats the cathode C which emits electrons. The anodes A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub> which are at high positive potential with respect to cathode, accelerate as well as focus the electronic beam to fixed spot on the screen S. The grid G is at a negative potential with respect to cathode. It controls the number of electrons which are accelerated by anodes, and thus it controls the brightness of the spot formed on the screen.

Now we would explain how the waveform of various voltages is formed in CRO.

The two set of deflecting plates, shown in Fig. 14.13(a) are usually referred as x and y deflection plates because a voitage applied between the x plates deflects the beam horizontally on the screen i.e. parallel to x-axis. A voltage applied across the y plates deflects the beam vertically on the screen i.e., along the y-axis. The voltage that is applied across the x plates is usually provided by a circuit that is built in the CRO. It is known as sweep or time base generator. Its output, waveform is a saw tooth voltage of period. The voltage increases linearly with time for a period. Then then drops to zero. As this voltage is impressed across the x plates, the spot is deflected linearly with time along the x-axis for a time. Then the spot returns to its starting point on the screen very quickly because a saw tooth voltage, rapidly falls to its initial value at the end of each

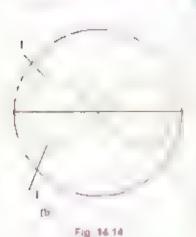


Saw looth voltage waveform Fig. 14.13 (b)



Fig. 14 13 (b) hired dimensional view of CRO

period. We can actually see the spot moving on the x-axis. If the time period T is very short, we see just a bright I ne on the screen



If a sinusoidal voltage is applied across the y plates when simustaneously the time base voltage is impressed across the x piates the sinusoidal voltage which itself gives rise to a vertical line, will now spread out and will appear as a sinusoidal trace on the screen. The pattern will appear stationary only if the time T is equal to or is some multiple of the time of one cycle of the voltage only plates. It is thus necessary to synchronize the frequency of the time base generator with the frequency of the voltage at the y plates. This is possible by adjusting the synchronization controls provided on the front panel of the CRO.

The CRO is used for displaying the waveform of a given voltage. Once the waveform is displayed, we can measure the voltage, its frequency and phase. For example, Fig. 14-14(a) shows the waveform of an a ternaling voltage. As the y-axis is calibrated in volts and the x-axis in time, we can easily find the instantaneous value and peak value of the voltage. The time period can also be determined by using the time calibration of x-axis, information about the phase difference between two voltages can be obtained by simultaneously displaying their waveforms. For example, the waveforms of two voltages are shown in Fig. 14-14(b). These waveforms show that when the voltage of Lis increasing, that of It is decreasing and vice versa. Thus the phase difference between these voltages is 180°.

# 14.9 TORQUE ON A CURRENT CARRYING

Consider a rectangular coil carrying a current / The coil is capable of rotation about an axis. Suppose it is placed in uniform magnetic field  $\bf B$  with its plane along the field (Fig. 14-15). We know that a current carrying conductor of length  $\bf L$  when placed in a magnetic field experiences a force  $F=ILB\sin\theta$  where  $\theta$  is the angle between conductor and the field. In case of sides AB and CD of the coil, the angle  $\theta$  is zero or  $180^\circ$ , so the force on these sides will be zero. In case of sides DA and BC, the angle  $\theta$  is  $90^\circ$  and the force on these sides will be

$$F_1 = F_2 = ILB$$

where L is the length of these sides F, is the force on the side DA and F<sub>2</sub> on BC. The direction of the force is given by the vector / L x B. It can be seen that F, is directed out of the plane of paper and F<sub>2</sub> into the plane of paper (Fig. 14.15 a). Therefore, the forces F, and F<sub>2</sub> being equal and opposite form a couple which tends to rotate it about the axis. The torque of this couple is given by

where a is the moment arm of the couple and is equal to the length of the side AB or CD. La is the area A of the coil.

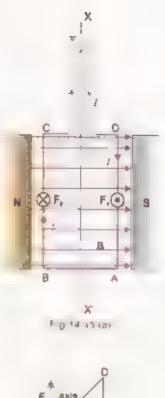
Note that the Eq. 14.15 gives the value of torque when the field B is in the plane of the coil. However if the field makes an angle  $\alpha$  with the plane of the coil, as shown in Fig. 14.15(b) the moment arm now becomes a cos $\alpha$ . So

$$\tau = ILB \times a\cos\alpha$$
 or 
$$\tau = IBA\cos\alpha \qquad (14.16)$$

## 14.10 GALVANOMETER

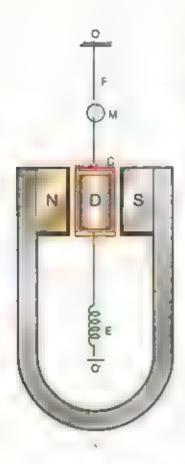
A galvanometer is an electrical instrument used to detect the passage of current. Its working depends upon the fact that when a conductor is placed in a magnetic field, it experience a force as soon as a current passes through it. Due to this force, a torque it acts upon the conductor if it is in the form of a coil or loop.

where N is the number of turns in the coil. A is its area, I is current passing through it, B is the magnetic field in which the coil is placed such that its plane makes an angle of with the direction of B. Due to action of the torque, the coil rotates and





(Top view of coil) Fig 14 15 (b)



N S

(a) Moving coil galvanomater (b) Concave pole piece and soft iron cylinder makes the field radial and stronger

thus it detects the current. The construction of a moving coil galvanometer is shown in Fig. 14.16 (a)

A rectangular coil C is suspended between the concave shaped poles N and S of a U-shaped magnet with the help of a fine metallic suspension wire. The rectangular coil is made of enameled copper wire. It is wound on a frame of non-magnetic material. The suspension wire F is also used as one current lead to the coil. The other terminal of the coil is connected to a loosely wound spiral E which serves as the second current lead. A soft iron cylinder D is placed inside the coil to make the field radial and stronger near the coil as shown in Fig. 14.16 (b).

When a current is passed through the coil it is acted upon by a couple which tends to rotate the coil. This couple is known as deflecting couple and is given by N / B A cosu. As the coil is placed in a radial magnetic field in which the plane of the coil is always parallel to the field (Fig. 14.16 b) so  $\alpha$  is always zero. This makes  $\cos \alpha = 1$  and thus,

#### Deflecting couple = N / B A

As the coil turns under the action of deflecting couple the suspension wire Fig. (14-16 a) is twisted which gives rise to a torsional couple. It tends to untwist the suspension and restore the coil to its original position. This couple is known as restoring couple. The restoring couple of the suspension wire is proportional to the angle of deflection  $\theta$  as long as the suspension wire obeys Hooke's law. Thus

#### Restoring torque = c 8

where the constant c of the suspension wire is known as torsional couple and is defined as couple for unit twist

Under the effect of these two couples coil comes to rest when Deflecting torque = Restoring torque

or 
$$I \approx \theta$$
  $I \approx \theta$   $I \approx \theta$  (14.17)

Thus  $I \approx \theta$  since  $\frac{c}{BAN} = \text{Constant}$ 

Thus the current passing through the coil is directly proportional to the angle of deflection.

There are two methods commonly used for observing the angle of deflection of the coil in sensitive galvanometers the angle of deflection is observed by means of small mirror attached to the coil along with a lamp and scale arrangement (Fig. 14-17). A beam of light from the lamp is directed towards the mirror of the galvanometer. After reflection from the mirror it produces a spot on a translucent scale placed at a distance of one metre from the galvanometer. When the coil rotates, the mirror attached to coil also rotates and spot of light moves along the scale. The displacement of the spot of light on the scale is proportional to the langle of deflection (provided the angle of deflection is small).

The galvanometer used in school and college laboratories is a pivoted type galvanometer. In this type of galvanometer, the coil is pivoted between two jewelled bearings. The restoring torque is provided by two hair springs which also serve as current leads. A light alumin um pointer is attached to the coil which moves over a scale (Fig. 14-18). It gives the angle of deflection of the coil.

It is obvious from Eq. 14-17 that a ga vanometer can be made more sensitive (to give large deflection for a given current) if ciBAN is made small. Thus, to increase sensitivity of a galvanometer ic may be decreased or B. A and N may be increased. The couple c for tin t twist of the suspension wire can be decreased by increasing its length and by decreasing ts d'ameter. This process, however, cannot be taken too far as the suspension must be strong enough to support the co-Another method to increase the sensitivity of galvanometer is to increase N, the number of turns of the coil in case of suspended coil type garvanometer, the number of turns can not be increased beyond a limit because it will make the coil heavy. To compensate for the loss of sensitivity in case. fewer turns are used in the coil, we increase the value of the magnetic field employed. We define current sensitivity of a galvanometer as the current in microamperes, required to produce one milimetre deflection on a scale placed one metre away from the mirror of the galvanometer.

When the current passing through the galvanometer is discontinued the coil will not come to rest as soon as the current flowing through the coil is stopped it keeps on oscillating about its mean position before coming to rest in the same way if the current is established suddenly in a galvanometer the coil will shoot beyond its final equilibrium position and will oscillate several times before coming to rest

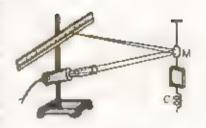
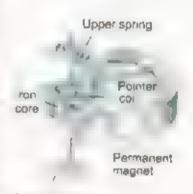


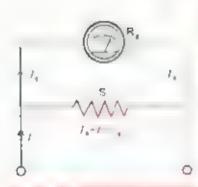
Fig. 14.17



Lower spring

Fig. 14-18

at its equilibrium position. As it is annoying and time consuming to wait for the coil to come to rest, artificial ways are employed to make the coil come to rest quickly. Such galvariometer in which the coil comes to rest quickly after the current passed through it or the current is stopped from flowing through it, is called stable or a dead beat galvariometer.



F 1.11 An ommeter 5 5 galvanometer which 5 shorted by a proper low realistance

An ammeter is an electrical instrument which is used to measure current in amperes. This is basically a galvanometer. The portion of the galvanometer whose motion causes the needle of the device to move across the scale is usually known as meter - movement. Most meter movements are very sensitive and full scale deflection is obtained with a current of few mill amperes only. So an ordinary galvanometer cannot be used for measuring large currents without proper modification.

Suppose we have a galvanometer whose meter - movement (coii) has a resistance R, and which gives full scale deflection when current  $I_s$  is passed through it. From Ohm's law we know that the potential difference  $V_s$  which causes a current  $I_s$  to pass through the galvanometer is given by

$$V_a = I_a R_a$$

If we want to convert this galvanometer into an ammeter which can measure a max mum current I it is necessary to connect a low value bypass resistor called shunt. The shunt resistance is of such a value so that the current  $I_s$  for full scale deflection of the galvanometer passes through the galvanometer and the remaining current  $I_s$  passes through the shunt in this situation (Fig. 14-19).

The shunt resistance R, can be calculated from the fact that as the meter - movement and the shunt are connected in parallel with each other, the potential difference across the meter - movement is equal to the potential difference across the shunt.

The resistance of the shunt is usually so small that a piece of

copper wire serves the purpose. The resistance of the ammeter is the combined resistance of the galvanometer's meter - movement and the shunt. Usually it is very small. An ammeter must have a very low resistance so that it does not disturb the circuit in which it is connected in series in order to measure the current.

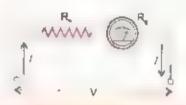
A voltmeter is an electrical device which measures the potential difference in volts between two points. This, too, is made by modifying a galvanometer. Since a voltmeter is always connected in parallel, it must have a very high resistance so that it will not short the circuit across which the voltage is to be measured. This is achieved by connecting a very high resistance  $R_n$  placed in series with the metermovement (Fig.14.20). Suppose we have a metermovement whose resistance is  $R_n$  and which deflects full scale with a current  $I_n$  in order to make a voltmeter from it which has a range of V volts, the value of the high resistance  $R_n$  should be such that full scale deflection will be obtained when it is connected across V volt. Under this condition the current through the meter - movement is  $I_n$ . Applying Ohm's law (Fig.14.20) we have

$$V = I_q (R_q + R_h)$$
 $R_h = \frac{V}{I_p} - R_g$  . . (14.19)

If the scale of the galvanometer is calibrated from 0 to V volts, the combination of galvanometer and the senes resistor acts as a voltmeter with range  $0 \cdot V$  volts. By properly arranging the resistance  $R_{\rm h}$  any voltage can be measured. Thus, we see that a voltmeter possesses high resistance.

It may be noted that a voltmeter is always connected across the two points between which potential difference is to be measured. Before connecting a voltmeter, it should be assured that its resistance is very high in companson with the resistance of the circuit across which it is connected otherwise it will load the circuit and will after the potential difference which is required to be measured.

**Example 14.6:** What short resistance must be connected across a galvanometer of 50 0  $\Omega$  resistance which gives full scale deflection with 2 0 mA current, so as to convert it into an ammeter of range 10 0A?



F : 14 Tr A galvanometer in senea with a high resistance acts as a voltmater

#### Solution:

Resistance of galvanometer - R = 50 0 Ω

Current for full scale deflection = I = 2 0 mA

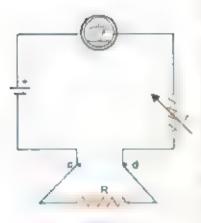
Current to be measured = I = 10 0 A

The shunt resistance R, is given by

$$R_{1} = \frac{1}{I_{a}} R_{9} = \frac{2.0 \times 10^{-3} \text{ A}}{10.0 \text{ A} + 2.0 \times 10^{-3} \text{ A}} \times 50.0 \text{ A} = 0.01 \Omega$$

#### Ohmmeter

It is a useful device for rapid measurement of resistance. If consists of a galvanometer, and adjustable resistance r, and a cell connected in senes (Fig 14 21-a). The senes resistance r, is so adjusted that when terminals c and d are short circuited, i.e., when R = 0, the galvanometer gives full scale deflection. So the extreme graduation of the usual scale of the galvanometer is marked 0 for resistance measurement. When terminals c and d are not joined, no current passes through the galvanometer and its deflect.on is zero. Thus zero of the scale is marked as infinity (Fig. 14.21-b). Now a known resistance R is connected across the terminals c and d. The galvanometer deflects to some intermediate point. This point is calibrated as R. In this way the whole scale is calibrated into resistance. The resistance to be measured is connected across the terminals c and d. The deflection on the calibrated scale reads the value of the resistance directly.



# Scale 10mA A moving co galvanometer is converted into an

#### 14.11 AVO METER - MULTIMETER

It is an instrument which can measure current in amperes, potential difference in volts and resistance in ohms. It besically consists of a sensitive moving colgalvanometer which is converted into a multirange ammeter voltmeter or ohimmeter accordingly as a current measuring circuit or a voltage measuring circuit or a resistance measuring circuit is connected with the galvanometer with the help of a switch known as function switch (Fig 14.22). Here X, Y are the main terminals of the AVO meter which are connected with the circuit in which measurement is required. FS is the function selector switch which connects the galvanometer with relevant measuring circuit.

#### Voltage Measuring Part of AVO Meter

The voltage measuring part of the AVO meter is actually a multirange voltmeter. It consists of a number of resistances each of which can be connected in series with the moving coil galvanometer with the help of a switch called the range switch (Fig. 14.23). The value of each resistance depends upon the range of the voltmeter which it controls.

Alternating voltages are also measured by AVO meter AC voltage is first converted into DC voltage by using diode as rectifier and then measured as usual

The current measuring part of the AVO meter is actually a multirange ammeter. It consists of a number of low resistances connected in parallel with the galvanometer. The values of these resistances depend upon the range of the ammeter (Fig. 14-24).

The circuit also has a range selection switch RS which is used to select a particular range of the current

#### Resistance Measuring Part of AVO Meter

The resistance measuring part of AVO meter is, in fact, a multirange chammeter C rout for each range of this meter consists of a battery of emf  $V_n$  and a variable resistance  $r_n$  connected in sense with galvanometer of resistance  $R_n$ . When the function switch is switched to position  $X_n$ . Fig. 14-22) this circuit is connected with the terminals  $X_n$  Y of he AVO meter (Fig.14-25 a).

Before measuring an unknown resistance by an ohmmeter it is first zeroed which means that we short circuit the terminals K, Y and adjust r<sub>e</sub>, to produce full scale deflection.

#### Digital Multimetor(DMM)

Inother useful device to measure resistance, current and roltage is an electronic instrument cailed digital multimeter

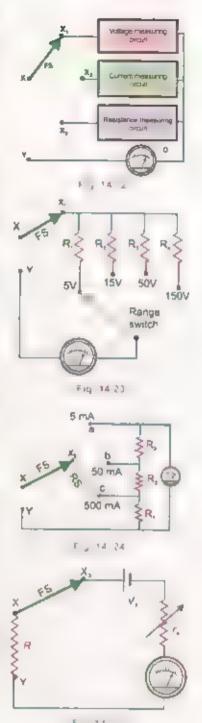




Fig 14 26

It is a digital version of an AVO meter. It has become a very popular testing device because the digital values are displayed automatically with decimal point, polarity and the unit for V. A or  $\Omega$ . These meters are generally easier to use because they eliminate the human error that often occurs in reading the dial of an ordinary AVO meter. A portable DMM is shown in Fig. 14.26.

## - DATHAGEA FIND

- A magnetic field is set up in the region surrounding a current carrying conductor.
- The right hand rule states. "If the wire is grasped in the fist of right hand with the
  thumb pointing in the direction of current, the fingers of the hand will circle the wire in
  the direction of the magnetic field"
- The strength of the magnetic field or magnetic induction is the force acting on one
  metre length of the conductor placed at right angle to the magnetic field when 1 A
  current is passing through it.
- A magnetic field is said to have a strength of one testal fill exerts a force of one
  newton on one metre length of the conductor praced at right angle to the field when a
  current of one ampere passes through the conductor
- The magnetic flux Φ, through plane element of area A in a uniform magnetic field B is given by dot product of B and A
- Ampere circuital law states the sum of the quantities B. AL for all path elements into
  which the complete loop has been divided equals pillines the total current enclosed
  by the loop.
- The force experienced by a single charge carner moving with velocity v in magnetic field of strength Bis. F = q(v × B)
- Cathode ray oscilloscope (CRO) is a high speed graph plotting device. It works by
  deflecting beam of electrons as they pass through uniform electric field between the
  two sets of parallel plates.
- A torque may act on a current carrying coil placed in a magnetic field.

#### T= / AB cosq

- A galvanometer is an electric device which detects the flow of current. It usually
  consists of a coil praced in a magnetic field. As the current passes through the coil
  the coil rotates, thus indicating the flow of current.
- Agaivanometer is converted into an ammeter by properly shunting it
- A galvanometer is converted into a voltmeter by connecting a high resistance in series.



- 14.1 A plane conducting loop is located in a uniform magnetic field that is directed along the x-axis. For what orientation of the loop is the flux a maximum? For what orientation is the flux a minimum?
- 14.2 A current in a conductor produces a magnetic field, which can be calculated using Ampere's law. Since current is defined as the rate of flow of charge, what can you conclude about the magnetic field due to stationary charges? What about moving charges?
- 14.3 Describe the change in the magnetic field inside a solenoid carrying a steady current I, if (a) the length of the solenoid is doubled but the number of turns remains the same and (b) the number of turns is doubled, but the length remains the same
- At a given instant, a proton moves in the positive x direction in a region where there is magnetic field in the negative z direction. What is the direction of the magnetic force? Will the proton continue to move in the positive x direction? Explain.
- 14.5 Two charged particles are projected into a region where there is a magnetic fleid perpendicular to their velocities. If the charges are deflected in opposite directions, what can you say about them?
- 14.6 Suppose that a charge q is moving in a uniform magnetic field with a velocity v. Why is there no work done by the magnetic force that acts on the charge q?
- 14.7 If a charged particle moves in a straight line through some region of space, can you say that the magnetic field in the region is zero?
- 14.8 Why does the picture on a TV screen become distorted when a magnet is brought near the screen?
- 14.9 Is it possible to orient a current loop in a uniform magnetic field such that the loop will not tend to rotate? Explain
- 14.10 How can a current loop be used to determine the presence of a magnetic field in a given region of space?
- 14.11 How can you use a magnetic field to separate isotopes of chemical element?
- 14.12 What should be the orientation of a current carrying coil in a magnetic field so that torque acting upon the coil is (a) maximum (b) minimum?
- 14.13 A loop of wire is suspended between the poles of a magnet with its plane parallel to the pole faces. What happens if a direct current is put through the coil? What happens if an alternating current is used instead?
- 14.14 Why the resistance of an ammeter should be very low?
- 14 15 Why the voltmeter should have a very high resistance?



14.1 Find the value of the magnetic field that will cause a maximum force of  $7.0 \times 10^{3} N$  on a 20.0 cm straight wire carrying a current of 10.0 A.

(Ans: 3.5 x 10<sup>-1</sup> T)

- How fast must a proton move in a magnetic field of 2.50 × 10° T such that the magnetic force is equal to its weight?

  (Ans: 4.09 x 10 ms.)
- A velocity selector has a magnetic field of 0.30 T if a perpendicular electric field of 10,000 Vm is applied, what will be the speed of the particle that will pass through the selector?

  (Ana: 3.3 x 10 ms 1)
- A coil of 0.1 m x 0.1 m and of 200 turns carrying a current of 1.0 mA is placed in a uniform magnetic field of 0.1 T. Calculate the maximum torque that acts on the coil.

  (Ans: 2.0 x 10<sup>4</sup> Nm)
- A power line 10.0 m high carries a current 200 A. Find the magnetic field of the wire at the ground. (Ans: 4.0 x 10°T)
  - You are asked to design a solenoid that will give a magnetic field of 0.10 T yet the current must not exceed 10.0 A. Find the number of turns per unit ength that the solenoid should have.

    (Ans: 7,96 x 10<sup>3</sup>)
- 14.7 What current should pass through a solenoid that is 0.5 m long with 10.000 turns of copper wire so that it will have a magnetic flexic of 0.4.7? (Ans: 16.0A)
- A galvanometer having an internal resistance  $R_s \approx 15.0~\Omega$  gives full scale deflection with current  $I_s = 20.0~\text{mA}$ . It is to be converted into an ammeter of range 10.0 A. Find the value of shunt resistance  $R_s = (\text{Ans}^2, 0.030~\Omega)$ .
- The resistance of a galvanometer is 50 0  $\Omega$  and reads full scale deflection with a current of 2.0 mA. Show by a diagram how to convert this galvanometer into voltmeter reading 200 V full scale. (Ans:  $R = 99950 \Omega$ )
- The resistance of a galvanometer coil is 10.0  $\Omega$  and reads full scale with a current of 1.0 mA. What should be the values of resistances R/R and R to convert this galvanometer into a multirange ammeter of 100–100 and 1.0 A as shown in the Fig P14.10?

  (Ans:  $R = 0.001 \Omega/R = 0.001 \Omega/R_1 = 0.001 \Omega$ )

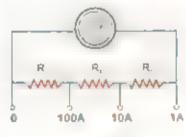


Fig. P 14 10

## Chapter 15

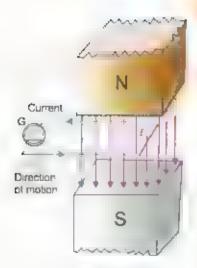
## **ELECTROMAGNETIC INDUCTION**

#### **Learning Objectives**

At the end of this chapter the students will be able to:

- 1 Recall that a changing magnetic flux through a circuit causes an emf to be induced in the circuit
- 2 Know that the induced emf-asts so long as the magnetic flux keeps changing.
- Determine Motional emf
- 4 Use Faraday's law of electromagnetic induction to determine the magnitude of induced emf.
- Apply Lenz's law to determine the direction of induced emf.
- Recognize self and mutual induction.
- 7 Define mutual inductance self-inductance and its unit henry.
- 8. Know and use the formula  $E = \frac{1}{2}LI^2$
- Calculate the energy stored in an inductance.
- 10 Describe the principle, construction and operation of an AC and DC generator
- 11 Describe the principle, construction and operation of DC motor
- 12 Recognize back emf in motors and back motor effect in generators
- 13 Describe the structure and principle of operation of transformer
- 14 Use  $\frac{N_s}{N_s} = \frac{V_s}{V_s}$  and  $V_s I_s = V_s I_s$  for an ideal transformer
- 15 Apply transformer equation to solve the problems.
- 16 Understand and describe eddy currents and use of laminated core

A sisson as Oersted discovered that electric currents produce magnetic fields, many scientists began to look for the reverse effect, that is, to cause an electric current by means of a magnetic field. In 1831 Michael Faraday in England and at the same time Joseph Henry in USA observed that an emf is set up in a conductor when it moves across a magnetic field if the moving conductor was connected to a sensitive galvanometer, it would show an electric current flowing through the circuit as long as the conductor is kept moving, in the magnetic field. The lemf produced in the conductor is called induced emf, and the current generated is called the induced current. This phenomenon is known as electromagnetic induction.



Ftg 15 1

#### 15.1 INDUCED EMF AND INDUCED CURRENT

There are many ways to produce induced emf. Fig. 15.1 illustrates one of them. Consider a straight piece of wire of length (piaced in the magnetic field of a permanent magnet. The wire is connected to a sensitive galvanometer. This forms a closed path or loop without any battery. In the beginning when the loop is at rest in the magnetic field, no current is shown by the galvanometer. If we move the loop from left to right, the length (of the wire is dragged across the magnetic field and a current flows through the loop. As we stop moving the loop current also stops. Now if we move the loop in opposite direction, current a so reverses its direction. This is indicated by the deflection of the gaivanometer in opposite direction.

The induced current depends upon the speed with which conductor moves and upon the resistance of the loop if we change the resistance of the loop by inserting different resistors in the loop, and move it in the magnetic field with the same speed every time, we find that the product of induced current / and the resistance R of the loop remains constant, i.e.

#### /xR=constant

This constant is the induced emf. The induced emf leads to an induced current when the circuit is closed. The current can be increased by

- i) Using a stronger magnetic field
- moving the loop faster
- iii) replacing the loop by a coil of many turns

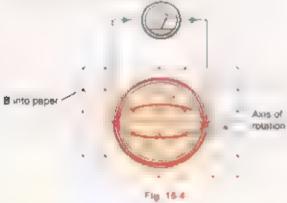
If we perform the above experiment in the other way, existed of moving the loop across the magnetic field we keep the loop stationary and move the magnet, then it can be easily observed that the results are the same. Thus, it can be concluded that it is the relative motion of the loop and the magnet that causes the induced emf.

In fact, this relative motion changes the magnetic flux through the loop, therefore, we can say that an induced emf is produced in a loop if the magnetic flux through it, changes. The greater the rate of change of flux, the larger is the induced emf.

There are some other methods described below in which an emf is induced in a loop by producing a change of magnetic

#### flux through it.

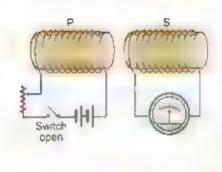
- Fig 15.2 (a) shows a bar magnet and a coil of wire to which a galvanometer is connected. When there is no relative motion between the magnet and the coil, the galvanometer indicates no current in the circuit. As soon as the bar magnet is moved towards the coil, a current appears in it (Fig 15.2 b). As the magnet is moved, the magnetic flux through the coil changes, and this changing flux produces the induced current in the coil. When the magnet moves away from the coil, a current is again induced but now in opposite direction. The current would also be induced if the magnets were held stationary and the coil is moved.
- There is another method in which the current is induced in a coil by changing the area of the coil in a constant magnetic field. Fig. 15.3 (a) shows that no current is induced in the coil of constant area, placed in a constant magnetic field. However, when the coil is being distorted so as to reduce its area, (Fig. 15.3 b) an induced emf and hence current appears. The current vanishes when the area is no longer changing if the distorted coil is brought to its ong nal circular, shape, thereby, increasing the area, an oppositely directed current is induced which lasts as long as the area is changing.

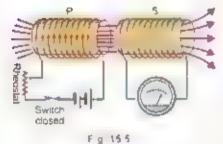


An induced current can also be generated when a coil of constant area is rotated in a constant magnetic field. Here, also, the magnetic flux through the coil changes (Fig. 15.4). This is the basic principle used in electric generators.

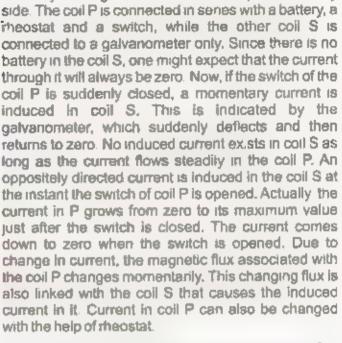
4 A very interesting method to induce current in a cod involves by producing a change of magnetic flux in





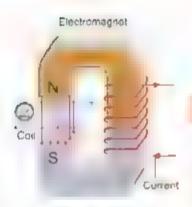


5.



a nearby coil. Fig. 15.5 shows two coils placed side by

It is also possible to link the changing magnetic flux with a coil by using an electromagnet instead of a permanent magnet. The coil is placed in the magnetic field of an electromagnet (Fig. 15.6). Both the coil and the electromagnet are stationary. The magnetic flux through the coil is changed by changing the current of the electromagnet, thus producing the induced current in the coil.



F p 156

#### 15.2 MOTIONAL EMF

In the previous section we have studied that when a conductor is moved across a magnetic field, an emf is induced between its ends. The emf of the moving conductor is similar to that of a battery, i.e. if the ends of the conductor are joined by a wire to make a closed circuit, a current flows through it.

The emf induced by the motion of a conductor across a magnetic field is called motional emf.

Consider a conducting rod of length I placed on two parallel metal rails separated by a distance I. A galvanometer is connected between the ends cland of the rails. This forms a complete conducting loop aboda (Fig. 15.7a). A uniform

magnetic field B is applied directed into the page. Initially when the rod is stationary, gaivanometer indicates no current n the loop. If the rod is pulled to the right with constant verocity v the galvanometer indicates a current flowing through the loop. Obvious yi the current is induced due to the motion of the conducting rod across the magnetic field. The moving rod is acting as a source of emf  $\varepsilon = V_1 - V_2 = \Delta V$ 

When the rod moves, a charge g within the rod also moves with the same velocity v in the magnetic field B and experiences a force given by

The magnitude of the force is

Since angle 6 between yand 8 is 90°, so

Applying the right hand rule, we see that F is directed from a to burn the rod. As a result the charge migrates to the top end. of the conductor. As more and more of the charges migrate. concentration of the charge is produced at the top b and deficiency of charges at the bottom a. This redistribution of charge sets up an electrostatic field. El directed from bito a. The electrostatic force on the charge is E = qE directed from b to a The system quickly reaches an equilibrium state in which these two forces on the charge, are balanced. If E is the electric intensity in this state then

The motions, emf  $\varepsilon$  will be equal to the potential difference  $\Delta V = V_s - V_s$  between the two ends of the moving conductor in this equilibrium state. The gradient of potential will be given by AVIL. As the electric intensity is given by the negative of the gradient therefore.

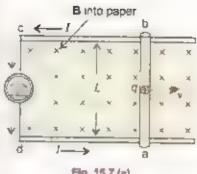


Fig. 15.7 (a)

$$\varepsilon = \Delta v = -LvB \qquad (15.3)$$

This is the magnitude of motional emf. However, if the angle between v and B is 9, then

$$\varepsilon = -\nu B L \sin \theta$$
 ....... (15.4)

Due to induced emf positive charges would flow along the path aboda, therefore the induced current is anticiockwise in the diagram. As the current flows the quantity of the charge at the top decreases so the electric intensity decreases but the magnetic force remains the same. Hence the equilibrium is disturbed in favour of magnetic force. Thus as the charges reach the end alof the conductor due to current flow they are carried to the top end bill of the conductor by the unbalanced magnetic field and the current continues to flow.





This heater operates on the principle of electromagne ic induction. The water in the metal pot is boiling whereas that in the glass pot is not Even the glass top of the heater is cook to fouch. The coil just beneath the top carries ac current that produces changing magnetic flux inking with pots and relief in them. Current is generated in the metal pot that heats up the water but no current flows through the glass pan why?

Example 15.1: A metal rod of length 25 cm is moving at a speed of 0.5 ms. In a direction perpendicular to a 0.25 T magnetic field. Find the emf produced in the rod.

#### Solution:

Speed of rod = v = 0.5 ms.' Length of rod = L = 25 cm = 0.25 m Magnetic flux density = B = 0.25 T = 0.25 NA.' m Induced emf =  $\epsilon = 7$ 

Using the relation,

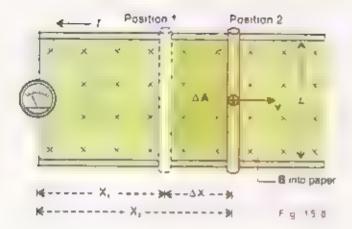
E=vBL

E = 05ms x 0 25NA m x 0 25m

ε=3 13x 10° JC '=3 13x 10° V

#### 15.3 FARADAY'S LAW AND INDUCED EMF

The motional emf induced in a rod moving perpendicular to a magnetic field is  $\varepsilon = -vBL$ . The motional emf as well as other induced emfs can be described in terms of magnetic flux. Consider the experiment shown in Fig. 15.8 again. Let the conducting rod L moves from position 1 to position 2 in a small interval of time  $\Delta t$ . The distance travelled by the rod in time  $\Delta t$  is  $x_2 - x_1 = \Delta x$ .



Since the rod is moving with constant velocity v, therefore

$$v = \frac{\Delta x}{\Delta t} \tag{15.5}$$

From Eq.15 3

$$\varepsilon = -vBL = -\frac{\Delta x}{\Delta t}BL \tag{15.6}$$

As the rod moves through the distance  $\Delta x$ , the increase in the area of loop is given by  $\Delta A = \Delta x.L$ . This increases the flux through the loop by  $\Delta \Phi = \Delta A.B = \Delta x.L.B$ . Putting  $\Delta x.L.B = \Delta \Phi$  in Eq. 15.6 we get

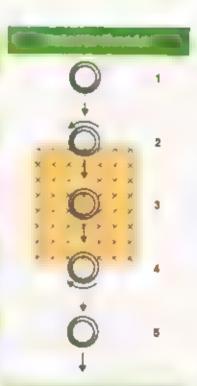
$$\varepsilon = \frac{\Delta \Phi}{\Delta t} \tag{15.7}$$

If there is a coil of N loops instead of a single loop, then the induced emf will become N times, i.e.,

$$\varepsilon = N \frac{\Delta \Phi}{\Delta t} \tag{15.8}$$

Although the above expression is derived on the basis of motional emf, but it is true in general. This conclusion was first arrived at by Faraday so this is known as Faraday's law of electromagnetic induction which states that

"The average emf induced in a conducting coil of N loops is equal to the negative of the rate at which the magnetic flux through the coil is changing with time".



A cooper ring passes through a rectangle region where a constant magnetic field is directed into the page What do you guess about the current in the ring at the positions 2-3 and 47.

The minus sign indicates that the direction of the induced emf is such that it opposes the change in flux.

Example 15.2. A loop of wire is placed in a uniform magnetic field that is perpendicular to the plane of the loop. The strength of the magnetic field is 0.6.T. The area of the

toop begins to shrink at a constant rate of  $\frac{\Delta A}{\Delta l} = 0.8 \text{ m/s}^{\circ}$ 

What is the magnitude of emf induced in the loop while it is shrinking?

#### Solution.

Rate of change of area = 
$$\frac{\Delta A}{\Delta t}$$
 = 0.8 m<sup>2</sup>s

Magnetic flux density = B = 0.6 T = 0.6 NA 'm'
Number of turns = N = 1
Induced emf - ε = ?

Rate of change of flux = 
$$\frac{\Delta \Phi}{\Delta t} = B \frac{\Delta A}{\Delta t} \cos 0^\circ = B \frac{\Delta A}{\Delta t}$$

Applying Faraday's Law magnitude of induced emf

$$\varepsilon = N \frac{\Delta t}{\Delta t} = NB \frac{\Delta A}{\Delta t}$$
  
= 1 x 0 6 NA'm x 0 8 m's'  
 $\varepsilon = 0.48 \text{ JC}' = 0.48 \text{ V}$ 

## 15.4 LENZ'S LAW AND DIRECTION OF INDUCED EMF

In the previous section, a mathematical expression of the Faraday's law of electromagnetic induction was derived as

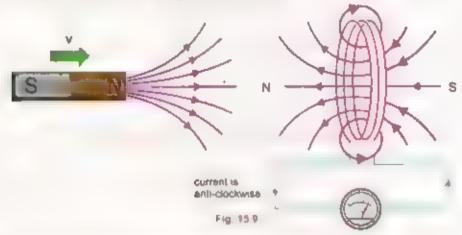
$$e = -N \frac{\Delta \Phi}{\Delta t}$$

The minus sign in the expression is very important. It has to do with the direction of the induced emf. To determine the direction we use a method based on the discovery made by the Russian Physicist Heinrich Lenz in 1834. He found that the polarity of an induced emf always leads to an induced current that opposes, through the magnetic field of the induced current, the change inducing the emf. The rule is known as Lenz's law which states that

"The direction of the induced current is always so as to oppose the change which causes the current"

The Lenz's law refers to induced currents and not to induced emf which means that we can apply it directly to closed conducting loops or colls. However, if the loop is not closed we can imagine as if it were closed, and then from the direction of induced current, we can find the direction of the induced emf.

Let us apply the Lenz's law to the coil in which current is induced by the movement of a bar magnet. We know that a current carrying coil produces a magnetic field similar to that of a bar magnet. One face of the coil acts as the north pole while the other one as the south pole. If the coil is to oppose the motion of the bar magnet, the face of the coil towards the magnet must become a north pole (Fig. 15.9). The two north poles will then repel each other. The right hand rule applied to



the coll suggests that the induced current must be anticlockwise as seen from the side of the bar magnet.

According to Lenz's law the "push' of the magnet is the "change" that produces the induced current, and the current acts to oppose the push. On the other hand if we pull the magnet away from the coil the induced current will oppose the "pull" by creating a south pole on the face of coil towards the bar magnet.

The Lenz's aw is also a statement of law of conservation of energy that can be conveniently applied to the circuits involving induced currents. To understand this consider once again the experiment in Fig. 15.8. When the rod moves towards right, emf is induced in it and an induced current flows through the loop in the anti-clockwise direction. Since the

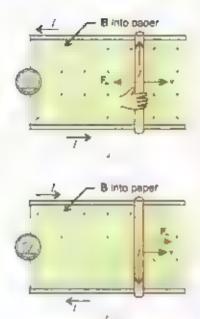


Fig. 15 10

current carrying rod is moving in the magnetic field, it expenences a magnetic force  $F_m$  having the magnitude  $F_m = ILB\sin 90^\circ$ . By right hand rule the direction of  $F_m$  is opposite to that of v, so it tends to stop the rod (Fig. 15.10 a). An external dragging force equal to  $F_m$  in magnitude but opposite in direction must be applied to keep the rod moving with constant velocity. This dragging force provides the energy for the induced current to flow. This energy is the source of induced current, thus electromagnetic induction is exactly according to law of conservation of energy.

The Lenz's law forbids the induced current directed clockwise in this case because the force F, would be then in the direction of v that would accelerate the rod towards right (Fig. 15.10 b). This in turn would induce a strongci current the magnetic field due to it also increases, that the magnetic force increases further. Thus the motion of the wire is accelerated more and more. Starting with a minute quantity of energy, we obtain an ever increasing kinetic energy of motion apparently from nowhere. Consequently, the process becomes self-perpetuating which is against the law of conservation of energy.

#### 15.5 MUTUAL INDUCTION

Consider two coils placed close to each other (Fig 15 11). One coil connected with a battery through a switch and a

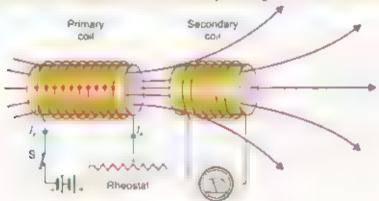


Fig. 18-11

rheostat is called the "phimary" and the other one connected to the galvanometer is called the "secondary" if the current in the primary is changed by varying the resistance of the rheostat, the magnetic flux in the surrounding region

changes. Since the secondary coil is in the magnetic field of the primary the changing flux also links with the secondary. This causes an induced emfinithe secondary.

The phenomenon in which a changing current in one coil induces an emf in another coil is called the mutual induction.

According to Faraday's law, the emf induced in the secondary coil is proportional to the rate of change of flux

$$\frac{\Delta \Phi_g}{\Delta t}$$
 passing through it, i.e.,  $\epsilon_n = -N_a \frac{\Delta \Phi_g}{\Delta t}$ 

where N, is the number of turns in the secondary coil.

Let the flux passing through one loop of the secondary coil be  $\Phi$ . Net flux passing through the coil of N, loops is N, $\Phi$ . As this flux is proportional to the magnetic field produced by the current  $I_p$  in the primary and the magnetic field itself is proportional to  $I_p$  therefore

$$N_s \Phi_s \propto I_s$$
  
 $N_s \Phi_s = MI_s$  . . . . (15.9)

Where  $M = \frac{N_{g} \Phi_{g}}{I_{p}}$  is proportionality constant called the

mutual inductance of the two coils. It depends upon the number of turns of the coils, their area of crossing section, their closeness together and the nature of the core material upon which the two coils are wound.

By Faraday's law the emf induced in the secondary coil is given by the rate of change of flux through the secondary.

$$\varepsilon_{x} = -N_{y} \frac{\Delta \Phi}{\Delta t} = -\frac{\Delta N_{y} \Phi}{\Delta t}$$

Putting N, $\phi_{\star} = M/$ , from Eq. 15.9

$$\varepsilon_{*} = \frac{\Delta \left(M I_{p}\right)}{\Delta l}$$

$$\varepsilon_{*} = -M \frac{\Delta I_{p}}{\Delta l} \tag{15.10}$$

The Eq 15 10 shows that the emf induced in the secondary is proportional to the time rate of change of current in the primary.

The negative sign in Eq.15.10 indicates the fact that the induced emf is in such a direction that it opposes the change of current in the primary co. While finding out the value of M from Eq.15.10, negative sign is ignored. Thus M may be defined as the ratio of average emf induced in the secondary to the time rate of change of current in the primary.

$$M = \frac{\epsilon_s}{\Delta I_p}$$

The SI unit for the mutual inductance M is Vs A1, which is called as henry (H) after Joseph Henry.

One henry is the mutual inductance of the pair of coils in which the rate of change of current of one ampere per second in the primary causes an induced emf of one volt in the secondary.

**Example 15.3:** An emf of 5.6 V is induced in a cor while the current in a nearby coil is decreased from 100 A to 20 A in 0.02 s. What is the mutual inductance of the two coils? If the secondary has 200 turns find the change in flux during this interval.

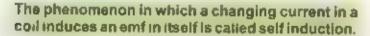
#### Solution:

emf induced in the secondary =  $\varepsilon_* = 5.6 \text{ V}$ Change in current in primary =  $\Delta I_* = 100 \text{ A} - 20 \text{ A} = 80 \text{ A}$ Time interval for the change =  $\Delta I_* = 0.02 \text{ s}$ Mutual inductance =  $M_* = 2$ No. of turns in the secondary =  $N_* = 200$ Change in flux =  $\Delta \Phi = 7$ Using  $\varepsilon_* = \frac{\Delta I_*}{\Delta I_*} M$   $5.8 \text{ V} = M \times \frac{80 \text{ A}}{0.02 \text{ s}}$   $M = \frac{5.6 \text{ V} \times 0.02 \text{ s}}{80 \text{ A}} = 1.4 \times 10^3 \text{ VsA}^3$ By Fareday's Lew  $\varepsilon_* = N_* = \frac{\Delta \Phi_*}{\Delta I_*}$  $\Delta \Phi_* = \frac{\varepsilon_* \Delta I_*}{N_*} = \frac{5.6 \text{ V} \times 0.02 \text{ s}}{200} = 5.6 \times 10^4 \text{ Wb}$ 

#### 15.6 SELF INDUCTION

According to Faraday's law, the change of flux through a coll by any means induces an emfinit. In all the examples we have discussed so far induced emf was produced by a changing magnetic flux from some external source. But the change of flux through a coll may also be due to a change of current in the coll itself.

Consider the circuit shown in Fig. 15.12. A coil is connected in series with a battery and a rheostat. Magnetic flux is produced through the coil due to current in it. If the current is changed by varying the rheostat quickly, magnetic flux through the coil changes that causes an induced emf in the coil. Such an emf is called as self-induced emf.



If the flux through one loop of the coil be  $\Phi$ , then the total flux through the coil of N turns would be N  $\Phi$ . As  $\Phi$  is proportional to the magnetic field which is in turn proportional to the current / therefore

$$N Φ ∝ I$$
 or  $N Φ = U$  ....... (15.11)

where  $L = \frac{N\Phi}{I}$  is the constant of proportionality called the self

inductance of the coil it depends upon the number of turns of the coil, its area of cross-section and the core material. By winding the coil around a ferromagnetic (iron) core, the magnetic flux and hence the inductance can be increased significantly relative to that for an air core.

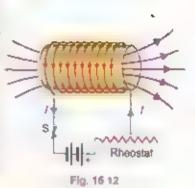
By Faraday's Law, emfinduced in the coil is

$$\varepsilon_{\rm c} = -N \frac{\Delta \Phi}{\Delta t}$$

$$\varepsilon_{\rm c} = -\frac{\Delta (N\Phi)}{\Delta t}$$

Putting NΦ = L/ from Eq 15.11

$$\varepsilon_{\rm L} = \frac{\Delta(LI)}{M}$$
 or 
$$\varepsilon_{\rm L} = -L \frac{M}{\Delta I}$$
 (15.12)



The Eq 15 12 shows that the self-induced emf in a coit is proportional to the time rate of change of current in the coil. Self-inductance L of a coil may be defined as the ratio of the emf to the rate of change of current in the coil. The unit of L is also benry (H).

The negative sign in Eq 15.12 indicates that the self induced emf must oppose the change that produced it. That is why the self induced emf is sometimes called as back emf. This is exactly in accord with the Lenz's law. If the current is increased, the induced emf will be opposite to that of battery and if the current is decreased the induced emf will aid, rather than opposing the battery. Because of their self inductance coils of wire are known as inductors, and are widely used in electronics in alternating current, inductors behave like resistors.

Example 15.4: The current in a coil of 1000 turns is changed from 5 A to zero in 0.2 s. If an average emf of 50 V is induced during this interval what is the self inductance of the coil? What is the flux through each turn of the coil when a current of 6 A is flowing?

#### Solution:

Change in current = \( \Delta / \cdot 5A \cdot 0 = 5A \)

Time interval  $=\Delta t = 0.2s$ 

emfinduced = E = 50 V

Self induction =L=?Steady current =I=6A

No of turns of coil = N= 1000

Flux through each turn =  $\Phi$  = ?

Using

$$L = \frac{\varepsilon}{\Delta I_{\Delta f}} = \frac{50 \text{ V}}{5 \text{ A}} = \frac{50 \text{ V}}{5 \text{ A}} = \frac{50 \text{ V}}{0.2 \text{ s}}$$

Now using Eq 15 11

$$N\Phi = LI$$
 or  $\Phi = \frac{LI}{N}$ 

$$\Phi = \frac{2 \text{H} \times 6 \text{ A}}{1000} = 1.2 \times 10^{2} \text{Wb}$$

#### 15.7 ENERGY STORED IN AN INDUCTOR

We have studied in chapter 12 that energy can be stored in the electric field between the plates of a capacitor in a similar manner lenergy can be stored in the magnetic field of an inductor.

Consider a coil connected to a battery and a switch in senes (Fig. 15.13). When the switch is turned on voltage V is applied across the ends of the coil and current through it rises from zero to its max mum value /. Due to change of current, an emf. is induced, which is opposite to that of battery. Work is done by the battery to move charges against the induced emf.

Work done by the battery in moving a small charge Aq is

$$W = \Delta q \, \varepsilon_{\rm L} \tag{15.13}$$

where  $\varepsilon_{c}$  is the magnitude of induced emf, given by

$$\varepsilon_{\rm L} = L \frac{\Delta I}{\Delta I}$$

Putting the value of s, in Eq.15.13 we get

$$W = \Delta q L \frac{\Delta l}{\Delta t} - \frac{\Delta q}{\Delta t} L \Delta l \qquad (15.14)$$

Total work done in establishing the current from 0 to / is found by inserting for  $\frac{\Delta q}{\Delta t}$  the average current, and the value of  $\Delta t$ 

Average current = 
$$\frac{\Delta q}{\Delta f} = \frac{0 \cdot 1}{2} \frac{1}{2}$$

Change in current =  $\Delta I = I - 0 = I$ 

Total work

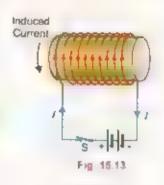
$$W = \left(\frac{1}{2}I\right)LI$$

$$W = \frac{1}{2} \coprod$$

This work is stored as potential energy in the inductor. Hence the energy stored in an inductor is

$$U_{m} = \frac{1}{2} L I^{2}$$
 (15.15)

As in case of a capacitor, energy is stored in the electric field between the plates it kewise in an inductor energy is stored in the magnetic field. Therefore, Eq. 15.15 can be expressed in terms of the magnetic field B of a solenoid which has n turns per unit length and area of cross section A. The magnetic field strength inside it is  $B = \mu_e n l$ . Since flux through the coil is



$$\Phi = BA$$

or

Substituting the value of \$\Phi\$ in Eq 15.11

$$N\Phi - LI$$
 or  $L = \frac{N\Phi}{I}$ 

we have

$$L = N \frac{\mu n I A}{T} = N \mu n A$$

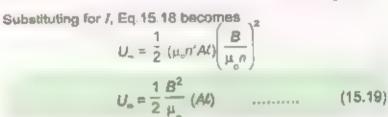
If t is the length of solenoid, then putting N = nt in above Eq. we get the self-inductance of the solenoid as

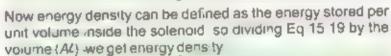
$$L = \mu_c n^2 A \ell \qquad (15.17)$$

Substituting for L, the Eq.15.15 becomes,

$$U_{\rm m} = \frac{1}{2} (\mu_{\rm o} n^2 A t) T^2$$
 (15.18)

Since 8 for a solenoid is given by  $B = \mu_e nI$  or  $I = \frac{1}{\mu_e n}$ 





$$u_{\mu} = \frac{1}{2} \frac{B^2}{\mu}$$
 (15.20)

**Example 15.5:** A solenoid coil 10.0 cm long has 40 turns per cm. When the switch is closed, the current rises from zero to its maximum value of 5.0 A in 0.01 s. Find the energy stored in the magnetic field if the area of cross-section of the solenoid be 28 cm<sup>2</sup>.

#### Solution:

An induction ammeter with its ironcore aw a open and it dissed around a wire carrying an atternating currior, some of the magnetic field

lings that encircle the wire are routed through the cuil by the man lord and

lead to an induced emf. The reter

directs the emf and is calibrated to display the amount of current in the

Length of sciencid = t = 10.0 cm = 0.1 m

No of turns = n - 40 per cm - 4000 per m

Area of cross section  $= A = 28 \text{ cm}^2 = 2.8 \times 10^2 \text{ m}^2$ Steady current = I = 5 AEnergy Stored  $= U_m = 7$ 

First, we calculate the inductance L using the Eq. (15.17)  $L = \mu_c n^2 AL$ 

= 
$$(4\pi \times 10^{-7})$$
 WbA  $^{1}$ m  $^{1} \times (4000 \text{ m}^{-1})^{2} \times 2.8 \times 10^{-3} \text{ m}^{2} \times 0.1 \text{ m}$ 

= 
$$(4\pi \times 10^{-4})$$
 WbA 'm 'x  $(4000 \text{ m}^{-4})^4 \times 2.8 \times 10^{-3} \text{ m}^4 \times 0.1 \text{ m}$   
=  $5.63 \times 10^{-3}$  WbA  $^4 = 5.63 \times 10^{-3}$  H

Energy stored= 
$$U_{=}=\frac{1}{2} L I = \frac{1}{2} (5.63 \times 10^{-3} \text{NmA}^{-2}) \times (5 \text{ A})^{2}$$

$$\approx 7.04 \times 10^{-2} \text{Nm} = 7.04 \times 10^{-2} \text{ J}$$

#### 15.8 ALTERNATING CURRENT GENERATOR

We have learnt that when a current carrying coil is placed in a magnetic field, a torque acts on it that rotates the coil. What happens if a coil of wire is rotated in a magnetic field? Can a current be produced in the coil? Yes lit does. Such a device is called a current generator.

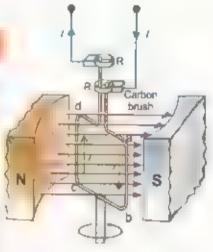
## A current generator is a device that converts mechanical energy into electrical energy.

The principle of an electric generator is based on Faraday's law of electromagnetic induction. When a coil is rotated in a magnetic field by some mechanical means, magnetic flux through the coil changes, and consequently an emf is induced in the coil.

If the generator is connected to an external circuit, an electric current is the output of the generator.

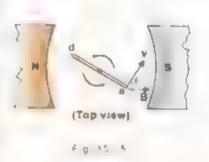
Let a rectangular loop of wire of area A be placed in a uniform magnetic field **B** (Fig 15.14). The loop is rotated about z-axis through its centre at constant angular velocity of One end of the loop is attached to a metal ring R and the other end to the ring R. These rings called the stip rings are concentric with the axis of the loop and rotate with it Rings R.R. slide against stationary carbon brushes, to which external circuit is connected.

To calculate the induced emf in the loop, consider its position (Fig 15.15) while it is rotating anticlockwise. The figure shows the top view of the coil. The vertical side ab of the loop is moving with velocity  ${\bf v}$  in the magnetic field  ${\bf B}$ . If the angle between  ${\bf v}$  and  ${\bf B}$  be  $\theta$ , the motional emf induced in the side ab has the magnitude,



FIB 15 14

(Front view)



The direction of induced current in the wire ab is the same as that of force F expenenced by the charges in the wire i.e., from top to the bottom. The same amount of emf. s. induced in the side od but the direction of current is from bottom to the top.

The net contribution to emf by sides be and da is zero because the force acting on the charges inside be and da is not along the wire.

Since both the emfs in the sides ab and cd drive current in the same direction around the loop, the total emf in the loop is

$$\mathbf{E} = \mathbf{E}_{10} + \mathbf{E}_{20}$$

$$\varepsilon = vBL \sin\theta + vBL \sin\theta$$

$$\varepsilon = 2vBL \sin\theta$$

If the toop is replaced by a coil of N turns, the total emf in the coil will be,

$$\varepsilon = 2 NvBL \sin \theta$$

(15.21)

The linear speed viol the vertical wire is related to the angular speed  $\omega$  by the relation

$$V = 608$$

where ris the distance of the vertical wires from the centre of the coil. Substituting or for vin Eq. (15.21)

Weget

$$\varepsilon = 2 N(\omega r) BL \sin \theta$$

$$\varepsilon = N_{co}AB\sin\theta$$
 ...... (15.22)

where A = 2 rL = area of the coil

As the angular displacement 8 = of so the Eq. 15.22 becomes

(15.23)

Eq. 15.23 shows that the induced emf varies sinusoidally with time.

It has the maximum value a when sin (oit) is equal to 1. Thus

The Eq 15.23 can be written as,

$$\varepsilon = \varepsilon_a \sin(\omega t)$$
 .... (15.25)

If R is the resistance of the coil, then by Ohm's law, induced current in the coil will be

$$I = \frac{\varepsilon}{R} = \frac{\varepsilon_0 \sin(\omega t)}{R} = \frac{\varepsilon_0}{R} \sin(\omega t)$$

$$I = I_0 \sin(\omega t) \qquad (15.26)$$

where I, is maximum current.

or

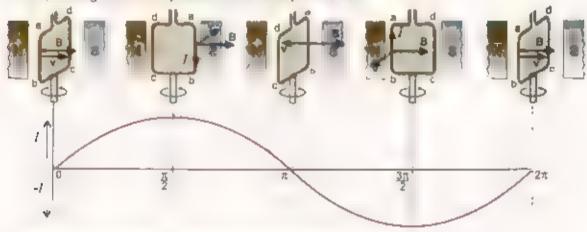
Angular speed  $\omega$  of the con is related to its frequency of rotation f as,  $\omega = 2\pi f$ 

The Eqs. 15.25 and 15.26 can be written as

$$E = E_o S \cdot \Pi(2\tau f t)$$
 (15.27)

$$I = I_a \sin(2\pi f t)$$
 (15.28)

Eq 15.28 indicates the variation of current as a function of  $\theta = 2\pi ft$ . Fig. 15.16 shows the graph for the current corresponding to different positions of one loop of the coil



When the angle between  $\mathbf{v} \cdot \mathbf{\hat{a}} \cdot \mathbf{B}$  is  $\theta = 0^\circ$  the plane of the loop is perpendicular to  $\mathbf{B}$  current is zero. As  $\theta$  increases current also increases and at  $\theta = 90^\circ = \pi/2$  rad, the loop is parallel to  $\mathbf{B}$ , current is maximum, directed along aboda. On further increase in  $\theta$  current decreases, and at  $\theta = 180^\circ = \pi$  rad the current becomes zero as the loop is again perpendicular to  $\mathbf{B}$ . For  $180^\circ < \theta < 270^\circ$  current increases, but reverses its direction as is clear from the figure. Current is now directed.

along debad. At  $\theta = 270^{\circ} = 3 \pi/2$  rad, current is maximum in

Fig. 15.16



Fig. 4 sy Temperor campers or y to when he was the opposite y the constitution of the

the reverse direction as the loop is parallel to **B** At  $\theta = 360^\circ = 2\pi$  rad, one rotation is completed, the loop is perpendicular to **B** and the current decreases to zero. After one rotation the cycle repeats itself. The current alternates in direction once in one cycle. Therefore, such a current is called the alternating current. It reverses its direction f times per second.

In actual practice a number of coils are wound around an iron cylinder which is rolated in the magnetic field. This assembly is called an armature. The magnetic field is usually provided by an electromagnet. Armature is rotated by a fuellengine or a turbine run by a waterfall. In some commercial generators, field magnet is rotated around a stationary armature.

Example 15.6: An alternating current generator operating at 50 Hz has a coil of 200 turns. The coil has an area of 120 cm<sup>2</sup>. What should be the magnetic field in which the coil rotates in order to produce an emf of maximum value of 240 volts?

#### Solution:

Frequency of rotation = f = 50 Hz

No of turns of the coil = N = 200

Area of the coil =  $A = 120 \text{ cm}^2 = 1.2 \times 10^4 \text{ m}^2$ 

Maximum emf = c\_ = 240 V

Magnetic flux density = B - ?

First, we shall find the angular speed or

Using

$$\omega = 2\pi f$$
  
 $\omega = 2 \times \frac{22}{7} \times 50 = 314.3 \text{ rad s}^{-1}$ 

Using & = No AB or

$$B = \frac{v_o}{N \omega A}$$

$$B = \frac{240 \text{ V}}{200 \times 314 \text{ 3 rad s}^{-1} \times 1.2 \times 10^{-2} \text{m}^2}$$

B=0 32 Vs rad 'm2=0 32 T

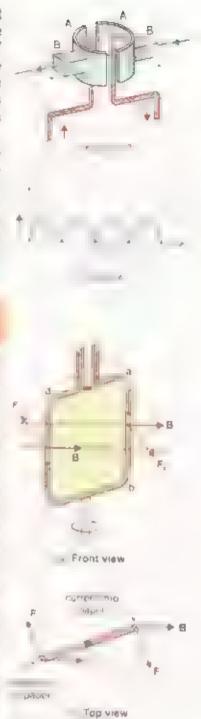
#### 15.9 D.C. GENERATOR

Atternating current generators are not suitable for many applications, for example, to run a D.C. Motor in 1834 William Sturgeon invented a simple device called a commutator that prevents the direction of current from

changing. Therefore a D.C. generator is similar to the A.C. generator in construction with the difference that "s ip nings" are replaced by "spot rings". The "sp. tinings" are two halves of a ring that act as a commutator. Fig. 15.17 shows the "sput rings" A and A attached to the two ends of the cor that rotates in the magnetic field. When the current in the coil is zero and is about to change direction, the split rings also change the contacts with the carbon brushes BB in this way the output from BB' remains in the same direction. a though the current is not constant in magnitude. The curve of the current is shown in Fig. 15-18. It is similar to a sine curve. with the lower half inverted. The fluctuations of the output can be significantly reduced by using many coils rather than a single one. Multiple corls are wound around a cylindrical core. to form the armature. Each coil is connected to a separate commutator and the output of every coil is tapped only as it reaches its peak emf. Thus the emf in the outer circuit is almost constant

## 15.10 BACK MOTOR EFFECT IN GENERATORS

Agenerator is the source of electricity production. Practically the generators are not so simple as described above. A large turbine is turned by high pressure steam or waterfal. The ahaft of the turbine is attached to the coil which rotates in a magnetic field. It converts the mechanica energy of the driven turbine to electrical energy. The generator supplies current to the external circuit. The devices in the circuit that consume electrical energy are known as the "load". The greater the lad the larger the current is supplied by the generator. When the circuit is open, the generator does not supply electrical energy and a very little force is needed to rotate the coil. As soon as the circuit is closed, a current is drawn through the coil. The magnetic lie diexerts force on the current carrying coil Fig. 15.19 shows the forces acting on the coil. Force F, is acting on the left side of the coil whereas. an equal but opposite force F, acts on the right side of the coal These forces are such that they prodice a counter torgue that opposes the rotational motion of the corr. This effect is sometimes referred to as pack motor effer in the generators The arger the current drawn the greater sith a content of the produced. That means more mechanical energy is required. to keep the coll rotating with constant angular speed. This is n agreement with the law of conservation of energy. The



energy consumed by the "load" must come from the "energy source" used to drive the turbine

#### 15.11 D.C. MOTOR

A motor is a device which converts electrical energy into mechanica energy. We already know that a wire carrying current placed in a magnetic field experiences a force. This is the basic principle of an electric motor. In construction a D C motor is similar to a D C generator, having a magnetic field a commutator and an armature in the generator, the armature is rotated in the magnetic field and current is the output in the D C motor current passes through the armature that rotates in the magnetic field, in the D C motor, the brushes are connected to a D C supply or battery (Fig. 15.20). When current flows through the armature con the force on the conductors produces a torque, that rotates the armature. The amount of this forque depends upon the current, the strength of the magnetic field, the area of the coil and the number of turns of the coil.

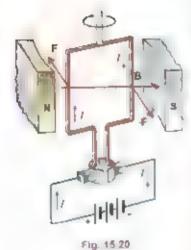
If the current in the coil were all the time in the same direction, the torque on it would be reversed after each half revolution. But at this moment commutator reverses the direction of current that keeps the torque a ways in the same sense. A little problem anses due to the use of commutator that is the torque vanishes each time the current changes its direction. This creates jerks in the smooth running of the armsture. However the problem is overcome by using more than one coil wrapped around a soft-ron core. This results in producing a more steady torque.

The magnetic field in the motor is provided by a permanent magnet or an electromagnet. The windings of the electromagnet are usually called the field coils. The field coils may be in series or in parallel to the armature coils.

### 15.12 BACK EMF EFFECT IN MOTORS

A motor is just like a generator running in reverse. When the coil of the motor rotates across the magnetic field by the applied potential difference V an emficis induced in it. The induced emfi is in such a direction that opposes the emfiruning the motor. Due to this reason the induced emf is called back emf of the motor. The magnitude of the back emfininglesses with the speed of motor.

Since V and  $\varepsilon$  are opposite in polarity, the net emf in the circuit is  $V - \varepsilon$ . If R is the resistance of the coil and I the current drawn



by the motor, then by Ohm's law

$$I = \frac{V - \varepsilon}{R}$$
 or  $V - \varepsilon + IR$  (15.29)

When the motor is just started, back emf is almost zero and hence a large current passes through the coil. As the motor speeds up, the back emf increases and the current becomes smaller and smaller. However, the current is sufficient to provide torque on the coil to drive the load and to overcome losses due to friction. If the motor is overloaded, it slows down. Consequently, the back emf decreases and allows the motor to draw more current. If the motor is overloaded beyond its limits, the current could be so high that it may burn out the motor.

Example 15.7: A permanent magnet D C motor is run by a battery of 24 volts. The coil of the motor has a resistance of 2 ohms. It develops a back emf of 22.5 volts when driving the load at normal speed. What is the current when motor just starts up? Also find the current when motor is running at normal speed.

#### Solution:

Operation Voltage = V=24 V

Resistance of the co 1 = R = 2 $\Omega$ Back emf =  $\varepsilon$  = 22.5 V

Current = I = ?

i) when motor just starts up, the back emf  $\varepsilon$  = 0

Using  $V = \varepsilon + IR$   $24V = 0 + I \times 2\Omega$   $I = \frac{24 \text{ V}}{2\Omega} = 12 \text{ V}\Omega = 12 \text{ A}$ when motor runs at normal speed,  $\varepsilon$  = 22.5 V
then using  $V = \varepsilon + IR$   $V = 22.5 \text{ V} + I \times 2\Omega$   $I = \frac{24 \text{ V}}{2\Omega} = 0.75 \text{ V}\Omega^{-1} = 0.75 \text{ A}$ 

#### 15.13 TRANSFORMER

A transformer is an electrical device used to change a given alternating emf into a larger or smaller alternating emf. It works on the principle of mutual induction between two coils

In principle, the transformer consists of two coils of copper, electrically insulated from each other, wound on the same ron core. The coil to which A.C. power is supplied is called primary and that from which power is delivered to the circuit is called the secondary.

It should be noted that there is no electrical connection between the two coils but they are magnetically linked. Suppose that an alternating emf is applied to the primary of at some instant (the flux in the primary is changing at the rate of  $\Delta\Phi/\Delta t$  then there will be back emf induced in the primary which will oppose the applied voltage. The instantaneous value of the self induced emf is given by

Self-induced emf = 
$$-N_p \left[ \frac{\Delta \Phi}{\Delta t} \right]$$

If the resistance of the cours negligible then the backlemf is equal and opposite to applied voltage V<sub>o</sub>

$$V_{\mu}$$
 backlemf  $N_{\mu} \stackrel{1\Phi}{\simeq} \Omega$  (15.30)

where N, is the number of turns in the primary.

Assuming the flux through the primary also passes through the secondary i.e., the two coils are tightly coupled the rate of change of flux in the secondary will also be 140.1f and the magnitude of the induced emf across the secondary is given by

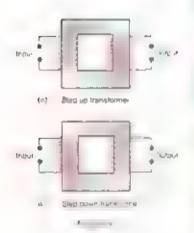
$$V = N_{\nu} \frac{\Delta \Phi}{\Delta t}$$
 (15.31)

where N<sub>c</sub> is the number of turns in the secondary

Dividing Eq. 15.31 by Eq. 15.30, we get

$$V_{\nu} = N_{\nu}$$
 (15.32)

If  $N_i \ge N_s$ , then according to Eq. 15.32,  $V_s \ge V_p$ , such a transformer in which voltage across secondary is greater than the primary voltage is cared a step up transformer (Fig. 15.20 a). Similarly if  $N_s \le N_p$ , i.e., the number of turns in the secondary is less than the number in primary, then  $V_s \le V_p$ , such transformer in which voltage across secondary is less than the primary voltage is called a step down transformer (Fig. 15.20 b)



It is important to note that the electrical power in a transformer is transformed from its primary to the secondary coil by means of changing flux. For an ideal case the power input to the primary is nearly equal to the power output from the secondary i.e.,

Power input = Power output

or 
$$\frac{V_c I - V_s I_c}{V_0 - I_s}$$
 (15.33)

In is the current in the primary and I, in the secondary. The currents are thus inversely proportional to the respective voltages. Therefore, in a step up transformer when the voltage across the secondary is raised, the value of current is reduced. This is the principle behind its use in the electric supply network where transformer increases the voltage and reduces the current so that it can be transmitted over long. distances without much power loss. When current / passes. through a resistance R the power loss due to heating effect is I'R Suppose R is the resistance of transmission, me. In order to min mize the loss during transmission, it is not possible to reduce R because it requires the use of thick copper wire which becomes highly uneconomical. The purpose is wellserved by reducing / At the generating power station the voltage is stepped up to several thousand of voits and power is transmitted at low current to long distances without much loss. Step down transformers then decrease the voltage to a safe value at the end of line where the consumer of electric power is located. Inside a house a transformer may be used. to step down the voltage from 250 voits to 9 voits for ringing. belior operating a transistor radio. Transformers with several secondaries are used in television and radio receivers where several different voltages are required.

On yin an idea; transformer the output power is nearly equato the input power. But in an actual transformer, this in not the case. The output is always less than input due to power losses. There are two main causes of power loss, namelyeddy currents and magnetic hysteresis.

In order to enhance the magnetic flux, the primary and secondary coils of the transformer are wound on soft iron core. The flux generated by the coils also passes through the core. As magnetic flux changes through a solid conductor induced currents are set up in closed paths in the body of the



Transformer symbol

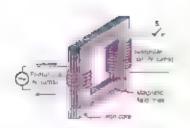


Fig. 15.21

conductor. These induced currents are set up in a direction perpendicular to the flux and are known as eddy currents. It results in power dissipation and heating of the core material In order to minimize the power loss due to flow of these currents, the core is laminated with insulation in between the tayers of laminations which stops the flow of addy currents (Fig. 15.21) Hystenses loss is the energy expended to magnetize and demagnetize the core material in each cycle of the A.C.

Due to these power losses, a transformer is far from being an idea: its output power sla ways essithan its input power. The efficiency of a transformer is defined as

In order to improve the efficiency care should be exercised, to minimize all the power losses. For example core should be assembled from the laminated sheets of a material whose hysteresis loop area is very smal. The insulation between lamination sheets should be perfect so as to stop the flow of eddy currents. The resistance of the primary and secondary coils should be kept to a minimum. As power transfer from primary to secondary takes place through flux linkages, so the primary and secondary coils should be wound in such a way that flux coupling between them is maximum.

Example 15.8: The turns ratios of a step up transformer 6 50 A current of 20 A is passed through its primary coil at 220 volts. Obtain the value of the voltage and current in the secondary con assuming the transformer to be ideatione

Solution:

Using the equation 
$$\frac{V_s}{V_p} = 50$$
  $I_s = 20 \text{ A}$   $I_s = 20 \text{ A}$ 

Voltage in the secondary co I = V, = 220 x 50 = 1100 volts

$$I_{\rm s} = \frac{V_{\rm p}}{V_{\rm s}} \times I_{\rm p} = \frac{1}{50} \times 20 = 0.4 \,\mathrm{A}$$



- An emf is set up in a conductor when it moves across a magnetic field. It is called an
  induced emf.
- The emf induced by the motion of a conductor across a magnetic field is called motional emf.
- Magnitude of imptional emf in a rod of length L moving with velocity v across a magnetic field of strength 8 making θ with it is ε = v8Lsin θ
- Faraday's law states that the emf induced in a conducting coil of Niloops is equal to the negative of the rate at which the magnetic flux through the coil is changing with time
- The Lenz's law states that the direction of the induced current is always so as to oppose the change which causes the current
- The phenomenon in which a changing current in one coil induces an emf in another coil is called the mutual induction.
- One heary is the mutual inductance of that pair of coils in which a change of current
  of one ampere per second in the primary causes an induced emf of one volt in the
  secondary
- The phenomenon in which a changing current in a coil induces an emf in itself is called self-induction.
- A current generator is a device that converts mechanical energy into electrical energy.
- The emf produced in a generator is  $\varepsilon = N \cap AB \sin(\omega t)$  or  $\varepsilon = \varepsilon_1 \sin(2\pi f t)$
- Amotor is a device, which converts electrical energy into mechanical energy.
- The induced emf in a motor opposes the emf running the motor. This induced emf is called the back emf of the motor.

#### **QUESTIONS**

- 15.1 Does the induced emf in a circuit depend on the resistance of the circuit? Does the induced current depend on the resistance of the circuit?
- A square loop of wire is moving through a uniform magnetic field. The normal to the loop is oriented parallel to the magnetic field. Is a emf induced in the loop? Give a reason for your answer.
- 15.3 Alight metallic ring is released from above into a vertical bar magnet (Fig. Q. 15.3). Viewed for above, does the current flow clockwise or anticlockwise in the ring?



What is the direction of the current through resistor R in Fig Q 15 4? When switch S is (a) closed (b) opened.

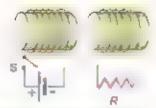


Fig. Q. 15.4

- 15.5 Does the induced emf always act to decrease the magnetic flux through a circuit?
- When the switch in the circuit is closed a current is established in the coil and the metaliring jumps upward (Fig Q.15.6). Why?

  Describe what would happen to the ring if the battery polarity were reversed?

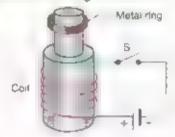


Fig. Q. 15.6

15.7 The Fig Q. 15.7 shows a coil of wire in the xy plane with a magnetic field directed along the y - axis. Around which of the three coord nate axes should the coil be rotated in order to generate an emf and a current in the coil?

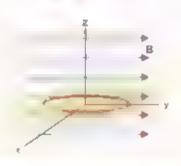


Fig. Q. 15.7

- 15.8 How would you position a flat loop of wire in a changing magnetic field so that there is no emfinduced in the loop?
- n a certain region the earth's magnetic field point vertically down. When a plane flies due north, which wingto is positively charged?
- 15.10 Show that  $\epsilon$  and  $\frac{\Delta \Phi}{\Delta t}$  have the same units.
- When an electric motor such as an electric drill is being used does it also act as a generator? If so what is the consequence of this?
- 15 12 Can a D C motor be turned into a D C generator? What changes are required to be done?
- 15.13 is it possible to change both the area of the roop and the magnetic field passing through the loop and stall not have an induced emf in the loop?
- 15.1.1 Can an electric motor be used to drive an electric generator with the output from the generator being used to operate the motor?
- 15 A suspended magnet is oscillating freely in a horizontal piane. The oscillations are strongly damped when a metal plate is placed under the magnet. Explain why this occurs?

- 15.16 Four unmarked wires emerge from a transformer. What steps would you take to determine the turns ratio?
- 15 17 a) Can a step-up transformer increase the power level?
  - b, In a transformer, there is no transfer of charge from the primary to the secondary. How is, then the power transferred?
- 15.18 When the primary of a transformer is connected to a cimains the current in it
  - a) Is very small if the secondary circuit is open, but
  - increases when the secondary circuit is closed. Explain these facts.

### PROBLEMS

- An emf of 0.45 V is induced between the ends of a metal bar moving through a magnetic field of 0.22 T. What field strength would be needed to produce an emf of 1.5 V between the ends of the bar lassuming that all other factors remain the same?

  (Ans: 0.73 T)
- The flux density B in a region between the pole faces of a horse-shoe magnet is 0.5 Wbm<sup>-1</sup> directed vertically downward. Find the emf induced in a straight wire 5.0 cm long perpendicular to B when it is moved in a direction at an angle of 60° with the horizontal with a speed of 100 cms. (Ans: 1.25 x 10 V)
- A coil of wire has 10 loops. Each loop has an area of 1.5 x 10 °m. A magnetic field is perpendicular to the surface of each loop at all times. If the magnetic field is changed from 0.05 T to 0.06 T in 0.1 s. find the average emfinduced in the co.l during this time.

  (Ans: +1.5 x 10 °V)
- A circular coil has 15 turns of radius 2 cm each. The plane of the coil lies at 40° to a uniform magnetic field of 0.2 T. If the field is increased by 0.5 T in 0.2 s. find the magnitude of the induced emf.

  (Ans: 1.8 x 10°V)
- 15.5 Two cors are placed side by side. An emf of 0.8 V is observed in one coil when the current is changing at the rate of 200 As in the other coil. What is the mutual inductance of the coils? (Ans: 4 mH)
- A pair of adjacent cors has a mutual inductance of 0.75 H. If the current in the primary changes from 0 to 10 A in 0.025 s, what is the average induced emf in the secondary? What is the change in flux in it if the secondary has 500 turns?
  (Ana: 300 V. 1.5 x 10° Wb)
- A solenoid has 250 turns and its self-inductance is 2.4 mH. What is the flux through each turn when the current is 2.A? What is the induced emf when the current changes at 20As.?

  (Ans: 1.92 x 10. Wb. 48 mV)
  - Aso enoid of length 8.0 cm and cross sectional area 0.5 cm² has 520 turns. Find the self-inductance of the solenoid when the core is air. If the current in the solenoid increases through 1.5 Air 0.2 s, find the magnitude of induced emf in t. (μ<sub>0</sub>=4π x 10<sup>3</sup> WbA²m²) (Ans: 1.6 x 10<sup>3</sup> V , 2.12 x 10<sup>4</sup> H)

- When current through a coil changes from 100 mA to 200 mA in 0 005 s, an induced emf of 40 mV is produced in the coil (a) What is the self-inductance of the coil?

  (b) Find the increase in the energy stored in the coil (Ans. 2 mH, 0 03 mJ)
- 15.10 Like any field, the earth's magnetic field stores energy. Find the magnetic energy stored in a space where strength of earth's field is 7 x 10 ° T, if the space occupies an area of 10 x 10° m² and has a height of 750 m. (Ans. 1.46 x 10° J)
- 15.11 A square coil of side 16 cm has 200 turns and rotates in a uniform magnetic field of magnitude 0.05 T If the peak emf is 12 V, what is the angular velocity of the coil (Ans: 47 rad s.)
- 15.12 A generator has a rectangular coil consisting of 360 turns. The coil rotates at 420 reviper min in 0.14 T magnetic field. The peak value of emf produced by the generator is 50 V if the coil s.5.0 cm wide, find the length of the side of the coil.

  (Ans: 45 cm)
- 15.13 It is desired to make an aic generator that can produce an emf of maximum value 5kV with 50 Hz frequency. A coil of area 1 milhaving 200 turns is used as armature. What should be the magnitude of the magnetic field in which the coil rotates?

  (Ans: 0.08 T)
- 15 14 The backlemfin a motor is 120 V when the motor is turning at 1680 reviper min. What is the backlemf when the motor turns 3360 reviper min? (Ans. 240 V)
- 15 15 AD C motor operates at 240 V and has a resistance of 0.5 Ω. When the motor is running at normal speed, the armature current is 15 A. Find the back emf in the armature.

  (Ans: 232.5V)
- 15 16 A copper ring has a radius of 4.0 cm and resistance of 1.0 mΩ. A magnetic field is applied over the ring, perpendicular to its plane. If the magnetic field increases from 0.2 T to 0.4 T in a time interval of 5 x 10. s, what is the current in the ring during this interval?

  (Ans: 201 A)
- 15 17 A coil of 10 turns and 35 cm area is in a perpendicular magnetic field of 0.5 T. The coil is pulled out of the field in 1.0 s. Find the induced emf in the coil as it is pulled out of the field.

  (Ans.1.75 x 10 <sup>2</sup> V)
- 15.18 An idea step down transformer is connected to main supply of 240 V. It is desired to operate a 12 V. 30 W lamp. Find the current in the primary and the transformation ratio?

  (Ans: 0.125A, 1/20)

# Chapter 16

## ALTERNATING CURRENT

#### **Learning Objectives**

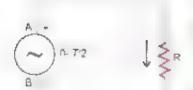
At the end of this chapter the students will be able to.

- 1 Understand and describe time period, frequency, the peak and root mean square values of an alternating current and voltage.
- 2 Know and use the relationship for the sinusoidal wave
- 3 Understand the flow of A C through resistors, capacitors and inductors
- Understand how phase tags and leads in the circuit.
- 5 Apply the knowledge to calculate the reactances of capacitors and inductors.
- 6 Describe impedance as vector summation of resistances.
- 7 Know and use the formulae of A.C. power to solve the problems.
- Understand the function of resonant circuits.
- 9 Appreciate the principle of metal detectors used for security checks.
- Describe the three phase A.C. supply
- 11 Become familiar with electromagnetic spectrum (ranging from radio waves to yrays)
- 12 Know the product on transmission and reception of electromagnetic waves

We have read in the last chapter that an A.C. generator produces alternating voltage/current. Now a days most of the electrical energy is produced by A.C. generators using water power or huge steam turbines. The main reason for the world wide use of A.C. is that it can be transmitted to long distances easily and at a very low cost.

#### **16.1 ALTERNATING CURRENT**

Alternating current (A.C., is that which is produced by a voltage source whose pointity keeps on reversing with time (Fig.16.1.a,b). In Fig.16.1.(a), the terminal A of the source is positive with respect to terminal B and it remains so during a time interval 0 to T/2. At t = T/2, the terminals change their polarity. Now A becomes negative with respect to B (Fig.16.1.b). This state continues during the time interval T/2 to T after which terminal A again becomes positive with respect to B and the next cycle starts. As a result of this change of polarity, the direction of the current flow in the circuit also changes. During the time 0 T/2, it flows in one direction and during the interval T/2 - T in opposite direction (Fig.16.1.a,b). This time interval T



(4)



(b Fg 161





during which the voltage source changes its polarity once is known as period 7 of the alternating current or voltage. Thus an alternating quantity is associated with a frequency figiven by

$$f = \frac{1}{T} \tag{16.1}$$

The most common source of alternating voltage is an A C generator which has been described in the previous chapter. The output V of this A C generator at any instant is given by

$$V = V \sin \frac{2\tau}{\tau} \cdot t \tag{16.2}$$

where T is period of the rotation of the coil and is equal to the

period of A.C. and  $\frac{2\pi}{T} = 2\pi f$  in is angular frequency of rotation

of the coil. Thus  $\frac{2\pi}{t} \cdot t$  of sithelangle  $\theta$  through which the

coil rotates in time f. Eq 16.2 shows that the value of alternating voltage V sinct constant it changes with time f.

When 
$$t=0$$
 to  $\frac{2^{-}}{t}$  is 0 and V is zero. When  $t=T/4$  to  $\frac{2\pi}{T} \times \frac{T}{4} = \frac{\pi}{2}$  and V attains its maximum value V at this

instant At t = T/2,  $\theta = \pi$  and V is zero. At this instant V changes its polarity and becomes negative henceforth

When 
$$t = \frac{37}{4}$$
 is  $\frac{37}{2}$  and  $V = -V$  and finally at the end of the

cycle when t=T,  $\theta=2\pi$  and V=0. The variation of V with time t and  $\theta$  is shown in Fig. 16.2 (a.b.) This graph between voltage and time is known as waveform of alternating voltage. It can be seen that it is a sine curve. Thus the output voltage of an A.C. generator varies sinusoidally with time in our daily life we are mostly dealing with this type of voltage so we will consider it in detail.

The value of voltage or current that exists in a circuit at any instant of time timestand from some reference point is known as its instantaneous value. It can have any value between plus maximum value +V and negative maximum

value  $-V_0$  and is denoted by V. The entire waveform shown in Fig. 16.2 is actually a set of all the instantaneous values that exist during a period T. Mathematically, it is given by  $V = V_0 \sin \theta = V_0 \sin \omega t$ 

$$V = V_a \sin \frac{2\pi}{T} \times t = V_a \sin 2\pi t$$
 ...... (16.3)

# 1

It is the highest value reached by the voltage or current in one cycle. For example, voltage shown in Fig. 16.2 has a peak value of  $V_a$ .

# Peak to Peak Value

It is the sum of the positive and negative peak values usually written as p-p value. The p-p value of the voltage waveform shown in Fig. 16.2 is 2V<sub>a</sub>

# ------

If we connect an ordinary D.C. ammeter to measure alternating current, it would measure its value as averaged over a cycle. It can be seen in Fig. 16.2 that the average value of current and voitage over a cycle is zero, but the power delivered during a cycle is not zero because power is //R and the values of / are positive even for negative values of /. Thus the average value of / is not zero and is called the mean square current. The alternating current or voltage is actually measured by square root of its mean square value known as root mean square (rms) value.

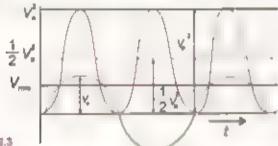
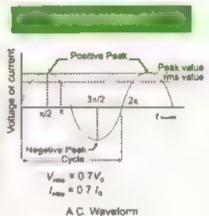


Fig. 18.3 It us come

Let us compute the average value of V' over a cycle. Fig. 16.3 shows an alternating voltage and the way its V' values vary. Note that the values of V' are positive on the negative half cycle also. As the graph of V' is symmetrical about the time  $\frac{1}{2}V_o$ , so for this figure the mean or the average value of V' is  $\frac{1}{2}V_o^2$ . The root mean square value of V is obtained by taking



113

the square root of V 2 Therefore,

$$V_{\text{crea}} = \sqrt{\frac{V_o^2}{2}} = \frac{V_o}{\sqrt{2}} = 0.7 V_o$$
 (16.4)

Similarly

$$I_{-} = \frac{I_o}{\sqrt{2}} = 0.7I_o$$

Most of the alternating current and voltage meters are calibrated to read rms values. When we speak of A.C. meter reading, we usually mean rms values unless stated otherwise.

**Example 16.1:** An A.C. voltmeter reads 250 V. What is its peak and instantaneous values if the frequency of a ternating voltage is 50 Hz?

#### Solution:

rms value of alternating voltage = V<sub>ms</sub> = 250 V

Its peak value V<sub>s</sub> is given by the relation

$$V_{-} = \frac{V_0}{\sqrt{2}}$$
  
 $V = \sqrt{2}V_{-} = \sqrt{2 \cdot 250} = 353.5 \text{ V}$ 

or

Angular frequency or - 2nf

Therefore instantaneous value is given by

#### Phonest Addition

We have seen that the instantaneous value of the alternating voltage is given by

V= V, sin wt

V=V,sin0

This angle  $\theta$  which specifies the instantaneous value of the alternating voltage or current is known as its phase. In Fig 16.2 (b), we can say that the phase at the points A, B, C, D and E is  $0.\pi/2.\pi.3\pi$ , 2 and  $2\pi$  respectively because these angles are the values of  $\theta$  at these points. Thus each point on the A.C. waveform corresponds to a certain phase

The phase at the positive peak is  $\pi/2 = 90^{\circ}$  and it is  $3\pi/2 = 270^{\circ}$  at the negative peak. The points where the waveform crosses the time axis correspond to phase 0 and  $\tau$ 

#### Phase Lag and Phase Lead

In practice, the phase difference between two alternating quantities is more important than their absolute phases. Fig. 16.4 shows two waveforms 1 and 2. The phase angles of the waveform 1 at the points A, B, C, D and E have been shown above the axis and those of waveform 2 below the axis. At the point B, the phase of 1 is  $\pi/2$  and that of 2 is 0. Similarly it can be seen that at each point the phase of waveform 2 is less than the phase of waveform 1 by an angle of  $\pi/2$ . It means that at each instant, the phase of A C, 2 is less than the phase of A.C. 1 by  $\pi/2$ . Similarly it can be seen in Fig. 16.5, that the phase at each point of the waveform of A C, 2 is greater than that of waveform 1 by an angle  $\pi/2$ . In this case, it is said that A C, 2 is leading the A.C. 1 by  $\pi/2$ . It means that at each instant of time the phase of A C, 2 is greater than that of time the phase of A C, 2 is greater than that of 1 by  $\pi/2$ .

Phase lead and lag between two alternating quantities is conveniently shown by representing the two A C quantities as vectors.

A sinusoidally alternating voltage or current can be graphically represented by a counter clockwise rotating vector provided it satisfies the following conditions.

- 1 Its length on a certain scale represents the peak or rms value of the alternating quantity
- It is in the horizontal position at the instant when the alternating quantity is zero and is increasing positively
- The angular frequency of the rotating vector is the same as the angular frequency of the alternating quantity

Fig. 16.6 (a) shows a sinusoidal voltage waveform leading an alternating current waveform by  $\pi$  / 2. The same fact has been shown vectorally in Fig. 16.6 (b). Here vector **OI** represents the peak or rms value of the current which is taken as the reference quantity. Similarly **OV** represents the rms or peak value of the alternating voltage which is leading the current by 90°. Both vectors are supposed to be rotating in the counter



Fig. 16 4

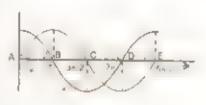
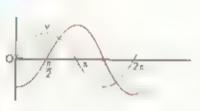


Fig. 16.5



(m)

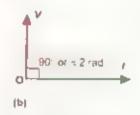


Fig. 16 6

clockwise direction at the angular frequency  $\omega$  of the two atternating quantities. Fig. 16.6 (b) shows the position of voltage and current vector at t=0

#### 16.2 A.C. CIRCUITS

The basic circuit element in a D.C. circuit is a resistor (R) which controls the current or voltage and the relationship between them is given by Ohm's law that is V = IR

In A.C. circuits, in addition to resistor R, two new circuit elements namely INDUCTOR (L) and CAPACITOR (C) become relevant. The current and voltages in A.C. circuits are controlled by three elements R L and C. We would study the response of an A.C. circuit when it is excited by an alternating voltage.

#### 16.3 A.C. THROUGH A RESISTOR

Fig. 16.7 (a) shows a resistor of resistance R connected with an alternating voltage source.

At any time t the potential difference across the terminals of the resistor is given by

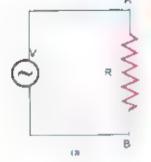
where V<sub>a</sub> is the peak value of the alternating voltage. The current I flowing through the circuit is given by Ohm's law

$$I = \frac{V}{R} = \frac{V_0}{R}$$
 sin  $\omega t$ 

where I is the instantaneous current and  $I_0 = \frac{v_0}{R}$  is the

peak value of the current. It follows from Eqs. 16.5 and 16.6 that the instantaneous values of both voltage and current are sine functions which vary with time (Fig. 16.7b). This figure shows that when voltage rises the current also rises. If the voltage falls, the current also does so – both pass their maximum and minimum values at the same instant. Thus in a purely resistive A.C. circuit, instantaneous values of voltage and current are in phase. This behaviour is shown graphically in Fig. 16.7 (b) and vectorially in Fig. 16.7 (c).

Fig. 16.7 (c) shows **V** and **I** vectors for resistance. They are drawn parallel because there is no phase difference between them. The opposition to A.C. which the circuit



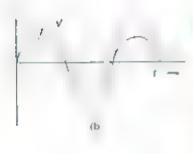




Fig. 16.7

presents is the resistance

$$R = \frac{V}{I}$$
 (167)

The instantaneous power in the resistance is given by

$$P = I^2 R = VI = V^2 / R$$
 ...... (16.8)

P sin watts, Visin volts, I is in amperes and R is in ohms. It is very important to note that the Eq. 16.8 holds only when the current and voltage are in phase.

#### 16.4 A.C. THROUGH A CAPACITOR

Alternating current can flow through a resistor, but it is not obvious that how it can flow through a capacitor. This can be demonstrated by the circuit shown in Fig 16 8. A low power bulb is connected in series with a 1 µF capacitor to supply mains through a switch. When the switch is closed, the bulb ights up showing that the current is flowing through the capacitor Direct current cannot flow through a capacitor continuously because of the presence of an insulating medium between the plates of the capacitor. Now let us see how does A.C. flows through a capacitor. The current flows. because the capacitor plates are continuously charged. discharged and charged the other way round by the alternating voltage (Fig. 16.9 a). The basic relation between the charge q on a capacitor and the voltage V across its plates re q = C V holds at every instant. If V = V, sin  $\omega t$  is the applied alternating voltage, the charge on the capacitor at any instant will be given by

$$q = C V = C V_s \sin \omega t$$
 ....... (16.9)

Since C: V are constants, it is obvious that q will vary the same way as applied voltage i.e., V and q are in phase (Fig. 16.9 b)

The current / is the rate of change of g with time i.e.,

$$I = \frac{\Delta q}{\Delta t}$$

So the value of / at any instant is the corresponding slope of the q - t curve. At O when q = 0, the slope is maximum, so / is then a maximum. From O to A, slope of the q-t curve decreases to zero. So / is zero at N. From A to B the slope of the q. I curve is negative and so / is negative from N to R. In this way the curve PNRST gives the variation of current with time.

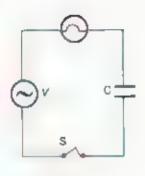
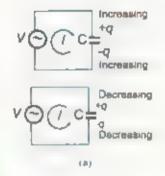
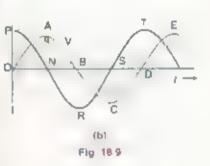
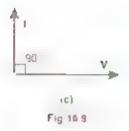


Fig. 16 8







Referring to the Fig. 16.2 bill toan be seen that the phase at O is zero and the phase at the upper maximum is  $\pi$  / 2. So in Fig. 16.9 (b) the phase of V at O is zero but the current at this point is maximum so its phase is  $\pi$  / 2. Thus, the current is leading the applied voltage by 90 or  $\pi$  2. Now consider the points A and N. The phase of alternating voltage at A is  $\pi$  2 but the phase of current at N is  $\pi$  Again the current is leading the voltage by 90 or  $\pi$  / 2. Similarly by companing the phase at the pair of points (B. R.) (C. S., and D. T.) tican be seen that at all these points the current leads the voltage by 90 or  $\pi$ /2. This is vectorially represented in Fig. 16.9 (c.).

Reactance of a capacitor is a measure of the opposition offered by the capacitor to the flow of A.C. It is usually represented by  $X_C$ . Its value is given by

$$X_{c} = \frac{V_{m}}{I_{m}}$$
 (16.10)

where  $V_{-}$  is the rms value of the alternating voltage across the capacitor and  $l_{-}$  is the rms value of current passing through the capacitor. The unit of reactance is ohm. In case of capacitor

$$X_C = \frac{1}{2\pi IC} = \frac{1}{\omega C}$$
 ...... (16.11)

According to Eq.16.11, a certain capacitor will have a large reactance at low frequency. So the magnitude of the opposition offered by it will be large and the current in the circuit will be small. On the other hand at high frequency the reactance will be low and the light frequency current himsigh the same capacitor will be large.

Example 16.2: A 100 µF capacitor is connected to an a ternating voltage of 24 V and frequency 50 Hz. Calculate

- a. The reactance of the capacitor and
- b. The current in the circuit

#### Solution:

From the equation 
$$X_c = \frac{V_m}{l_m}$$
  
or  $I_m = \frac{V_m}{X_c} = \frac{24 \text{ V}}{31.8 \Omega} = 0.75 \text{ A}$ 

#### 16.5 A.C. THROUGH AN INDUCTOR

An inductor is usually in the form of a coil or a sciencid wound from a thick wire so that it has a large value of self-inductance and has a negligible resistance. We have already seen how self-inductance opposes changes of current. So when an alternating source of voltage is applied across an inductor, it must oppose the flow of A.C. which is continuously changing (Fig. 16.10). Let us assume that the resistance of the coil is negligible. We can simplify the theory by considering first, the current and then finding the potential difference across the inductor which will cause this current. Suppose the current is  $I \simeq I_s \sin 2 \pi f t$ . If L is the inductance of the coil, the changing current sets up a back emf in the coil of magnitude.

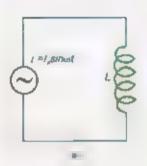
$$c = L \frac{\Delta I}{\Delta t}$$

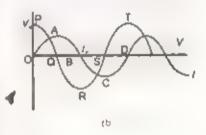
To maintain the current, the applied voltage must be equal to the back e m f. The applied voltage across the coil must, therefore, be equal to

$$V = L \frac{\Delta I}{\Delta t}$$

Since L is a constant, V is proportional to  $\frac{\Delta l}{\Delta l}$  Fig 16.10 (b)

shows how the current I varies with time. The value of  $\Delta I / \Delta I$  is given by the slope of the I - t curve at the various instants of time. At O, the value of the slope is maximum, so the maximum value of V equal to V, occurs at O and is represented by OP (Fig. 16.10 b). From O to A the slope of I - t graph decreases to zero so the voltage decreases form  $V_n$  to zero at Q. From A to B, the slope of the I - t graph is negative, so the voltage curve goes from Q to R. In this way the voltage is represented by the curve PQRST corresponding to current curve OABCD. By comparing the phases of the pair of points O(P), O(P),







This is vectorially shown in Fig. 16 10(c). Inductive reactance is a measure of the opposition offered by the inductance coll to the flow of A.C. It is usually denoted by X<sub>i</sub>.

 $X_{-} = V_{--}$  (16 12)

If  $V_{\rm max}$  is rms value of the alternating voltage across an inductance and  $I_{\rm rms}$ , the rms value of the current passing through it, the value of  $X_{\rm L}$  is given by

 $X_{i} = \frac{V_{-}}{I_{-}} = 2\pi f L \quad \omega L \tag{16.13}$ 

The reactance of a coil, therefore, depends upon the frequency of the A C and the inductance L it is directly proportional to both f and L. L is expressed in henry, f in hertz, and  $X_{\ell}$  in ohms. It is to be noted that inductance and capacitance behave oppositely as a function of frequency. If f is low  $X_{\ell}$  is small but  $X_{\ell}$  is large. For high f  $X_{\ell}$  is large but  $X_{\ell}$  is small. The behaviour of resistance is independent of frequency.

Referring to Fig 16.10 (b) it can be seen that no power is dissipated in a pure inductor. In the first quarter of cycle both V and I are positive so the power is positive, which means energy is supplied to inductor. In the second quarter, V is positive but I is negative. Now power is negative which implies that energy is returned by the inductor. Again in third quarter, it receives energy but returns the same amount in the fourth quarter. Thus, there is no net change of energy in a complete cycle. Since an inductor coil does not consume energy, the coil is often employed for controlling A.C. without consumption of energy. Such an inductance coil is known as choke.

#### 16.6 IMPEDANCE

We already know that resistance R offers opposition to the flow of current. In case of A.C. an inductance L or a capacitance C also offer opposition to the flow of A.C. which is measured by reactances  $X_t$  and  $X_C$  respectively An.A.C. circuit may consist of a resistance R, an inductance L, a capacitance C or a combination of these elements. The combined effect of resistance and reactances in such a circuit is known as impedance and is denoted by Z.

It is measured by the ratio of the rms value of the applied voltage to the rms value of resulting A.C. Thus

$$Z = \frac{V_{\text{max}}}{I_{\text{max}}} \tag{16.14}$$





Inductors are made in many sizes to perform a wide variety of functions in business and industry

It is also expressed in ohms.

Example 16.3. When 10 V are applied to an A.C. circuit, the current flowing init is 100 mA. Find its impedance.

#### Solution:

rms value of applied voltage =  $V_{ms}$  = 10 V rms value of current =  $I_{ms}$  = 100 mA = 100 x 10  $^{3}$ A  $V_{ms}$  = 10 V Impedance  $Z = I_{ms}$  = 100 x 10  $^{3}$ A

#### 16.7 R-C AND R-L SERIES CIRCUITS

Consider a series network of resistance R and a capacitor C excited by an alternating voltage (Fig. 16.11 a). As R and C are in series, the same current would flow through each of them. If  $I_{mal}$  is the value of current, the potential difference across the resistance R would be  $I_{mal}$  R and it would be in phase with current  $I_{mal}$ . The vector diagram of the voltage and current is shown in Fig.16.11 (b). Taking the current as reference, the potential difference  $I_{mal}$  R across the resistance is represented by a line along the current line because potential drop  $I_{mal}$  R is in phase with current. The potential difference across the capacitor will be  $I_{mal} X_c = I_{mal} I_{mal} C$ . As this voltage lags the current by 90° so the line representing the vector  $I_{mal} I_{mal} C$  is drawn at right angles to the current line (Fig.16.11 b).

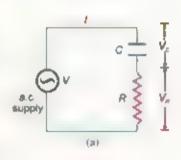
The applied voltage  $V_{\rm eq}$  that will send the current / in the circuit is obtained by the resultant of the vectors  $I_{\rm eq}$  R and

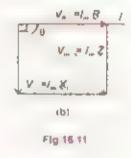
$$V_{m_0} = \sqrt{(I_{m_0}R)^2 + \left(\frac{I_{m_0}}{\omega C}\right)^2}$$

$$V_{m_0} = I_{m_0}\sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}$$

Impedance 
$$Z = \frac{V_{m}}{I_{m}} = \sqrt{R^2 + \frac{1}{(\omega C)^2}}$$
 (16.15)

It can be seen in Fig. 16.11 (b) that the current and the applied voltage are not in phase. The current leads the applied voltage by an angle 8 such that





Eq 16.15 suggests that we can find the impedance of a senes A C circuit by vector addition. The resistance R is represented by a horizontal line in the direction of current

which is taken as reference. The reactance  $X_c = \frac{I}{\omega C}$  is

shown by a line tagging the R - line by 90° (Fig 16 11 c). The impedance **Z** of the circuit is obtained by the vector summation of resistance and reactance. Fig 16 11 (c) is known as impedance diagram of the circuit. The angle which the line representing the impedance **Z** makes with **R** line gives the phase difference between the voltage and current in Fig 16 11(c), the current is leading the voltage applied by an angle.

$$\theta = \tan^{-1} \left( \frac{X_{C}}{R} \right) = \tan^{-1} \left( \frac{1}{\omega CR} \right)$$

Now we will calculate the impedance of a R-L series directly drawing its impedance diagram. Fig. 16-12 (a) shows an R-L series directly excited by an A.C. source of frequency of the current is taken as reference, so it is represented by a horizontal line. Resistance R is drawn along this line because the potential drop  $I_{m_0}(R)$  is in phase with current. As the potential across the inductance  $V_{i_0} = I_{m_0}(R) = I_{m_0}(R)$  leads the current by  $90^\circ$ , so the vector line of reactance  $X_{i_0} = R L$  is drawn at right angle to R line (Fig. 16.12 b). The impedance Z of the circuit is obtained by the vector sum of R and R L lines.

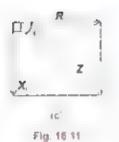
$$Z = \sqrt{R^2 + (\omega L)^2}$$

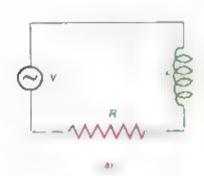
The angle  $\theta = \tan^{-1} \frac{\alpha L}{R}$  which Z makes with R line gives the

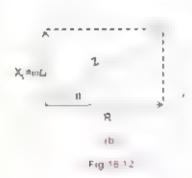
phase difference between the applied voltage and current. In this case the voltage leads the current by  $\theta^*$ . By comparing the impedance diagrams of  $R \cdot C$  and  $L \cdot R$  circuits, it can be seen that the vector lines of reactances  $X_C$  and  $X_L$  are directed opposite to each other with R as reference.

#### 16.8 POWER IN A.C. CIRCUITS

The expression for power is  $P = V_{m_0}I_{m_0}$  This expression is true in case of A.C. circuits only when V and I are in phase as in







case of a purely resistive circuit. We have already seen that the power dissipation in a pure inductive or in a pure capacitance circuit is zero. In these cases the current lags or leads the applied voltage by 90° and component of applied voltage vector  $\mathbf{V}$  along the current vector is zero (Fig.16.9 c and 16.10 c) in A.C. circuit the phase difference between applied voltage  $\mathbf{V}$  and the current  $I_{max}$  is  $\mathbf{0}$  (Fig.16.11 b and 16.12 b). The component of  $\mathbf{V}$  along current  $I_{max}$  is  $V_{max}$  cos $\mathbf{0}$ . Actually it is this component of voltage vector which is in phase with current. So the power dissipated in A.C. circuit

$$P - I_{\text{max}} \times V_{\text{max}} \cos \theta \tag{16.17}$$

The factor cos0 is known as power factor.

**Example 16.4:** At what frequency will an inductor of  $1.0 \,\mathrm{H}$  have a reactance of  $500 \,\Omega$ ?

**Example 16.5:** An iron core coil of 2.0 H and 50  $\Omega$  is placed in series with a resistance of 450  $\Omega$ . An A.C. supply of 100 V, 50 Hz is connected across the circuit. Find (i) the current flowing in the coil, (ii) phase angle between the current and voltage.



A metal detector is used to locate burned metal objects

#### Solution:

Resistance =  $R = 50 \,\Omega + 450 \,\Omega = 500 \,\Omega$ Inductance =  $L = 20 \,\text{H}$ Supply voltage =  $V_{\text{max}} = 100 \,\text{V}$ Frequency =  $f = 50 \,\text{Hz}$ The reactance =  $X_1 = \omega L = 2\pi f L$ =  $2 \times 3.14 \times 50 \,\text{s}^{-1} \times 2.0 \,\text{H} = 628 \,\Omega$ Impedance =  $Z = \sqrt{R^2 + (\omega L)^2}$ =  $\sqrt{(500 \,\Omega)^2 + (628 \,\Omega)^2} = 803 \,\Omega$ Current  $I_{\text{max}} = \frac{V_{\text{max}}}{Z} = \frac{100 \,\text{V}}{803 \,\Omega} = 0.01245 \,\text{A} = 12.45 \,\text{mA}$ Phase difference  $\theta = \tan^{-1}\left(\frac{\omega L}{R}\right)$ 

$$= \tan^{-1} \left( \frac{628 \,\Omega}{500 \,\Omega} \right) = 51.5^{\circ}$$

**Example 16.6:** A circuit consists of a capacitor of  $2 \, \mu F$  and a resistance of  $1000 \, \Omega$  connected in series. An alternating voltage of  $12 \, V$  and frequency  $50 \, Hz$  is applied. Find (i) the current in the circuit, and (ii) the average power supplied.

#### Solution:

Resistance = 
$$R = 1000 \Omega$$

Reactance = 
$$X_C = \frac{1}{2\pi fC}$$

$$=\frac{1}{2\times3.14\times50}$$
 s<sup>-1</sup> × 2×10 <sup>6</sup>F = 1592  $\Omega$ 

Impedance = 
$$Z = \sqrt{R^2 + (X_C)^2}$$

$$=\sqrt{(1000 \Omega)^2 + (1592 \Omega)^2} = 1880 \Omega$$

Current = 
$$I_{m_1} = \frac{V_{m_0}}{Z} = \frac{12 \text{ V}}{1880 \Omega} = 0.0064 \text{ A} = 6.4 \text{ mA}$$

Phase Difference 
$$\theta = \tan^{-1} \frac{X_C}{R} = \tan^{-1} \frac{1592 \Omega}{1000 \Omega} = 57.87^{\circ}$$

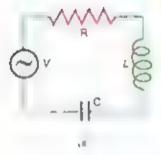
### 16.9 SERIES RESONANCE CIRCUIT

Consider a R - L - C series circuit which is excited by an alternating voltage source whose frequency could be varied (Fig. 16.13.a). The impedance diagram of the circuit is shown in Fig. 16.13 (b). As explained earlier, the inductive reactance.

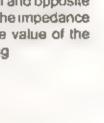
 $X_c = \omega L$  and capacitor reactance  $X_c = \frac{1}{\omega C}$  are directed

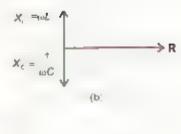
opposite to each other. When the frequency of A.C. source is very small  $X_c = \frac{1}{\omega C}$  is much greater than  $X_t = \omega L$ . So the

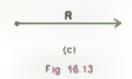
capacitance dominates at low frequencies and the circuit



behaves like an R + C circuit. At high frequencies  $X_t = \omega L$  is much greater than  $X_C = \frac{1}{\omega C}$ . In this case the inductance dominates and the circuit behaves like R + L circuit. In between these frequencies there will be a frequency  $\omega_c$  at which  $X_t = X_C$ . This condition is called resonance. Thus at resonance the inductive reactance being equal and opposite to capacitor reactance, cancel each other and the impedance diagram assumes the form (Fig. 16.13 c). The value of the resonance frequency can be obtained by putting





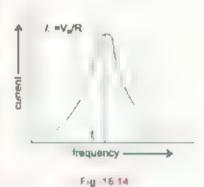


The following are the properties of the series resonance.

r) The resonance frequency is given by

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

- The impedance of the circuit at resonance is resistive so the current and voltage are in phase. The power factor is 1.
- ii) The impedance of the circuit is minimum at this frequency and it is equal to R
- v) If the amplitude of the source voltage V<sub>a</sub> is constant, the current is a maximum at the resonance frequency and its value is V<sub>a</sub>/R. The variation of current with the frequency is shown in Fig. 16.14.
- At resonance V<sub>1</sub>, the voltage drop across inductance and V<sub>C</sub> the voltage drop across capacitance may be much larger than the source voltage.



#### 16.10 PARALLEL RESONANCE CIRCUIT

Fig. 16.15 shows an L - C parallel circuit. It is excited by an alternating source of voltage whose frequency could be varied. The inductance coil L has a resistance r which is negligibly small. The capacitor draws a leading current,

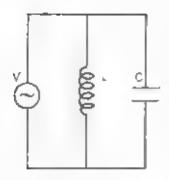
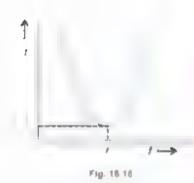


Fig. 16 15



whereas the coil draws a lagging current. The circuit resonates at a frequency  $\omega = \omega$ , which makes  $X_c = X_c$  so that the two branch currents are equal but opposite. Hence, they cancel out with the result that the current drawn from the supply is zero. In actual practice, the current is not zero but has a minimum value due to small resistance r of the coil

Properties of parallel resonant circuits are

- i) Resonance frequency is  $f = \frac{1}{2\pi \sqrt{LC}}$
- At the resonance frequency the circuit impedance is maximum. It is resistive.
- phase with the applied voltage. So the power factor is one. The variation of current with the frequency of the source is shown in Fig. 16.16.
- At resonance, the branch currents I<sub>c</sub> and I<sub>c</sub> may each be larger than the source current I.

**Example 16.7:** Find the capacitance required to construct a resonance circuit of frequency 1000 kHz with an inductor of 5 mH.

#### Solution:

Resonance frequency = f = 1000 kHz

Resonance frequency = fr = 2 = LC

$$C = \frac{1}{4\pi^2 f^2 L} + \frac{1}{4 \times (3.14)^5 + (10^6 \text{ s}^{-1})^4 + 5 \cdot 10^{-3} \text{ H}} = 5.09 \text{ pF}$$

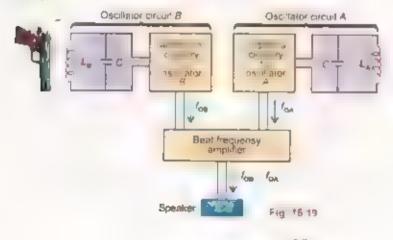
#### 16.11 THREE PHASE A.C. SUPPLY

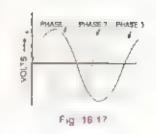
We have already studied that an A.C. generator consists of a con with a pair of slip rings. As the coil rotates an a ternating voltage is generated across the slip rings. In a three phase A.C. generator instead of one coil, there are three coils inclined at 120° to each other each connected to its own pair of slip rings. When this combination of three coils rotate in the magnetic field, each coil generates an alternating voltage across its own pair of slip rings. Thus, three alternating voltages are generated. The phase difference between these voltages is 120°. It means that when voltage across the first

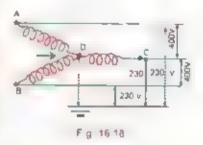
pair of slip rings is zero, having a phase of 0, the voltage across the second pair of silp rings would not be zero but it will have a phase of 120° Similarly at this instant the voltage generated across the third pair will have a phase 240°. This is shown in Fig. 16.17. The machine instead of having six terminals, two for each pair of slip rings, has only four terminals because the starting point of all the three coils has a common junction which is often earthed to the shaft of the generator and the other three ends of the coils are connected. to three separate terminals on the machine. These four terminals along with the lines and coils connected to them are shown in Fig 16.18. The voltage across each of lines connected to terminals A, B, C and the neutral line is 230 V Because of 120° phase shift, the voltage across any two lines is about 400 V. The main advantage of having a three phase supply is that the total load of the house or a factory is divided in three parts, so that none of the line is over loaded. If heavy load consisting of a number of air conditioners and motors etc., is supplied power from a single phase supply, its voltage is like y to drop at full load. Moreover, the three phase supply also provides 400 V which can be used to operate some special appliances requiring 400 V for their operation.

#### 16.12 PRINCIPLE OF METAL DETECTORS

A coll and a capacitor are electrical components which together can produce oscillations of current. An L. C circuit behaves just like an oscillating mass - spring system. In this case energy oscillates between a capacitor and an inductor. The circuit is called an electrical oscillator. Two such oscillators A and B are used in the operation of a common type of metal detector (Fig. 16-19). In the absence of any nearby.







metal object, the inductances  $L_{\rm A}$  and  $L_{\rm B}$  are the same and hence the resonance frequency of the two circuits is also same. When the inductor B, called the search coil comes near a metal object, its inductance  $L_{\rm B}$  decreases and corresponding oscillator frequency increases and thus a beat note is heard in the attached speaker Such detectors are extensively used not only for various security checks but also to locate buried metal objects

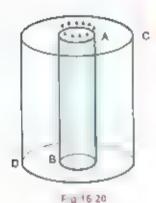
#### 16.13 CHOKE

It is a coil which consists of thick copper wire wound closely in a large number of turns over a soft iron laminated cores. This makes the inductance  $\ell$  of the coil quite large whereas its resistance R is very small. Thus it consumes extremely small power. It is used in A.C. circuits to limit current with extremely small wastage of energy as compared to a resistance or a rheostat.

#### 16.14 ELECTROMAGNETIC WAVES

It is a very important class of waves which requires no medium for transmission and which rapidly propagates through vacuum.

In 1864 British physicist James Clark Maxwell formulated a set of equations known as Maxwel's equations which explained the various electromagnetic phenomena According to these equations a changing magnetic flux creates an electric field and a changing electric flux creates a magnetic field. Consider a region of space AB as shown in Fig. 16-20. Suppose a change of magnetic flux is taking place through it. This changing magnetic flux will set up a changing electric flux in the surrounding region. The creation of electric field in the region CD will cause a change of electric flux through it due to which a magnetic field would be set up in the space surrounding CD and so on. Thus each field generates the other and the whole package of electric and magnetic fields will move along propelling itself through space. Such moving electric and magnetic fields are known as electromagnetic waves. The electric field, magnetic field and the direction of their propagation are mutually orthogonal (Fig 16.21). It can be seen in this figure that the electromagnetic waves are periodic, hence they have a wavelength  $\lambda$  which is given by the relation  $c = f\lambda$  where f is the frequency and c is the speed of the wave. In free space the speed of electromagnetic waves is 3 x 10<sup>8</sup> ms <sup>1</sup>



128

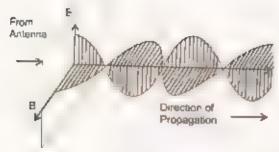
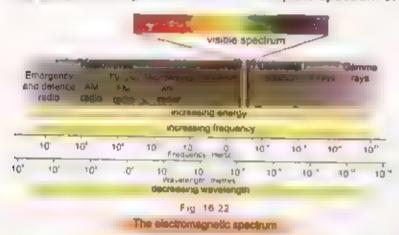


Fig. 16.21

Depending upon the values of wavelength and frequency, the electromagnetic waves have been classified into different types of waves as radiowaves, microwaves infrared rays, visible light etc. Fig 16.22 shows the complete spectrum of



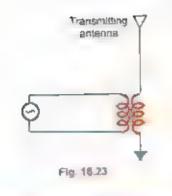
Electromagnetic waves from the low radio waves to high frequency gamma rays.

#### 16.15 PRINCIPLE OF GENERATION, TRANSMISSION AND RECEPTION OF ELECTROMAGNETIC WAVES

We have seen that electromagnetic waves are generated when electric or magnetic flux is changing through a certain region of space. An electric charge at rest gives rise to a Coulomb's field which does not radiate in space because no change of flux takes place in this type of field. A charge moving with constant velocity is equivalent to a steady current which generates a constant magnetic field in the

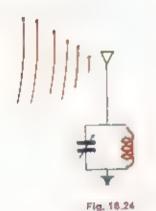


Shake an electrically charged object to and fro and you produce electromagnet waves.





When electrons in the transmitting antenna vibrate 94 000 times each second they produced radio waves having fraquericy 94 kHz.



surrounding space, but such a field also does not radiate out because no changes of magnetic flux are involved. Thus only change to generate a wave of moving field is when we accelerate the electrical charges.

A radio transmitting antenna provides a good example of generating electromagnetic waves by acceleration of charges. The piece of wire along which charges are made to accelerate is known as transmitting antenna (Fig 16 23). It is charged by an atternating source of potential of frequency f and time period 7. As the charging potential alternates, the charge on the antenna also constantly reverses For example if the top has + q charges at any instant, then after time 1/2 the charge on it will be - q. Such regular reversal of charges on the antenna gives rise to an electric flux that constantly changes with frequency f. This changing electric flux sets up an electromagnetic wave which propagates out in space away from the antenna. The frequency with which the fields alternate is always equal to the frequency of the source generating them. These electromagnetic waves which are propagated out in space from antenna of a transmitter are known as radio waves. In free space these waves travel with the speed of light.

Suppose these waves impinge on a piece of wire (Fig. 16.24). The electrons in the wire move under the action of the oscillating electric field which give rise to an alternating voltage across the wire. The frequency of this voltage is the same as that of the wave intercepting the wire. This wire receiving the wave is known as receiving antenna. As the electric field of the wave is very weak at a distance of many kilometres from the transmitter, the voltage that appears across the receiving antenna is very small. Each transmitter propagates radio waves of one particular frequency. So when a number of transmitting stations operate simultaneously we have a number of radio waves of different frequencies in the space. Thus the voltage that appears across a receiving antenna placed in space is usually due to the radio waves of large number of frequencies. The voltage of one particular frequency can be picked up by connecting an inductance t and a variable capacitor C in parallel with one and of the receiving antenna (Fig.16.24).

If one adjusts the value of the capacitor so that the natural frequency of L - C circuit is the same as that of the transmitting station to be picked up, the circuit will resonate

under the driving action of the antenna. Consequently, the L - C circuit will build up a large response to the action of only that radio wave to which it is tuned. In your radio receiver set when you change stations you actually adjust the value of C.

#### 16.16 MODULATION

Speech and music etc. are transmitted hundred of knometres away by a radio transmitter. The scene in front of a television camera is also sent many kilometres away to viewers. In all these uses, the carrier of the programme is a high frequency radio wave. The information i.e., light, sound or other data is impressed on the radio wave and is carried along with it to the destination.

Modulation is the process of combining the low frequency a gnal with a high frequency radio wave called carrier wave. The resultant wave is called modulated carrier wave. The low frequency signal is known as modulation signal. Modulation is achieved by changing the amplitude or the frequency of the carrier wave in accordance with the modulating signal. Thus we have two types of modulations which are

1 Amplitude modulation (A M), 2 Frequency modulation (F M)

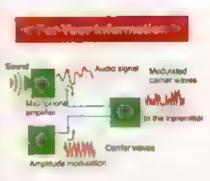
#### Amplikude Modulation

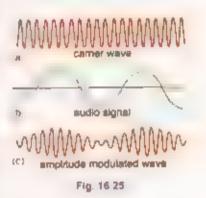
In this type of modulation the amplitude of the carrier wave is increased or diminished as the amplitude of the superposing modulating signal increases and decreases.

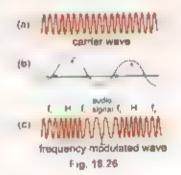
Fig 16 25 (a) represents a high frequency carrier wave of constant amplitude and frequency Fig 16.25(b) represents a low or audio frequency signal of a sine waveform. Fig 16 25 (c) shows the result obtained by modulating thecarrier waves with the modulating wave. The AM transmission frequencies range from 540 kHz to 1600 kHz.

#### requency Modulation

In this type of modulation the frequency of the camer wave is increased or diminished as the modulating signal amplitude increases or decreases but the carrier wave amplitude remains constant. Fig 16.26 shows frequency modulation. The frequency of the modulated carrier wave is highest (point H) when the signal amplitude is at its maximum positive value and is at its lowest frequency (point L) when signal amplitude has maximum negative. When the signal amplitude is zero, the carrier frequency is at its normal frequency  $f_{\rm e}$ .







The FM transmission frequencies are much higher and ranges between 88 MHz to 108 MHz. FM, radio waves are affected less by electrical interference than A.M. radio waves and hence, provide a higher quality transmission of sound. However, they have a shorter range than A.M. waves and are less able to travel around obstacles such as hills and large buildings.

Alternating current is that which is produced by a voltage source whose polarity keeps on reversing with time.

The time interval during which the voltage source changes its polarity once is known
as period. Tof the alternating current or voltage.

The velue of voitage or current that exists in a circuit at any instant of time measured from some reference point is known as its instantaneous value.

The highest value reached by the voltage or current in one cycle is called the peak value of the voltage or current.

The sum of positive and negative peak values is called peak to peak value and is written as p-pivalue.

The root mean square value (rms) is the square root of the laverage value of V<sup>2</sup>or I<sup>\*</sup>.

The angle  $\theta$  which specifies the instantaneous value of the alternating voltage of current, gives the phase lag or phase lead of one quantity over the other

An inductor is usually in the form of a coil or a solenoid wound from a thick wire so that it has a large value of self-inductance and has negligible resistance.

The combined effect of resistance and reactance in a circuit is known as impedance and is denoted by Z.

- Choke is a coll which consists of thick copper wire wound closely in a large number of turns over a soft iron faminated core.
- Electromagnetic waves are those which require no medium for transmission and rapidly propagate through vacuum.
- Modulation is the process of combining the low frequency signal with a high frequency radio wave called carrier waves. The resultant wave is called modulated carrier wave.



15.1 Asinusoidal current has rms value of 10A. What is the maximum or peak value?

- Name the device that will a permit flow of direct current but oppose the flow of alternating current permit flow of alternating current but not the direct current.
- How many times per second will an incandescent lamp reach maximum brilliance when connected to a 50 Hz source?
  - A circuit contains an iron-cored inductor a switch and a D C source arranged in series. The switch is closed and after an interval reopened. Explain why a spark jumps across the switch contacts?
- How does doubling the frequency affect the reactance of a an inductor (b) a capacitor?
- 16.6 In a R L circuit, will the current lag or lead the voltage? If ustrate your answer by a vector diagram.
- A choke coil placed in series with an electric lamp in an A.C. circuit causes the lamp to become dim. Why is it so? A variable capacitor added in series in this circuit may be adjusted until the lamp glows with normal brilliance. Explain how this is possible?
  - Explain the conditions under which electromagnetic waves are produced from a source?
  - How the reception of a particular radio station is selected on your radio set?
  - What is meant by A.M. and F.M.?

# PROBLEM

- An externating current is represented by the equation / = 20 sin100 π/. Compute its frequency and the maximum and rms values of current (Ans: 50 Hz, 20 A, 14 A)
- A sinuso dal A C has a maximum value of 15 A. What are its rms values? If the time is recorded from the instant the current is zero and is becoming positive, what is the instantaneous value of the current after 1 / 300 s, given the frequency is 50 Hz (Ans.: I<sub>mi</sub>=10.6 A, Instantaneous current = 13.0 A)
- Find the value of the current and inductive reactance when A.C. voltage of 220 V at 50 Hz is passed through an inductor of 10 H (Ans.  $I_{eq} = 0.07 \text{ A}, X_{b} = 3140 \Omega$ )
- A circuit has an inductance of  $1/\pi$  H and resistance of 2000  $\Omega$  A 50 Hz A.C is supplied to it. Calculate the reactance and impedance offered by the circuit. (Ans:  $X_L = 100 \Omega$ ,  $Z = 2002.5 \Omega$ )
- An inductor of pure inductance  $3/\pi$  H is connected in series with a resistance of  $40~\Omega$ . Find the peak value of the current the rms value, and (ii ) the phase difference between the current and the applied voltage  $V=350~\mathrm{sm}(100\pi~\mathrm{f})$ .
  - (Ans: (i) 1.16 A, (ii) 0.81 A, (iii) 82.4°)
- 16.6 A 10 mH, 20 Ω coil is connected across 240 V and 180 /π Hz source. How much power does it dissipate? (Ans: 2778 W)

- 16.7 Find the value of the current flowing through a capacitance 0.5 μF when connected to a source of 150 V at 50 Hz (Ans: I<sub>ms</sub> = 0.024 A)
- An alternating source of emf 12 V and frequency 50 Hz is applied to a capacitor of capacitance 3 μF in series with a resistor of resistance 1k Ω. Calculate the phase angle.

  (Ans: 46.7°)
- What is the resonant frequency of a circuit which includes a coil of inductance 2.5 H and a capacitance 40 µF? (Ans: 15.9 Hz)
- 16 10 An inductor of inductance 150 µH is connected in parallel with a variable capacitor whose capacitance can be changed from 500 pF to 20 pF. Calculate the maximum frequency and minimum frequency for which the circuit can be tuned (Ans. 2.91 MHz, 0.58 MHz)

# Chapter 17

# PHYSICS OF SOLIDS

#### **Learning Objectives**

At the end of this chapter the students will be able to:

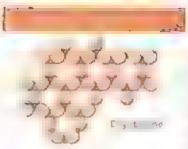
- Distinguish between the structure of crystalline, glassy, amorphous and polymeric souds
- Understand the idea of lattice.
- 3 Appreciate that deformation is caused by a force and that, in one dimension, the deformation can be tensile or compressive.
- 4 Define and use the terms Young's modulus, bulk modulus and shear modulus.
- 5 Describe an experiment to determine elastic limit and yield strength.
- 6 Distinguish between elastic and plastic deformation of a material
- 7 Synthesize and deduce the strain energy in a deformed material from the area under the force extension graph.
- Describe the energy bands in solids.
- 9 Classify insulators conductors, semi-conductors on the basis of energy bands
- 10 Distinguish between intrinsic and extrinsic semiconductors
- 11 Explain how electrons and holes flow across a junction
- Describe superconductors.
- 13 Distinguish between dia, para and ferro magnetic materials.
- 14 Understand and describe the concept of magnetic domains in a material
- 15. Know the Curie point.
- 16 Classify hard and soft ferro magnetic substances.
- 17 Understand hysteresis and hysteresis loss.

aterials have specific uses depending upon their characteristics and properties, such as hardness, ductivity, malleability, conductivity, etc. What makes steel hard, lead soft, iron magnetic and copper electrically conducting? It depends upon the structure -- the particular order and bonding of atoms in a material. This clue has made it possible to design and create materials with new and unusual properties for use in modern technology.

#### 17.1 CLASSIFICATION OF SOLIDS

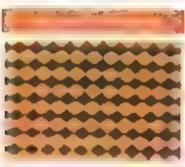


In crystalline solids there is a regular arrangement of molecules. The neighbours of every molecule are arranged in a regular pattern that is constant throughout the crystal. There is, thus an ordered structure in crystalline solids.

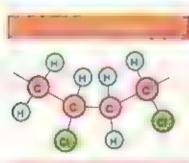




Glassy and crystalline solide-shortand long-range order



Transmission Electors Micrograph of the atomic lettics of a gold crystal.



Part of a PVC molecule

The vast majority of solids, e.g., metals such as copper, iron and zinc. ionic compounds such as sodium chloride, ceramics such as zirconia are crystalline. The arrangement of molecules atoms or ions within all types of crystalline solids can be studied using vanous X-ray techniques. It should be noted that atoms, molecules or ions in a crystalline solid are not static. For example, each atom in a metal crystall vibrates about a fixed point with an amplitude that increases with rise in temperature. It is the average atomic positions which are perfectly ordered overlarge distances.

The cohesive forces between atoms, molecules or ons in crystalline solids maintain the strict long-range order inspite of atomic vibrations. For every crystal, however, there is a temperature at which the vibrations become so great that the structure suddenly breaks up, and the solid melts. The transition from solid (order) to liquid (disorder) is, therefore, abrupt or discontinuous. Every crystailine solid has a definite melting point.

The word amorphous means without form or structure. Thus in amorphous solids there is no regular arrangement of molecules like that in crystaline solids. We can therefore say that amorphous solids are more like liquids with the disordered structure frozen in

For example ordinary glass which is a solid at ordinary temperature, has no regular arrangement of molecules. On heating it gradually softens into a paste like state before it becomes a very viscous liquid at almost 800°C. Thus amorphous solids are also called glassy solids. This type of solids have no definite melting point.

Polymers may be said to be more or less solid materials with a structure that is intermediate between order and disorder. They can be classified as partially or poorly crystalline solids.

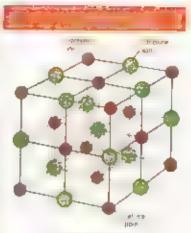
Polymers form a large group of naturally occurring and synthetic materials. Plastics and synthetic rubbers are termed 'Ploymers' because they are formed by polymerization reactions in which relatively simple molecules are chemically combined into massive long chain molecules or "three dimensional" structures. These materials have rather low specific gravity compared with even the lightest of metals, and

#### yet exhibit good strength-to-weight ratio.

Polymers consist who, ly or in part of chemical combinations of carbon with oxygen hydrogen nitrogen and other metallic or non-metallic elements. Polythene polystrene and nylon etclare examples of polymers. Natural rubber is composed in the pure state entirely of a hydrocarbon with the formula (C<sub>5</sub>H<sub>6</sub>).

#### Crystal Latin

A crystaline solid consists of three dimensional pattern that repeats itself over and over again. This smallest three dimensional basic structure is called unit cell. The whole structure obtained by the repetition of unit cell is known as crystal lattice. For example, the pattern of NaCl particles have a cube shape. The cube shape of the sodium chloride is just one of several crystal shapes. In a cubic crystal all the sides meet at right angles. Other crystal shapes have comers in which one or more of the angles are not right angles.



NaCl crystal lattice

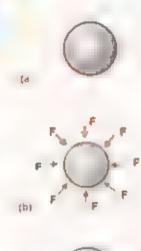
# 17.2 MECHANICAL PROPERTIES OF SOLIDS



If we hold a soft rubber ball in our hand and then squeeze it the shape or volume of the ball will change. However, if we stop equeezing the ball, and open our hand, the ball will return to its original spherical shape. This has been illustrated schematically in Fig. 17.1.

Similarly if we hold two ends of a rubber string in our hands and move our hands apart to some extent, the length of the string will increase under the action of the applied force exerted by our hands. Greater the applied force larger will be the increase in length. Now on removing the applied force, the string will return to its original length. From these examples, it is concluded that deformation (i.e. change in shape, length or volume) is produced when a body is subjected to some external force.

In crystalline solids atoms are usually arranged in a certain order. These atoms are held about their equilibrium position which depends on the strength of the inter-atomic cohesive force between them. When external force is applied on such a body, a distortion results because of the displacement of the atoms from their equilibrium position and the body is said to be in a state of stress. After the removal of external force,

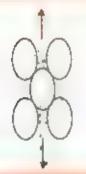




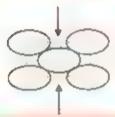
Onginal rubber ball
Squeezed rubber ball subjected
force F by the hand
Rubber ball after removing force



(a, Unstretched unit cell



(in Unit cell under outwerd atretching force



(e) Unit cell under inward applied force



 (d) unit cell after removing applied force

Fig. 17.2

the atoms return to their equilibrium position, and the body regains its original shape provided that external applied force was not too great. The ability of the body to return to its original shape is called elasticity. Fig. 17.2 illustrates deformation produced in a unit cell of a crystal subjected to an external applied force.

Callingual Section

The results of mechanical tests are usually expressed in terms of stress and strain, which are defined in terms of applied force and deformation.

It is defined as the force applied on unit area to produce any change in the shape, volume or length of a body. Mathematically it is expressed as

Stress 
$$(\sigma) = \frac{\text{Force } (F)}{\text{Area } (A)}$$
 (17.1)

The SI unit of stress (o) is newton per square metre. (Nm²) which is given the name pascal (Pa).

Stress may cause a change in length volume and shape. When a stress changes length it is called the tensile stress, when it changes the volume it is called the volume is tress and when it changes the shape it is called the shear stress.

Strain is a measure of the deformation of a solid when stress is applied to it. In the case of deformation in one dimension, strain is defined as the fractional change in length if  $\Delta t$  is the change in length and t is the original length (Fig. 17.3 a) then strain is given by

Strain (
$$\epsilon$$
) = Change in length ( $\Delta \ell$ ) (17.2) Original length ( $\ell$ )

Since strain is ratio of tengths, it is dimensionless, and therefore, has no units. If strain a is due to tensile stress or it is called tensile strain, and if it is produced as a result of compressive stress or it is termed as compressive strain.

In case when the applied stress changes the volume the change in volume per unit volume is known as volumetric strain (Fig. 17.3 b). Thus

Volumetric strain = 
$$\frac{\Delta V}{V_o}$$

Now referring to Fig. 17.3 (c), when the opposite faces of a rigid cube are subjected to shear stress, the shear strain produced is given by

$$\gamma = \frac{\Delta \theta}{\theta} = \tan \theta \tag{17.3}$$

However, for small values of angle  $\theta$ , measured in radian,  $\tan \theta = \theta$ , so that

$$\gamma = 0 \qquad \dots \qquad (17.4)$$

#### Control of the contro

Experiments have revealed that the ratio of stress to strain is a constant for a given material, provided the external applied force is not too great. This ratio is called modulus of elasticity, and can be mathematically described as

Since strain is a dimensionless quantity, the units of modulus of elasticity are the same as those of stress, i.e., Nm² or Pa.

In the case of linear deformation, the ratio of tensile (or compressive) stress  $\sigma$  (= F/A) to tensile (or compressive) strain  $\varepsilon = \Delta t/t$  is called Young 5 modulus

$$Y : \frac{F_{/A}}{\Delta^{r}_{//}} \qquad (17.6)$$

For three dimensional deformation, when volume is involved, then the ratio of applied stress to volumetric strain is called Bulk modulus.

$$K = \frac{F_A}{\Delta V_V} \qquad (17.7)$$

where  $\Delta V$  is the change in original volume V.

However when the shear stress  $\tau = (F/A)$  and shear strain  $\gamma (= \tan \theta)$  are involved, then their ratio is called shear modulus

$$G = \frac{F_{/A}}{\tan \theta} \tag{17.8}$$

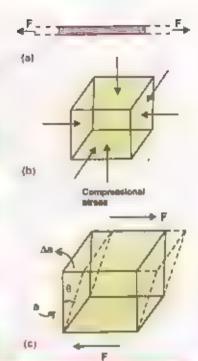
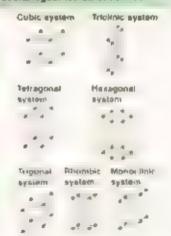


FIG 17 3

- atWire builed along its length by stretching force F
- Cylinder subjected to compressive force F
- . Cube subjected to shearing force F

#### ( For Your Information ...)

There are seven different crystals systems based on the geometrical arrangement of their atoms and the resultant geometrical structures.



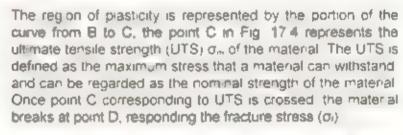
Elastic constants for some of the materials are given in Table 17.1.

Table17 1 Elastic constants for some materials

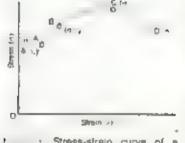
Material	Young's Modulus	Modulus Modulus	Shear Moderals
	ED MIN	TO CHILI	THE CHITE
Aluminum	70	70	30
Bone	15		80
Brass	g1	.61	36
Concrete	25		*
Copper	110	140	44
Diamond	1120	540	450
Giass	55	31	23
Ice	14	8	3
Lead	5	7.7	56
Mernury	0	27	0
Stoel	200	160	84
Tungsten	390	200	150
Water	0	2.2	0

In a tensile test, metal wire is extended at a specified deformation rate and stresses generated in the wire during deformation are continuously measured by a suitable electronic device fitted in the mechanical testing machine. Force-elongation diagram or stress-strain curve is plotted automatically on X-Y chart recorder. A typical stress-strain curve for a ductile material is shown in Fig. 17.4.

In the initial stage of deformation, stress is increased linearly with the strain till we reach point A on the stress-strain curve. This is called proportional limit (o<sub>b</sub>) It is defined as the greatest stress that a material can endure without losing straight line proportionality between stress and strain. Hooke's law which states that the strain is directly proportional to stress is obeyed in the region OA. From A to B stress and strain are not proportional but nevertheless if the load is removed at any point between O and B, the curve will be retraced and the material will return to its original length. In the region OB, the materia is said to be elastic. The point B is called the yield point. The value of stress at B is known as elastic limit o. If the stress is increased beyond the yield stress or elastic limit of the material the specimen becomes permanently changed and does not recover its original shape or dimension after the stress is removed. This kind of behaviour is called plasticity.



Substances which undergo plastic deformation until they break are known as ductile substances. Lead copper and wrought iron are ductile. Other substances which break just after the elastic limit is reached are known as brittle substances. Glass and high carbon steel are brittle.



Stress-strain curve of a hypical ductile material

Example 17.1: A steel wire 12 mm in diameter is fastened

to a log and is then pulled by tractor. The length of steel wire between the log and the tractor is 11 m. A force of 10,000 N is required to pull the log. Calculate (a) the stress in the wire and (b) the strain in the wire. (c) How much does the wire stretch when the log is pulled? ( $E = 200 \times 10^9 \, \text{Nm}^3$ )

#### Solution:

(a) As tensile stress 
$$\sigma = \frac{F}{A} = \frac{10,000 \text{ N}}{3.14 \times (6 \times 10^{-3} \text{ m})^2}$$
  
= 88.46 × 10° Nm<sup>2</sup> = 88.46 MPa

(b) The tensile strain ε = 
$$\frac{\Delta \ell}{\ell}$$

Also 
$$E = \frac{\text{Stress}}{\text{Strain}} = \frac{88.46 \times 10^6 \text{ Nm}^{-2}}{\text{Strain}} = 200 \times 10^9 \text{ Nm}^{-2}$$

Strain = 
$$\frac{88.46 \times 10^6 \text{ Nm}^{-2}}{200 \times 10^9 \text{ Nm}^{-2}} = 4.4 \times 10^{-4}$$

(c) Now using the relation Strain = 
$$\frac{\Delta \ell}{\ell}$$
, we get

 $\Delta \ell = 4.4 \times 10^4 \times 11 \text{ m} = 4.84 \times 10^3 \text{ m} = 4.84 \text{ mm}$ 

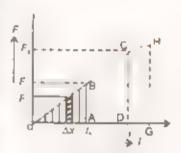
#### State Energy Deformed Mate

Consider a wire suspended vertically from one end. It is stretched by attaching a weight at the other end. We can increase the stretching force by increasing the weight. By noting the extension  $\ell$  of the wire for different values of the stretching force F, a graph can be drawn between the force F and the extension  $\ell$  (Fig. 17.5). If the elastic limit is not exceeded the extension is directly proportional to force F as the force F stretches the wire, it does some amount of work on wire which is equal to product of force F and the extension  $\ell$ . Suppose we are required to find the amount of the work done when the extension is  $\ell$ . Let the force for this extension be  $F_1$ , Fig.17.5 shows that the force F does not remain constant in producing the extension  $\ell$ , it values uniformly from 0 to F, in such a situation the work is calculated by graphical method

Suppose at some stage before the extension  $\ell$  is reached, the force in the wire is F and that the wire now extends by a very small amount  $\Delta x$ . The extension  $\Delta x$  is so small that the force F may be assumed constant in  $\Delta x$ , so the work done in producing this small extension is  $F \times \Delta x$ . In the figure it can be



This is a machine used to investigate the way the national of a material varies with the force stretching it.



Energy in stretched wire Fig. 1 - 5

seen that it is represented by the area of the shaded strip. In this way the total extension  $\ell$ , can be divided into very small extensions and the work done during each of these small extensions would be given by the area of the strips (Fig. 17.5). So the total work done in producing the extension  $\ell$  is the sum area of all these strips which is equal to area between the graph and the axis on which extension has been plotted upto  $\ell$ = $\ell$ . In this case it equals to area of the triangle OAB.

Work done = Area of 
$$\triangle OAB$$
  
=  $\frac{1}{2} OA \times AB$   
=  $\frac{1}{2} \iota_{,x} F_{t}$  (17.9)

This is the amount of energy stored in the wire. It is the gain in the potential energy of the molecules due to their displacement from their mean positions. Eq. 17.9 gives the energy in joules when Fis in newton and & in metres.

Eq 17.9 can also be expressed in terms of modulus of elasticity *E*. If *A* is the area of cross-section of the wire and *L* its total length then

$$E = \frac{F_1}{A} \times \frac{L}{\ell_1}$$
$$F_1 = \frac{EA \times \ell_1}{\ell_1}$$

or

Substituting the value of F, in Eq. 17.9 we have

Workdone = 
$$\frac{1}{2} \left[ \frac{EA \times I_{\star}^{2}}{L} \right]$$
 (17.10)

The area method is quite a general one. For example, if the extension is increased from 4, to 4, the amount of work done by the stretching force would be given by the area of the trapezium ABCD (Fig. 17.5). It is also valid for both the linear (elastic) and the non-linear (non-elastic) parts of the force-extension graph. If the extension occurs from O to G (Fig. 17.5), this work done would be the area of OHG.

#### 17.3 ELECTRICAL PROPERTIES OF SOLIDS

The fundamental electrical property of a solid is its response to an applied electric field, i.e. its ability to conduct electric current. The electrical behaviours of various materials are

diverse. Some are very good conductors, e.g., metals with conductivities of the order of 10° (Ωm). At the other extreme, some solids, e.g., wood, diamond etc., have very low conductivities ranging between 10° and 10° (Ωm)°, these are called insulators. Solids with intermediate conductivities, generally from 10° to 10° (Ωm)°, are termed semiconductors, e.g., suicon germanium etc. The conventional free electron theory based on Bohr model of electron distribution in an atom failed to explain completely the vast diversity in the electrical behaviour of these three types of materials.

On the other hand, energy band theory based on wave mechanica model has been found successful in resolving the problem

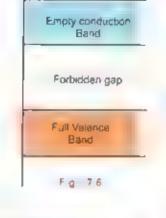


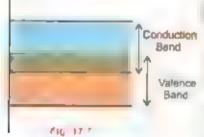
Glass is also known as solid liquid because its molecules are irregularly arranged as in a liquid but fixed in their relative positions.

#### Energy Band Theory

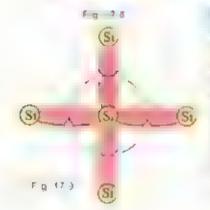
Electrons of an isolated atom are bound to the nucleus, and can only have distinct energy levels. However, when a large number of atoms, say N, are brought close to one another to form a solid, each energy level of the solated atom splits into N sub-levels, called states, under the action of the forces exerted by other atoms in the solid. These permissible energy states are discrete but so closely spaced that they appear to form a continuous energy band. In between two consecutive permissible energy bands, there is a range of energy states which cannot be occupied by electrons. These are called forbidden energy states, and its range is termed as forbidden energy gap.

The electrons in the outermost shell of an atom are called valence electrons and the energy band occupying these electrons is known as valence band. It is obviously the highest occupied band. It may be either completely filled or partially filled with electrons and can never be empty. The band above the valence band is called conduction band. In conduction band, electrons move freely and conduct electric current through solids. That is why the electrons occupying this band are known as conductive electrons or free electrons. Any electron leaving the valence band is accommodated by this band. It may be either empty or partially filled with electrons. The bands below the valence band are normally completely filled and as such play no part in the conduction process. Thus, while discussing the ejectrical conductivity we will consider only the valence and conduction bands









Insulators are those materials in which valence electrons are bound very tightly to their atoms and are not free. In terms of energy bands, it means that an insulator, as shown in Fig. 17.6 has

- a) an empty conduction band (no free electrons)
- a full valence band
- a large energy gap (several eV) between them

Conductors are those which have plenty of free electrons for electrical conduction. In terms of energy bands, conductors are those materials in which valence and conduction bands largely overlap each other (Fig 17.7). There is no physical distinction between the two bands which ensures the availability of a large number of free electrons.

Semiconductors | In terms of energy bands, semiconductors are those materials which at room temperature have

(i) partially filled conduction band (ii) partially filled valence band (iii) a very narrow forbidden energy gap (of the order of 1 eV) between the conduction and valence bands (Fig. 17.8)

At 0 K there are no electrons in the conduction band and their valence band are completely filled. It means at 0 K a piece of Ge or SI is a perfect insulator. However, with increase in temperature, some electrons posses sufficient energy to jump across the small energy gap from valence to conduct on band. This transfers some free electrons in the conduction bands and creates some vacancies of electrons in the valence band. The vacancy of electron in the valence band is known as a hole. It behaves like a positive charge. Thus at from temperature. Ge or Si crystal becomes a semiconductor.

A semi-conductor in its extremely pure form is known as intrinsic semi-conductor. The electrical behaviour of semi-conductor is extremely sensitive to the purity of the material it is substantially changed on introducing a small amount of impurity into the pure semi-conductor attice. The process is called doping in which a small number of atoms of some other suitable elements are added as impurity in the ratio of 1 to 10. The doped semi-conducting materials are called extrinsic semi-conductors.

Pure element of silicon and germanium are Intrinsic

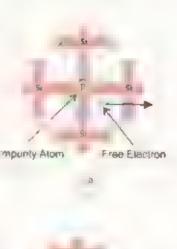
semi-conductors. These semi-conductor elements have atoms with four valence electrons. In solid crystalline form, the atoms of these elements arrange themselves in such a pattern that each atom has four equidistant neighbours. Fig 17.9 shows this pattern along with its valence electrons. Each atom with its four valence electrons shares an electron from its neighbours. This effectively allocates eight electrons in the outermost shell of each atom which is a stable state. This sharing of electrons between two atoms creates covalent bonds. Due to these covalent bonds electrons are bound in their respective shells.

When a stillion crystal is doped with a pentavalent element, e.g. arsenic antimony or phosphorous etc. four valence electrons of the impunity atom form covalent bond with the four neighbouring Si atoms while the fifth valence electron provides a free electron in the crystal. Such a doped or extrinsic semi-conductor is called n-type semi-conductor. Fig. 17.10(a) Illustrates silicon crystal attice doped with a pentavalent impurity such as phosphorous. The phosphorous atom is called a donor atom because it read by donates a free electron, which is thermally excited into the conduction band.

On the other hand, when a silicon crystal is doped with a trivalent element, e.g., aluminium, boron, gellium or indium etc., three valence electrons of the impurity atom form covalent bond with the three neighbouring Si atoms while the one missing electron in the covalent bond with the fourth neighbouring Si atom, is called a hole which in fact is vacancy where an electron can be accommodated. Such a semi-conductor is called p-type semi-conductor Fig. 17-10 (b) islustrates silicon crystal lattice doped with aluminium. The aluminium atom is called an acceptor atom because it is easy for the aluminium ion core to accept a valence electron from a nearby silicon atom, thus creating a hole in the valence bond.



Consider a semi-conductor crystal lattice, e.g., Ge or Si as shown in F.g. 17.11. The circles represent the positiveion cores of Si or Ge atoms, and the blue dots are valence electrons. These electrons are bound by covalent bond. However, at room temperature they have thermal kinetic motion which in case of some electrons, is so vigorous that



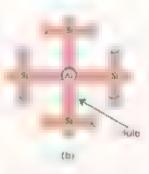
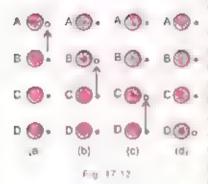
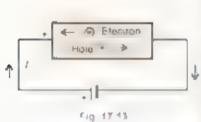


Fig. 17 10



Fg 17 11







the covalent bond is unable to keep them bound. In such cases the electrons break the covalent bond and get themse ves free leaving a vacant seat for an electron, e, a hole. Thus whenever a covalent bond is broken, an electron-hole pair is created. Both the electrons and the holes move in the semi-conductor crystal lattice as explained below.

Consider a row of Si atoms in crystal attice. Suppose a hole. is present in the valence shell of atom A. As hole is a deficiency of electron, so the core of atom Awould have a net positive charge (Fig. 17, 12 a). This attracts an electron from a neighbouring atom say B. Thus the electron moves from 8 to A and the hore (+ve charge) shifts to B (Fig. 17, 12 a b). Now an electron is attracted from C to B and a hole is created at C (Fig. 17.12 b.c) and positive charge appears at C This process is repeated between the atoms C and D with the result that the electron moves from D to C and the hole (+ve charge) appears at D (Fig. 17.12 c,d). Thus we notice that if a hole is present in any valence shell, it cannot stay there but it moves from one atom to other with the electron moving in opposite direction. Secondly we notice that the appearance of hole is accompanied by a positive charge Thus a moving he elis aguiya ant to a movir gipositive charge.

In this example we have considered a special case in which the electron and the hole are moving in a straight line. Actually their motion is random because positively charged core of the atom can attract an electron from any of its neighbouring atoms.

Thus in semi-conductors there are two kinds of charge carriers, a free electron (-e) and a hole (+e)

When a battery is connected to a semi-conductor, it establishes an electric field across it due to which a directed flow of electrons and holes takes place. The electrons drift towards the positive end whereas the holes drift towards the negative end of the semi-conductor (Fig. 17-13). The current / flowing through the semi-conductor is carried by both electrons and holes it may be noted that the electronic current and the hole current add up together to give the current /.

#### 17.4 SUPERCONDUCTORS

There are some materials whose resistivity becomes zero below a certain temperature *T* called critical temperature as shown in resistivity-temperature graph in Fig. 17.14. Below this temperature such materials are called superconductors

They offer no resistance to electric current and are, therefore, perfect conductors. Once the resistance of a material drops to zero, no energy is dissipated and the current, once established, continues to exist indefinitely without the source of an emf

The first superconductor was discovered in 1911 by Kmaerlingh Ornes when it was observed that electrical resistance of mercury disappears suddenly as the temperature is reduced below 4.2 K. Some other metals such as aluminium (T, =1.18 K), tin (T  $\div$ 3.72 K), and lead (T,  $\Rightarrow$ 7.2 K) also become superconductors at very low temperatures. In 1986 a new class of ceramic materials was discovered that becomes superconductor at temperatures as high as 125 K. Any superconductor with a critical temperature above 77 K the boiling point of liquid nitrogen is referred as a high temperature superconductor.

Recently a complex crystaline structure known as Yttrium barium copper oxide (YBa,Cti, O.) have been reported to become superconductor at 163 K or -110 °C by Prof Yao Lian's Lee at Cambridge University Perhaps one day even room temperature superconductor will be developed and that day will be a new revolution in electrical technologies. Superconductors have many technological applications such as in magnetic resonance imaging (MRI). magnetic levitation trains, powerful but small electric motors and faster computer chips



Super conductors are alloys that at certain temperatures, conduct electricity with no resistance





Magnetic Resonance imaging MRI uses, strong magnetic field at wair ed. by super conducting maintains for scanning computer processing produces the mage identifying turnura and inflamed issues

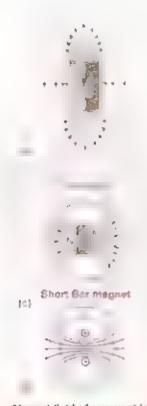
#### 17.5 MAGNETIC PROPERTIES OF SOLIDS

From the study of the magnetic fields produced by bar magnets and moving charges, i.e., currents, it is possible to trace the origin of the magnetic properties of the material. It is observed that the field of a long bar magnet is like the field produced by a long solenoid carrying current and the field of a short bar magnet resembles that of a single loop (Fig 17 15). This similarity between the fields produced by magnets and currents urges an enquiring mind to think that ali magnetic effects may be due to circulating currents (i.e., moving charges) a view first held by Ampere. The idea was not considered very favourably in Ampere's time because the structure of atom was not known at that time. Taking into consideration the internal structure of atom discovered thereafter, the Ampere's view appears to be basically correct

The magnetism produced by electrons within an atom can



Long Bar magnet



Magnet field of a current loop. Fig. 17-15



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arise from two motions. First, each electron orbiting the nucleus behaves like an atomic sized loop of current that generates a small magnetic field, this situation is similar to the field created by the current loop in Fig 17.15 (d), Secondly each electron possesses a spin that also gives rise to a magnetic field. The net magnetic field created by the electrons within an atom is due to the combined field created. by their orbital and spin motions. Since there are a number of electrons in an atom, their currents or spins may be so or ented or aligned las to cance, the magnetic life of multiplies or strengthen the effects of each other. An air min which there is a resultant magnetic field, behaves like a tiny magnet and is called a magnetic dipole. The magnetic fields of the atoms are responsible for the magnetic behaviour of the substance made up of these atoms. Magnetism is therefore, due to the soin and orbital motion of the electrons surrounding the nucleus and is thus a property of all substances. It may be mentioned that the charged nucleus itself spins giving use to a magnetic field. However, it is much weaker than that of the orbital electrons. Thus the source of magnetism of an atom is the electrons. Accepting this view of magnetism it is concluded that it is impossible to obtain an isolated northpole. The north-pole is merely one side of a current loop. The other's de will always be present as a south pulp and these cannot be separated. This is an experimental reality.

Two cases arise which have to be distinguished. In the first case, the orbits and the spin axes of the electrons in an atom are so oriented that their fields support each other and the atom behaves like a tiny magnet. Substances with such atoms are called paramagnetic substances. In second type of atoms there is no resultant field as the magnetic fields produced by both orbital and spin motions of the electrons might add upto zero. These are called diamagnetic substances for example the atoms of water cupper to smoth and antimony.

However, there are some solid substances e.g. Fa, Co, Ni, Chromium dioxide, and Alnico (an iron aluminium - nickel - cepa l alloy) in which the atoms co-operate with each other in such a way so as to exhibit a strong magnetic effect. They are called ferromagnetic substances. Ferromagnetic materials are of great interest for electrical engineers.

Recent studies of ferromagnetism have shown that there exists in ferromagnetic substance small regions called 'domains' The domains are of macroscopic size of the order

of mitimetres or less but large enough to contain 10 to 10 atoms. Within each domain the magnetic fields of all the spinning electrons are parallel to one another i.e., each domain smagnetized to saturation. Each domain behaves as a small magnet with its own north and south potes. In unmagnetised iron the domains are oriented in a disorderly fashion (Fig.17.16), so that the net magnetic effect of a sizeable specimen is zero. When the specimen is placed in an external magnetic field as that of a solenoid, the domains make up parallel to lines of external magnetic field and the entire is specimen, becomes saturated (Fig.17.17). The combination of a solenoid and a specimen of iron inside it thus makes a powerful magnetiand is called an electromagnet.

Iron is a soft magnetic material, its domains are easily oriented on applying an external field and also read ly return to random positions when the field is removed. This is desirable in an electromagnet and also in transformers. Domains in steel, on the other hand, are not so easily oriented to order. They require very strong external fields but once oriented retain the aignment. Thus steel makes a good permanent magnet and is known as hard magnetic material and another such material is a special alloy Alnico V.

Finally, it must be mentioned that thermal vibrations tend to disturb the orderliness of the domains. Ferromagnetic materials preserve the orderliness at ordinary temperatures. When heated they begin to lose their orderliness due to the increased thermal motion. This process begins to occur at a particular temperature, different for different materials, called Curie temperature. Above the Curie temperature iron is paramagnetic but not ferromagnetic. The Curle temperature for iron is about 750 °C.

# Hystorocistcoop

To investigate a ferromagnetic material, a bar of that material such as ron is placed in an alternating current solenoid. When the alternating current is at its positive peak value, it fully magnetises the specimen in one direction and when the current slat its negative peak, it fully magnetises it in opposite direction. Thus as the alternating current changes from its positive peak value to its negative peak value and then back to its positive peak value, the specimen undergoes a complete cycle of magnetization. The flux density versus the magnetization current of the specimen for the vanous values of magnetizing current of the sole, old is clotted by a CRO (Fig. 17-18).



Magnetic domains within an unmagnetized fortomagnet







its main features are as follows:

The portion of OA of the curve is obtained when the magnetizing current is increased and AR is the portion when the current is decreased it may be noted that the value of flux density for any value of current is always greater when the current is decreasing than when it is increasing. Let, magnetism lags behind the magnetizing current. This phenomenon is known as hysteresis.



The magnetic flux density increases from zero and reaches a maximum value. At this stage the material is said to be magnetically saturated.



When the current is reduced to zero, the material still remains strongly magnetized represented by point R on the curve. It is due to the tendency of domains to stay parily in line, once they have been aligned.

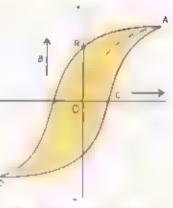


To demagnetize the material the magnetizing current is reversed and increased to reduce the magnetization to zero. This is known as coercive current represented by C on the curve. The coercivity of steel (Fig. 17.19 a), is more than that of ron as more current is needed to demagnetize it. Once the material is magnetized its magnetization curve never passes through the origin. Instead it forms the closed loop ACDC A, which is called hysteresis loop.

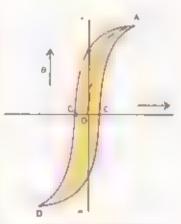


The area of the loop is a measure of the energy needed to magnetize and demagnetize the specimen during each cycle of the magnetizing current. This is the energy required to do work against internal friction of the domains. This work, like all work that is done against friction is dissipated as heat. It is called hysteresis loss.

Hard magnetic materials like steel can not be easily magnetized or demagnetized so they have large loop area as compared to soft magnetic material such as iron which can easily be magnetized. The energy dissipated per cycle, thus, for iron is less than for steel.



Hystereets loop of steel



b) Hysteresis loop of soft from

OR = Retentivity

OC = Coercivity

Fig. 17-19

Suitability of magnetic materials for different purposes can be studied by taking the specimen through a complete cycle and drawing the hysteresis loop. A material with high retentivity and large coercive force would be most suitable to make a permanent magnet. The cores of electromagnets used for alternating currents where the specimen repeatedly undergoes magnetization and demagnetization should have narrow hysteresis curves of small area to minimize the waste of energy.



A builer train is affect above the ralis due o magnetic effect thus friction is reduced to minimum and speed can be enhanced up to 500kmh.



- Crystail ne solids are those in which there is a regular arrangement of molecules.
   The neighbours of every molecule are arranged in a regular pattern that is constant throughout the crystai. Thus, there is an ordered structure in crystaline solids.
- n amorphous sol ds there is no regular arrangement of molecules. These are more
  like liquids with the disordered structure frozen in
- Polymers may be said to be more or less solid materials with a structure that is intermediate between order and disorder. These can be classified as partially or poorly crystaltine solids.
- A crystal me so id consists of three dimens anal pattern that repeats itself over and over again. This basic structure is called unit cell
- The force applied on unit area to produce any change in the shape ivolume or length of a body is called stress.
- When a long wire of length \( \ell \) with area of cross section \( A \) is being pulled by a force \( F \)
  which results in an increase in length \( \ell \) the stress is called tensile deformation.
- When a small cylinder is subjected to a force Flalong the inward drawn normal to its
  area of cross section A to reduce its length, the stress is called compressive stress
  and deformation produced by it is called compressive deformation.
- If a force F is applied tangent ally to the surface of the opposite face of a cube to deform or twist, it through an angle θ, the stress is termed as shear stress.
- Strain is a measure of the deformation of a solid when stress is applied to it. In the
  case of deformation in one dimension, strain is defined as the fractional change in
  length per unit length. If strain is due to tensile stress it is called tensile strain and if it
  is produced as a result of compressive stress it is termed as compressive strain.
- The ratio of stress to strain is a constant for a given material provided the external
  applied force is not too great. This is called clodulus of elasticity.
- The strain energy can be obtained by the area of the force-extension graph.
- The electrical behaviour of semi-conductor is substantially changed on introducing.

a small amount of impurity into the pure semi-conductor fattice. The process is called doping in which a small number of atoms of some other suitable elements are added as impurity. The doped semi-conducting materials are called extrinsic.

- When a silicon crystal is doped with a pentavalent element, four valence electrons of the impurity atom form covalent bond with the neighbouring S, atoms, while the fifth valence electron provides a free electron in the crystal. Such a doped or extrinsic semi-conductor is called n-type semi-conductor.
- There are some materials whose resistivity becomes zero below a certain temperature T called critical temperature. Below this temperature, such materials are called superconductors.
- Substances in which the orbits and the spin axes of the electrons in an atom are so
  oriented that their magnetic fields support each other and the atom behaves like a
  tiny magnetiare called paramagnetic substances
- The substances in which magnetic fields produced by orbital and spin molecules of the electrons add up to zero are called diamagnetic substances.
- Substances in which the atoms co-operate with each other in such a way so as
  to exhibit a strong magnetic effect are called ferromagnetic

#### QUESTIONS

- 17.1 Distinguish between crystalline, amorphous and polymeno solids
  - 17. Define stress and strain. What are their SI units? Differentiate between tensile compressive and shear modes of stress and strain.
- 17.3 Define modulus of elasticity. Show that the units of modulus of elasticity and stress are the same. Also discuss its three kinds.
  - 17.4 Draw a stress-strain curve for a ductive material, and then define the terms. Elastic limit. Yield point and Ultimate tensile stress.
  - 17.5 What is meant by strain energy? How can it be determined from the force-extension graph?
  - 17.6 Describe the formation of energy bands in solids. Explain the difference amongst electrical behaviour of conductors insulators and semi-conductors in terms of energy band theory.
- 17.7 Distinguish between intrinsic and extransic semi-conductors. How would you obtain in-type and p-type material from pure silicon? Itustrate it by schematic diagram.
- 17.8 Discuss the mechanism of electrical conduction by holes and electrons in a pure semi-conductor element.
- 17.9 Write a note on superconductors
- 17.10 What is meant by paralidia and ferromagnetic substances? Give examples for each
- 7.11 What is meant by hysteresis loss? How is it used in the construction of a transformer?



- 17.1 A 1.25 cm diameter cylinder is subjected to a load of 2500 kg. Calculate the stress on the bar in mega pascals. (Ans.: 200 MPa)
- 17.2 A 1.0 m ong copper wire is subjected to stretching force and its length increases by 20 cm. Calculate the tensile strain and the percent elongation which the wire undergoes. (Ans: 0.20, 20%)
- A wire 2.5 m long and cross-section area 10° m² is stretched 1.5 mm by a force of 100 N in the elastic region Calculate (i) the strain (ii) Young's modulus (ii) the energy stored in the wire (Ans: 6.02 x 10°, 1.66 x 10°Pa, 7.5 x 10°J)
- 17.4 What stress would cause a wire to increase in length by 0.01% if the Young's modulus of the wire is 12 x 10.9 Pa. What force would produce this stress if the diameter of the wire is 0.56 mm?

  (Ans. 1.2 x 10.9 Pa. 2.96 N)
- 17.5 The length of a steel wire is 1.0 m and its cross-sectional area is 0.03 x 10 m². Calculate the work done in stretching the wire when a force of 100 N is applied within the elastic region. Young's modulus of steel is 3.0 x 10° Nm². (Ans: 5.6 x 10° J).

# Chapter 18

# **ELECTRONICS**

# **Learning Objectives**

At the end of this chapter the students will be able to:

- Describe forward and reserve biasing of a p-n junction.
- 2 Understand half and full wave rectification.
- 3 Know the uses of light emitting diode, photo diode and photo voltaic ce I
- 4 Describe the operation of transistor.
- 5 Know current equation and solve related problems.
- onderstand the use of transistors as an ampillier and a switch
- 7 Understand operational amplifier and its characteristics
- 8 Know the applications of an operational amplifier as inverting and non-inverting amplifier using virtual ground concept.
- 9 Understand the use of an operational amplifier as a comparator eight switch
- Understand the function of each of the following ogic gates AND NOT OR and NAND gates and represent their functions by means of truth tables (I mited to a maximum of two inputs)
  - Describe how to combine different gates to form XOR and XNOR gates. Understand combinations of logic gates to perform control functions.

he huge advances in electron is over the recent past are due to discovery and use of semi-conductors. Sixon is one of the most commonly used semi-conductors, and is the basic material from which highly sophisticated integrated circuits known as 'chips are made. The use of chips in analogue as well as in digital electron is sidescribed in the form of the black boxes. This chapter is based on the preliminary concepts introduced in the secondary school physics course.

# 18.1 BRIEF REVIEW OF p-n JUNCTION AND ITS CHARACTERISTICS

Ap-n junction is formed when a crystal of germanium or silicon is grown in such a way that its one half is doped with a trivalent impurity and the other half with a pentavalent impurity. One of the most important building blocks of electronic devices is the p-n unction. Its n-region contains free electrons as majority charge camers and p-region contains holes as majority charge camers and p-region contains holes as majority charge camers and p-region contains holes as majority charge camers and p-region in the n-region because of their random motion diffuse into the pinegion. As a result of this diffusion a region is formed around the unction in which charge carriers are not present. This region is known as depict on region. Fig. 18.1 a. in this figure, blue dots represent the free electrons and the small circles show the holes whereas the circles with + and - signs show the positive and negative ions which constitute the depiction region. Due to charge on

these ions a potential difference develops across the depletion region (Fig.18.1 b). Its value is 0.7 V in case of silicon and 0.3 V in case of germanium. This potential difference called potential barrier, stops further diffusion of electrons into the p-region

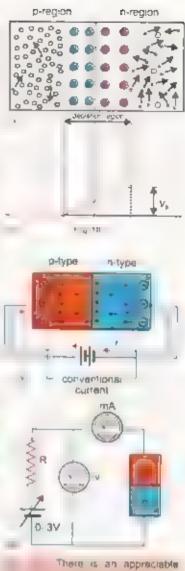
When an external potential difference is applied across a p-n junction such that p-side is positive and n-side is negative then this external potential difference supplies energy to free electrons in the n-region and to holes in p-region. When this energy is sufficient to overcome the potential barrier a current of the order of a few miliamperes begins to flow across the p-n junction. In this state the p-n junction is said to be forward biased (Fig. 18.2 a). The variation of current through the junction with the bias voltage can be studied by the circuit shown in Fig. 18.2 (b). The value of current for different values of bias voltage is noted and a current-bias voltage graph is plotted. Fig. 18.3 shows the graph for all typical low power silicon diode.

As shown in Fig. 18.3 if forward bias voltage is increased by  $\Delta V$  the current increases by  $\Delta I$ . The ratio  $\Delta V_i/\Delta I_i$  is known as forward resistance of the p-n junction, i.e.

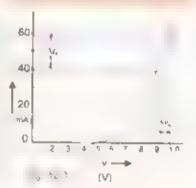
$$r_i = \frac{\sqrt{V}}{\Delta f_i} \qquad \dots \dots \dots \qquad (18.1)$$

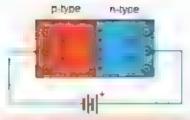
It is the resistance offered by the p-n junction when it is conducting. The value of r, is only a few ohms.

When the external source of voltage is applied across a p-n junction such that its positive terminal is connected to n-region and its negative terminal to p-region, the p-n junction is said to be reverse blased (Fig. 18.4). In this situation no current flows due to the majority charge carries. However a very small current of the order of few microamperes flows across the junction due to flow of minority charge carriers (Fig. 18.4). It is known as reverse current or leakage current. The variation of reverse current with the applied bias voltage can be studied by the circuit shown in Fig. 18.5. Fig. 18.6 shows the reverse characteristic for the p-n junction. It can be seen that as the reverse voltage is increased from 0, the reverse current quickly rises to its saturation value I<sub>c</sub>. As the reverse voltage is further increased, the reverse current

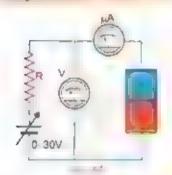


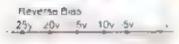
There is an appreciable current through he diode when the diode showard biased

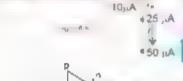


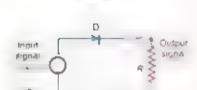


f Inder a reversed brased condition there is almost no current through he diode.











remains almost constant. Here the resistance offered by the diode is very high - of the order of several mega ohms

As the reverse voltage is increased, the kinetic energy of the minority charge carriers with which they cross the depiet on region also increases till it is sufficient to break a covalent bond. As the covalent bond breaks, more electron-hole pairs are created. Thus, immority charge carriers begin to multiply due to which the reverse current begin to increase till a point is reached when the junction breaks down and reverse current uses sharply (Fig. 18.6). After breakdown the reverse current will rise to very high value which will damage the junction.

P-n junction is also known as a semi-conductor diode whose symbolic representation is given in Fig. 18.7. The arrow head represents the pinegion and is known as anode. The vertical line represents the ninegion and is known as cethode. The current flows in the direction of arrow when the diode is forward biased.

#### 18.2 RECTIFICATION

Conversion of alternating current into direct current is called rectification. Semi-conductor diodes are extensively used for this purpose. There are two very common types of rectification.

Half-wave rectification and

Full wave rectification

A half-wave rectification is shown in Fig. 18.8 where an atternating voltage of period T called input voltage is applied to a diode D which is connected in series with a load resistance R. In this method only one half of alternating current cycle is converted into direct current.

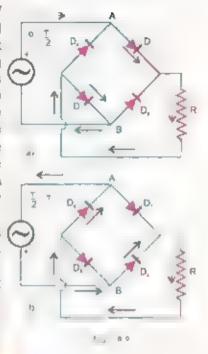
During the positive half cycle of the input alternating voltage i.e. during the interval  $0 \rightarrow T/2$ , the diode D is forward biased, so it offers a very low resistance and current flows through R. The flow of current through R causes a potential drop across it which varies in accordance with the alternating input (Fig. 18.8 c).

During the negative half cycle e during the period T/2 + T the diode is reverse biased. Now it offers a very high resistance, so practically no current flows through R and potential drop across it is almost zero (Fig. 18.8 c). The same events repeat during the next cycle and so on. The current through R flows in only one direction which means it is a direct current. However, this current flows in pulses (Fig. 18.8 c). The

voltage which appears across load resistance R is known as output voltage

#### **Full-Wave Floatification**

We have seen that in a half wave rectification, only one half of the alternating input voitage is used to send a unidirectional current through a resistance. However both haives of the input. voltage cycle can be utilized using full-wave rectification. Its circuit consists of four diodes. connected in a bridge type arrangement (Fig. 189). To understand the operation of the circuit, recall that a diode conducts only when it is forward biased. During the positive haif cycle, i.e. during the time 0 > 7/2, the terminal A of the bridge is positive with respect to its other terminal B. Now the diodes D, and D, become forward biased and conduct. A current flows through the circuit in the direction shown by arrows in Fig. 18.9 (a). During the negative half cycle, i.e., during the time interval 7/2 + 7 termina Ais negative and Bis f positive. Now the diodes D, and D, conduct and current flows. through the circuit in the path shown by arrows in Fig. 18.9 (b). By companing Figs. 18.9 (a) and 18.9 (b), it can be seen that direction of current flow through the load resistance R is the same in both the halves of the cycle. Thus both halves of the alternating input voltage send a unidirectional current through R. The Input and output voltages are shown in Fig. 18.10. However the output voitage is not smooth but pulsating. It can be made smooth by using a circuit known as filter



#### 18.3 SPECIALLY DESIGNED p-n JUNCTIONS

In addition to the use of semi-conductor diode as rectifier, many types of p-n junctions have been developed for special purposes. Three most commonly used such diodes are

- (i) Light emitting diode
- (II) Photo diode
- (i i) Photo voltaic cell

### **Light Crititing Disab**

Light emitting diodes (LED) are made from special semi-conductors such as gallium arsenide and gallium arsenide phosphide in which the potential barrier between pland in sides is such that when an electron combines with a hole during forward bias conduction, a photon of visible light is eight ted. These diodes are commonly used as small light

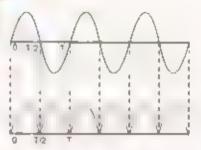


Fig. 6 G

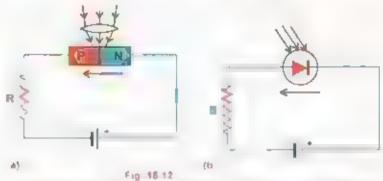


Fig. 18 11

sources. A specially formed array of seven LED's is used for displaying digits etc., in electronic appliances (Fig. 18.11).



Photo diode is used for the detection of light, it is operated in the reverse biased condition (Fig. 18.12 a). A photo diode symbol is shown in Fig. 18.12 (b). When no light is incident



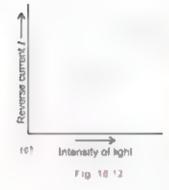
on the junction the reverse current / is almost negligible but when its p-n junction is exposed to light the reverse current increases with the intensity of light (Fig 18.12 c).

A photo diode can turn its current ON and OFF in nano-seconds Hence it is one of the fastest photo detection devices Applications of photo diode include

- Detection of both visible and invisible radiations
- I Automatic switching
- in Logic circuits
- iv. Optical communication equipment etc.

#### Photo-Voltaic Cell

It consists of a thick n-type region covered by a thin p-type layer. When such a p-n junction having no external bias (Fig 18 13) is exposed to light absorbed photons generate electron-hole pairs. It results into an increase percentage of minority charge carriers in both the p and n-regions and when they diffuse close to the junction, the electric field due to junction potential barner sweeps them across the junction it causes a current flow through the external circuit R. The current is proportional to intensity of light.



P Light R Fig. 18, 13

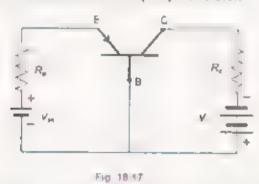
#### 18.4 TRANSISTORS

A transistor consists of a single crystal of germanium or sil con which is grown in such a way that it has three regions (Figs. 18.14 & 18.15).

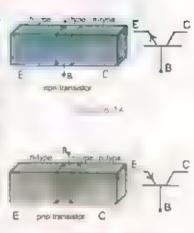
In Fig. 18-14 the central region is pitype which is sandwiched between two nitype regions. It is known as n-p-n transister. In Fig. 18-15, the nitype central region is sandwiched between two pitype regions, it forms a p-n-pitransistor. The central region is known as base and the other two regions are called emitter and collector. Usually the base is very thin, of the order of 10° m. The emitter and collector have greater concentration of impurity. The collector is comparatively larger than the emitter. The emitter has greater concentration of impurity as compared to the collector.

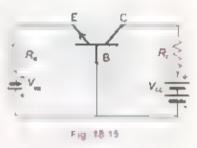
It can be seen in Figs 18 14 and 18 15 that a transistor is a combination of two back to back p-ri junctions, emitter-base junction and collector-base junction.

For normal operation of the transistor batteries  $V_{ta}$  and  $V_{ta}$  are connected in such a way that its emitter-base junction is forward biased and its collector base function is reverse biased  $V_{rr}$  is of much higher value than  $V_{av}$ . Fig. 18 16 shows the biasing arrangement for n-p-n transistor when the transistor has been represented by its symbolic form. Fig. 18.17 shows the same for a p-n-p transistor.



It may be noted that polarities of the biasing batteries  $V_{\rm se}$  and  $V_{\rm re}$  are opposite in the two types of the transistors. In actual practice, it is the n-p-n transistor that is generally used. So we will discuss n-p-n transistors only





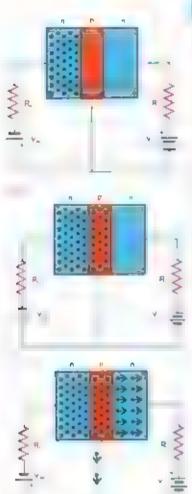
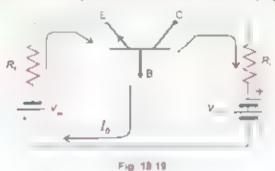


Fig. 18 18 (a) shows a n-p-n transistor at the instant when the biasing voltage is applied. Electrons in the emitter shown by black dots have not yet entered the base region. After the application of the biasing voltage, emitter base junction is forward biased, so emitter injects a large number of electrons in base region (Fig. 18-18-b). These free electrons in the base can flow in either of two directions. They can either flow out of the base to the positive terminal of Ves or they can be attracted towards the collector because of battery Vcc. Since the base is extremely thin, very few electrons manage to recombine with holes and escape out of the base. Almost all of the free electrons injected from the emitter into the base are attracted by the collector due to the large positive potential V., (Fig. 18 18 c). Thus, in a normally biased transistor due to above mentioned flow of electrons, we can say, that an electronic current  $I_{\rm e}$ , flows from the emitter into the base. A very small part of it, current I, flows out of the base, the rest of it /, flows out of the collector (Fig. 18 19).



The flow of conventional current is shown in Fig. 18.20. In future we will use conventional current only. From the figure it can be seen that

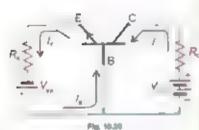
$$I_{\rm h} = I_{\rm c} + I_{\rm 0}$$
 ........... (18.2)

As very few electrons flow out of base, so  $I_a$  is very small as compared to  $I_a$ .

It is also found that for a given transistor the ratio of collector current I<sub>c</sub> to base current I<sub>n</sub> is nearly constant tie...

$$\beta = \frac{I_{\rm C}}{I_{\rm B}} \tag{18.3}$$

The ratio  $\beta$  is called current gain of transistor its value is quite large – of the order of hundreds. Eqs.18.2 and 18.3 are



fundamental equations of all transistors.

Example 18 1: In a certain circuit, the transistor has a collector current of 10 mA and a base current of 40 µA. What is the current gain of the transistor?

Solution:

$$\beta = \frac{I_C}{I_B} = \frac{10 \times 10^{1} \text{ A}}{40 \times 10^{6} \text{ A}} = 250$$

# 18.5 TRANSISTOR AS AN AMPLIFIER

In majority of electronic circuits, transistors are basically used as amplifiers. An amplifier is thus the building block of every complex electronic circuit. It is for this reason that study of transistor amplifier is important.

The circuit in Fig. 18-21 is a transistor voltage amplifier. The battery  $V_{\rm ex}$  forward biases the base-emitter junction and V reverse biases the collector-base junction.  $V_{\rm ex}$  and  $V_{\rm cx}$  are the input and output voltages respectively. The base current is  $I_{\rm ex} = v_{\rm ex}/r_{\rm ex}$  where  $r_{\rm ex}$  is base emitter resistance of the transistor. The transistor amplifies it  $\beta$  times. So

$$I_c = \beta I_e = \beta V_{ee} / r_e$$

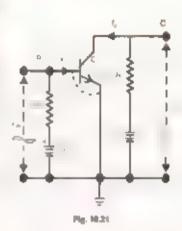
The output voltage  $V_a = V_{c\epsilon}$  is determined by applying KVL equation in the output loop which gives

$$V_{cc} = I_c R_c + V_{ce}$$
 or  $V_{ce} = V_{cc} - I_c R_c$   
Substituting the value of  $I_c$  and replacing  $V_{ce}$  by  $V_c$ 

$$V_a = V_{cc} - \beta V_{cc} R_c/r_c$$
 18.4(a)

When small signal voltage  $\Delta V_e$  is applied at the input termina B, the input voltage changes from  $V_{\rm ec}$  to  $V_{\rm ec}$  +  $\Delta V_e$ . This causes a little change in base current from  $I_{\rm e}$  to  $(I_{\rm e} + \Delta I_{\rm e})$  due to which the collector current changes from I to  $(I_{\rm c} + \Delta I_{\rm e})$ . As the collector current changes, the voltage drop across R<sub>c</sub> i.e.  $(I_{\rm e})$  also changes due to which the output voltage  $V_{\rm e}$  changes by  $\Delta V_{\rm e}$ . Substituting the changed values in Eq. 18.4(a)

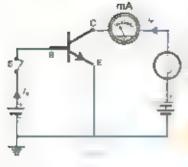
Subtracting Eq. 18 4(a) from Eq. 18.4(b)  $\Delta V_o = -\beta \Delta V_a R_c / r_a$ 

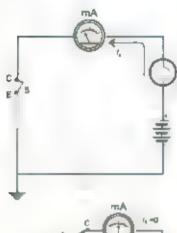


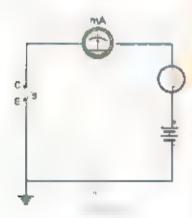
#### Parities internation



Various shapes of frame stors







Therefore the gain of the amplifier  $A = \Delta V_c/\Delta V_c = \beta R_c/r_c$ . The value of the factor  $\beta R_c/r_c$  is of the order of hundreds, so the input voltage is amplified. The negative sign shows that there is a phase shift of 180° between the input and the output signals.

#### 18.6 TRANSISTOR AS A SWITCH

Fig. 18.22 (a) shows the circuit in which a transistor is used as a switch. The collectors C and emitter E behave as the terminals of the switch. The circuit in which the current is to be tuned OFF and ON, is connected across these terminals. The base B and emitter E act as control terminals which decide the state of the switch.

In order to turn on the switch, a potential V, is applied between control terminals B-E (Fig. 18 22 a). This injects a large current /, into the base circuit due to which a very heavy current /, begins to flow in the CE circuit. This large value of collector current is possible only when the resistance between C and E drops down to such a small value that the potential drop across CE is nearly 0.1 volt in Fig. 18.22 (a). emitter is at ground, so we can assume that collector is a soat ground and cohector emitter circuit of Fig. 18,22 (a) can be drawn as shown in Fig. 18 22 (b). CE switch is closed and the bulb glows due to flow of large collector current. To turn the switch OFF the base current I, is set zero by opening the base circuit (Fig. 18.22 c). As  $I_c = \beta I_a$ , so  $I_c$  becomes zero and C-E circuit becomes open (Fig. 18 22 d). Now the resistance between C and E becomes nearly infinity which opens the CE switch.

An electronic computer is basically a vast arrangement of electronic switches which are made from transistors.

#### 18.7 OPERATIONAL AMPLIFIER

As stated earlier, amplifier is an important electronic circuit that is used in almost every electronic instrument. So instead of making amplifier circuit by discrete components, the whole amplifier is integrated on a small silicon chip and enclosed in a capsule. Pins connected with working terminals such as input, output and power supply project outside the capsule (Fig. 18-23 a). The enclosed circuit of the amplifier is used by making requisite connections with these pins. Such an

integrated amplifier is known as operational amplifier (op-amp), as it is some times used to perform mathematical operations electronically

The op-amp is usually represented by its symbol shown in Fig 18.23 (b). It has two input terminals. One is known as inverting input (-) and the other non-inventing input (+). A signal that is applied at the inverting (-) input, appears after amplification, at the output terminal with a phase shift of 180° (Fig. 18.24 a). It can be seen that the signal is inverted as it appears at the output. This is why this terminal is known as inverting. If the signal is applied at non-inverting input (+), it is amplified at the output without any change of phase (Fig. 18.24 b).

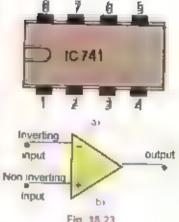
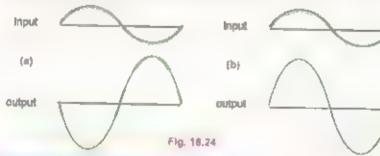


Fig. 18 23





An op-amp has a large number of characteristic parameters. We will discuss only three of them.

Fig. 18.25

It is the resistance between the (+) and (-) inputs of the amp ifier (Fig. 18.25). Its value is very high - of the order of several mega ohms. Due to high value of the input resistance. Re practically no current flows between the two input termina's It is a very important feature of op-amps

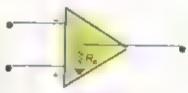
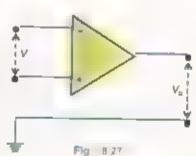


Fig. 18 26

It is the resistance between the output terminal and ground (Fig. 18.26 Its value is only a few ohms.



It is the ratio of output voltage V<sub>c</sub> to the voltage difference between non-inverting and inverting inputs when there is no external connection between the output and the inputs (Fig. 18.27) i.e.,



$$A_{\rm OL} = \frac{V_{\rm o}}{V_{\rm o}} = \frac{V_{\rm o}}{V} \tag{18.5}$$

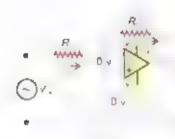


Fig 18 48

The open loop gain of the amplifier is very high. It is of the order of 10°

# 18.8 OP-AMP AS INVERTING AMPLIFIER

Fig. 18 28 shows the circuit of an op-amp when used as an inverting amplifier. The input signa V, which is to be amplified is applied at inverting terminal (-) through a resistance R V is is output. The non-inverting terminal (+) s grounded i.e. its potential is zero. We know that Ao, is v, very high, of the order of 10° As V, may have any value between +V<sub>cc</sub> (+12V) and -V<sub>cc</sub> (-12V) so according to Eq 18.5, for finite (±12V) value of V., V. - V. = 0 or V. = V. Since V is at ground so V is virtually at ground potential i.e., V ≈ 0. Referring to Fig. 18.28.

Current through 
$$R_1 = I_1 = \frac{V_n - V_n - V_n}{R_1} = \frac{V_n}{R_1}$$

Current through  $R_1 = I_1 = \frac{V_n - V_n}{R_2} = \frac{V_n}{R_2} = \frac{V_n}{R_2}$ 

As practically no current flows between (-) and (+) term nals so according to Kirchhoff's current rule

or 
$$\frac{V_{i_1}}{R_i} = -\frac{V_{i_2}}{R_{i_2}}$$
 or  $\frac{V_{i_2}}{V_{i_3}} = -\frac{R_{i_2}}{R_{i_1}}$ 

As  $V_o/V_a$  is defined as gain G of the inverting amplifier, so

$$G = -\frac{R_2}{R_1}$$
 ...... (18.6)

The negative sign indicates that the output's gnatis 180" out of phase with respect to input signal. It is interesting to note that the closed loop gain depends upon the two externally connected resistances R and R. The gain is independent of what is happening inside the amplifier.

If 
$$R_c = 10 \text{ k}\Omega$$
 and  $R_z = 100 \text{ k}\Omega$ , the gain of the amplifier is
$$G = \frac{V_o - R_z}{V - R_z} = 100 \Omega \qquad 10$$

# 18.9 OP-AMP AS NON-INVERTING AMPLIFIER

The circuit diagram of op-amp as non-inverting amplified is shown in Fig. 18.29 in this case the input signal V is applied at the non-inverting termina (+) As explained earlier, due to high open loop gain of amplifer, the inverting ( ) and non

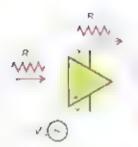


Fig. 18 29

inverting (+) inputs are virtually at the same potential. That is

$$V_{\star} \approx V_{\star} = V_{\rm in}$$

Also, from Fig.18.29,

Current through 
$$R_1$$
 /  $R_1$   $R_2$   $R_3$   $R_4$   $R_5$   $R_5$  Current through  $R_2$  /  $R_2$   $R_3$   $R_4$   $R_5$ 

As practically no current flows between (-) and (+) terminals, so by Kirchhoff's current rule  $I_1 = I_2$ 

Hence 
$$\frac{-V_{o}}{R_{i}} = \frac{V_{m} - V_{o}}{R_{2}}$$
  
or  $V_{m} \left( \frac{1}{R_{i}} + \frac{1}{R_{2}} \right) = \frac{V_{o}}{R_{2}}$   
or  $Gain = \frac{V_{o}}{V_{in}} = 1 + \frac{R_{2}}{R_{i}}$  (18.7)

Again the gain of the amplifier is independent of the internal structure of the op-amp. It just depends upon the two externally connected resistances R and R. The positive sign of gain indicates that the input and out put signals are in phase

Example 18.2° Find the gain of the circuit as shown in Fig 18.30

#### Solution:

As the input signal V<sub>a</sub> is connected to non-inverting input (+) so the op-amp acts as a non-inverting amplifier Comparing it with the circuit of non-inverting amplifier as shown in Fig. 18-29, we have

$$R = infinity$$
 and  $R = 0$   
Gain  $1 = \frac{R_2}{R_1} = 1$ 

# 18.10 OP-AMPASACOMPARATOR

Op-amp usually requires two power supplies of equal voltage but of opposite polarity. Most op-amp operate with  $V = \pm 12 \text{ V}$  supply (Fig. 18.31).



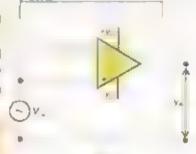


Fig. 18 30

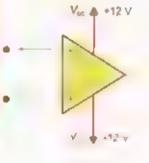
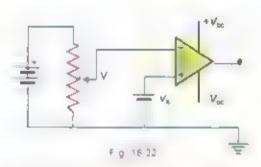


Fig. 18.31



Integrated circuit IC chips are manufactured on waters of semiconductor material

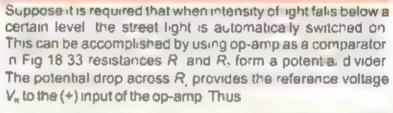
As the open loop gain of the op-amp is very high ( $10^{\circ}$ ), even a very small potential difference between the inverting and non-inverting inputs is amplified to such a large extent that the amplifier gets saturated i.e. its output either becomes equal to  $\pm V_{cc}$  or  $\pm V_{cc}$ . This feature of op-amp is used to compare two voltages. Fig. 18.32 shows the circuit of an op-amp used as



comparator  $V_n$  is reference voltage which is connected with (+) terminal and V is the voltage which is to be compared with the reference  $V_n$ . It is connected with (-) terminal.

When 
$$V > V$$
, or  $V > V_{R}$ , then  $V_u = -V_{CC}$   
and if  $V_u < V_c$  or  $V < V_{R}$ , then  $V_o = +V_{CC}$ 

#### 18.11 COMPARATOR AS A NIGHT SWITCH

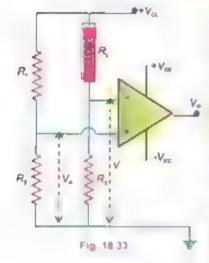


$$V_{\rm R} = \frac{R_2}{R_1 + R_2} \times V_{\rm CC}$$
 (18.8)

LDR is a light dependent resistance. The value of its resistance R, depends upon the intensity of light falling upon it R and R, form another potential divider. The potential drop across R, is V which is given by

$$V = \frac{R_3}{R_L + R_3} \times V_{CC} \tag{18.9}$$

V'provides the voltage to (-) input of the op-amp - V'will not be



a constant voltage but it will vary with the intensity of light. During day time, when light is falling upon LDR,  $R_c$  is small. According to Eq.18.9, V' will be large such that  $V' \ge V_c$  so that  $V_c = -V_{cc}$ . The output of the op is connected with a relay system which energizes only when  $V_c = +V_{cc}$  and then it turns on the street lights. Thus when  $V_c = -V_{cc}$ , the light will not be switched ON

As it gets darker,  $R_i$  becomes larger and V decreases. When V becomes just less than  $V_{\rm p}$ , the output of op-amp switches to  $+V_{\rm cc}$  which energizes the relay system and the street lights are turned ON

### 18.12 DIGITAL SYSTEMS

A digital system deals with quantities or variables which have only two discrete values or states. Following are the examples of such quantities

- (i) A switch can be either open or closed.
- The answer of a question can be either yea or no.
- (iii) Acertain statement can be either true or false.
- (IV) Abulb can be either off or on

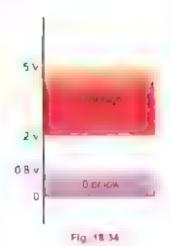
Various designations are used to represent the two quantized states of such quantities. The most common of these are listed in Table 18.1.

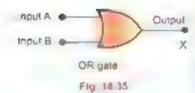
Table 18.1						
	1	2	3	4	5	6
One of the states	True	High	1	Yes	On	Closed
The other state	False	Low	0	No	Off	Open

Mathematical manipulation of these quantities can be best carned if they are represented by binary digits 1 and 0. When we are dealing with voltages, designation No.2 is also a convenient representation.

In describing functions of digital systems a closed switch will be shown as 1 and open switch will be shown as 0. Similarly, a lighted bulb will be described as 1 and an off bulb will be described as 0.

Just as we require two basic mathematical operations, i.e., addition and subtraction for the mathematical manipulation











of ordinary quantities which can possess all continuous values, we require a special algebra, known as Boolean algebra for the manipulation of the quantities which have values 1 and 0, now designated as Boolean variables. Boolean algebra is based upon three basic operations namely AND operation, OR operation and NOT operation. You have already read about these operations. Here we would study about logic gates which implement these operations.

### 18.13 FUNDAMENTAL LOGIC GATES

The electronic circuits which implement the various logic operations are known as logic gates. In these gates the high and low states, i.e., 1 and 0 states are simulated by certain voltage levels ideally one particular voltage level represents a high (1) and another voltage level represents a low (0) in practical digital circuits, however a 1 or high can be any voltage between a specified minimum value and a specified maximum value. Likewise 0 or low can be any voltage between a specified minimum and a specified maximum Fig. 18,34 shows the range 1 and 0 levels for a certain type of digital gates. Thus if voltage of 3.5 V is applied to a gate, tiviliaccept it as high or 1. If a voltage of 0.5 V is applied, the gate will recognize it as 0 or low.

# ORTES

OR gate as symbolically represented in Fig.18.35, implements the logic of OR operation. It has two or more inputs and a single output X. The output has a value 1 when at least one of its inputs A and B is at 1. Thus X will be zero only when both the inputs are 0. Thus it implements the truth table of OR operation (Table 18.2). The mathematical notation for OR operation is

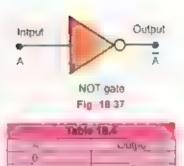
$$X = A + B$$

# AMD Code

The AND gate shown in Fig. 18.36 has two or more inputs and a single output. It is designed such that it implements the truth table of AND operation i.e., its output X is 1 only when both of its Inputs A and B are at 1 and for all other combinations of the values of A and B, X is zero (Table 18.3). The mathematical notation for AND operation is

$$X = A \cdot B$$

it performs the operation of inversion or complementation That is why it is also known as inverter. It changes a logic level to its opposite level, i.e., it changes 1 to 0 and 0 to 1. The symbolic representation of NOT gate is shown in Fig. 18.37. Whenever a bar is placed on any variable, it shows that the value of the variable has been inverted. For example 1 = 0 and 0 = 1. The "bubble" (o) in Fig 18.37 indicates operation of inversion. Its truth table is given in Table 18.4 The mathematical notation for NOT operation is X = A





In NOR gate the output of OR gate is inverted its symbol is shown in Fig.18.38 and its truth table is given in Table 18.5. The mathematical notation for NOR operation is

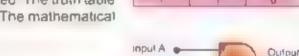


With the



 $X = A \cdot B$ 

In NAND gate the output of an AND gate is inverted its symbol is shown in Fig. 18 39. The bubble in this figure shows that the output of AND gate is inverted. The truth table implemented by it is shown in Table 18.6. The mathematical notation for NAND operation is









Exclusive OR Gate(XOR)

Consider a Boolean function X of two variables A and B such X=AB+AB that

The first term of the function X is obtained by ANDing the variable A with NOT of B. The second term is NOT of A ANDed with B. The function X is obtained by ORing these two terms it can be constructed by combining AND, OR and NOT gates according to the scheme shown nFig 18 40(a) The

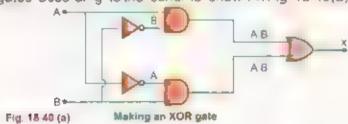


Table 16.7				
A	В	Output		
0	0	0		
1	0	T		
0	1	1		
1	1			





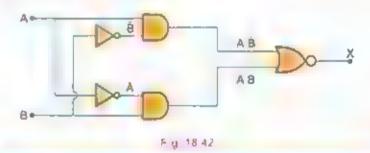
Table 18,8				
À	₿	Quipol		
0	0	3		
D	1	Ü		
1	O.	0		
+	1	1		

value of this function can be obtained by drawing the truth table (Table 18.7) which gives the value of X for all the values of the variables A and B. The value of X is 0 when the two inputs have the same values and it is 1 when the inputs have different values. It can be verified that the circuit of Fig. 18.40(a) implements this truth table. The symbol of XOR gate is shown in Fig. 18.40(b).

# Walker NOR gate (XNOR)

The exclusive NOR gate is obtained by inverting the output of a XOR gate. Its symbol is shown in Fig. 18.41. The bubble shown at the output in this figure shows that the output of XOR gate has been inverted. So its Boolean expression is

The truth table of XNOR gate is given in the Table 18.8 Its output is 1 when its two inputs are identical and 0 when the two inputs are different. Like XOR gate, it is also constructed by a combination of NOT, AND and NOR gates by the scheme shown in Fig. 18.42.



# 18.15 APPLICATIONS OF GATES IN CONTROL SYSTEMS

Gates are widely used in control systems. They control the function of the system by monitoring some physical parameter such as temperature, pressure or some other physical quantity of the system. As gates operate with electrical voltages only, so some devices are required which can convert various physical quantities into electric voltage.

These devices are known as sensors. For example, in the example of night switch, Light Dependent Resistance (LDR) is a sensor for light because it can convert changes in the intensity of light into electric voltage. A thermister is a sensor for temperature. A microphone is a sound sensor. Similarly there are level sensors which give an electrical signal when the level of liquid in a vessel attains a certain limit. One such application is described here. For example sensors are used to monitor the pressure and temperature of a chemical solution stored in a vat. The circuitry for each sensor is such that it produces a HIGH, re., 1 when either the temperature or pressure exceeds a specified value. A circuit is to be designed which will ring an alarm when either the temperature or pressure or both cross the maximum specified limit. The aiarm requires a LOW(0) voltage for its act vation

The block diagram of the problem is shown in Fig 18 43 in which C is the circuit to be designed. Its inputs A and B are fed by the temperature and pressure sensors T and P fitted into the vat. Whenever output of the circuit C is LOW, the alarm is activated. So the circuit C should be such that its output is 0 as soon as the limit for temperature or pressure is exceeded, i.e., when A=0, B=1 or when A=1, B=0 or when A=B=1. The output of C should be HIGH when temperature and pressure are within the specified limit i.e., when A=B=0. This gives the truth table 18.9 which the circuit C has to implement. It can be seen that it is the truth table of NOR gate. So the circuit C in Fig 18.43 should be a NOR gate as shown in Fig 18.44.

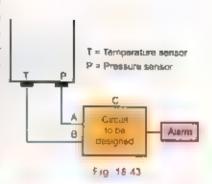
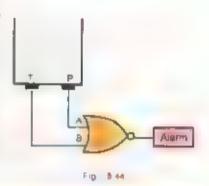


Table 18.9				
A	В	С		
0	0	1		
Ö	†	0		
1	_ 0	0		
i	1	0		



# - CONTRACTOR

- When an external potential difference is applied across a p-n junction such that
  p-side is positive and n-side is negative, it is called forward biased
- When the external source of voltage is applied across a p-n junction such that its
  positive terminal is connected to n-region and its negative terminal to p- region, the
  p-n junction is said to be reverse biased
- Conversion of alternating current into direct current is called rectification
- When only one half of alternating current cycle is converted into direct current, it is called half-wave rectification
- Transistor is a semiconductor device consisting of three electrodes, namely emitter, base and collector. For normal operation, the base-emitter junction is forward biased whereas the collector-base junction is reverse biased.

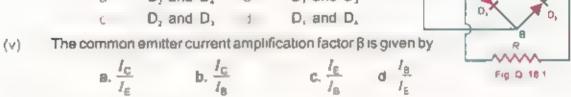
- n. religion is the service positive and negative of the anti-entire.
- · Prostar and refer at the ethother off them has and ground
- Total 1 may
   The second of the se
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- A 4 1 1/42 + A 1 1 4 1 45 2 and beside the decrete
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# QUESTIONS

- 18.1 How does the motion of an electron in a n-type substance differ from the motion of holes in a p-type substance?
  - 18.2 What is the net charge on a n-type or a p-type substance?
  - 18.3 The anode of a diode is 0.2 V positive with respect to its cathode is 1 forward biased?
  - 18.4 Why charge camers are not present in the depletion region?
  - 18.5 What is the effect of forward and reverse biasing of a diode on the width of depletion region?
  - 18.6 Why ordinary stlicon diodes do not emit light?
  - 18.7 Why a photo diode is operated in reverse biased state?
  - 18.8 Why is the base current in a transistor very small?
  - 18.9 What is the biasing requirement of the junctions of a transistor for its normal operation? Explain how these requirements are metin a common emitter amplifier?
  - 18.10 What is the principle of virtual ground? Apply it to find the gain of an inverting amplifier.
- 18.11 The inputs of a gate are 1 and 0 identify the gate if its output is a .0 ib. 1
- 18.12 Tick (✓) the correct answer
- (i) A diode characteristic curve is a plot between
  - (a) current and time (b) voltage and time
  - (c) voltage and current d, forward voltage and reverse voltage

- (ii) The colour of light emitted by a LED depends on
  - (a) its forward bias
- (b) its reverse bias
- (c) the amount of forward current
- (d) the type of semi-conductor material used
- (iii) In a half-wave rectifier the diode conducts during
  - a both halves of the input cycle
  - b a portion of the positive half of the input cycle
  - c. a portion of the negative half of the input cycle
  - d. One half of the input cycle.
- (iv) In a bridge rectifier of Fig. Q. 18.1 when V, is positive at point B with respect to point A, which diodes are ON





- (vi) Truth table of logic function
  - e. summanzes its output values
  - tabulates all its input conditions only
  - display all its input/output possibilities
  - d. is not based on logic algebra
- (v i) The output of a two inputs OR gate is 0 only when its
  - both inputs are 0
     b. either input is 1
  - c. both inputs are 1 d. either input is 0
- (VIII) Atwo nputs NAND gate with inputs A and 8 has an output 0 if
  - a. Ais0

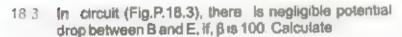
- b. Bis 0
- c. both A and B are zero
- d. both A and B are 1
- (ix) The truth table shown below is for
  - a. XNOR gate
  - b. OR gate
  - c. AND gate
  - d. NAND gate

A	8	X
0	0	1
0	1	O.
1	0	0
1	1	1

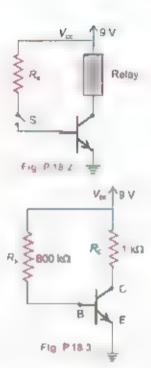
# PROBLEMO

- The current flowing into the base of a transistor is 100  $\mu$ A. Find its collector current  $I_{cr}$  its emitter current  $I_{c}$  and the ratio  $I_{c}/I_{c}$ , if the value of current gain  $\beta$  is 100 (Ans: 10 mA, 10 1 mA, 0.99)
- Fig P18.2 shows a transistor which operates a relay as the switch S is closed. The relay is energized by a current of 10 mA. Calculate the value R<sub>s</sub> which will just make the relay operate. The current gain β of the transistor is 200. When the transistor conducts, its V<sub>sc</sub> can be assumed to be 0.6 V.

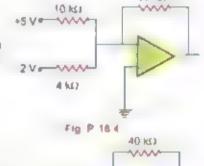
  (Ans: 168 kΩ)



- (i) base current
- (III) collector current
- (III) potential drop across R<sub>c</sub>
- (iV) V<sub>cc</sub>, (Ans: 11.25 μA, 1.125 mA, 1.125 V, 7.875 V)

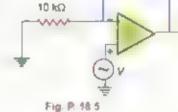


18.4 Calculate the output of the op-amp circuit shown in Fig P 18.4 (Ans. 0)



20 KL1

Calculate the gain of non-inverting amplifier shown in Fig P.18.5. (Ans: 5)



# Chapter 19

# **DAWN OF MODERN PHYSICS**

# **Learning Objectives**

At the end of this chapter the students will be able to.

- 1 Distinguish between inertial and non-inertial frames of references.
- 2 Describe the postulates of special theory of relativity and its results.
- 3 Understand the NAVASTAR navigation system.
- Understand the concept of black body radiation.
- Understand and describe how energy is distributed over the wavelength range for several values of source temperature
- Know Planck's assumptions.
- Know the origin of quantum theory.
- 8 Show an appreciation of the particle nature of electromagnetic radiation.
- Describe the phenomenon of photoelectric effect.
- 10 Explain photoelectric effect in terms of photon energy and work function
- 11 Explain the function of photocell and describe its uses
- 12 Describe Compton's effect.
- 13 Explain the phenomena of pair production and pair annihilation
- 14 Describe de-Broglie's hypothesis of wave nature of particles
- Describe and interpret qualitatively the evidence provided by electron diffraction for the wave nature of particles
- 16 Understand the working principle of electron microscope
- 17 Understand and describe uncertainty principle

In the early part of the twentieth century many experimental and theoretical problems remained unresolved. Attempts to explain the behaviour of matter on the atomic level with the laws of classical physics were not successful. Phenomena such as black body radiation, the photoelectric effect, the emission of sharp spectral lines by atoms in a gas discharge tube, and invariance of speed of light, could not be understood within the framework of classical physics. To explain these observations a revolutionary framework of explanation was necessary which we call modern physics. Its two most significant features are relativity and quantum theory. The observations on objects moving very fast, approaching the speed of light, are well explained by the special theory of relativity. Quantum theory has been able to explain the behaviour of electromagnetic radiation as discrete packets of energy and the particles on a very small scale are dominated by wave properties.

Classical physics is still valid in ordinary processes of everyday life. But to explain the behaviour of tiny or very fast moving particles, we have to use the above mentioned theories. In this chapter, we shall discuss various aspects of theory of relativity and quantum.

theory. Before introducing special theory of relativity some related terms are discussed briefly.

### 19.1 RELATIVE MOTION

When we say a ball is thrown up the 'up direction is only for that particular place. It will be down' position for a person on the diametrically opposite side of the globe. The concept of direction is purely relative. Similarly, the rest position or the motion of an object is not same for different observers. For example, the walls of the cabin of a moving train are stationary with respect to the passengers sitting inside it but are in motion to a person stationary on the ground. So we cannot say whether an object is absolutely at rest or absolutely in motion. All motions are relative to a person or instrument observing it.

Let us perform an experiment in two cars moving with constant velocities in any direction. Suppose a ball is thrown straight up it will come back straight down. This will happen in both cars. But if a person in one car observes the experiment done in the other car, which is moving with constant velocity. The person in the other car, which is moving with constant velocity throws a ball straight up. He will receive the ball straight down. On the other hand, the fellow silling in the stationary car observes that the path of the ball is a parabola. Thus, when experimenters observe what is going on in their own frame of reference, the same experiment gives identical observations. But if they look into other frames, they observe differently.

### 19 2 FRAMES OF REFERENCE

We have discussed the most commonly used Cartesian coordinate system. In effect, a frame of reference is any coordinate system relative to which measurements are taken. The position of a table in a room can be located relative to the walls of the room. The room is then the frame of reference. For measurements taken in the college laboratory, the laboratory is the reference frame of the same experiment is performed in a moving train the train becomes a frame of reference. The position of a spaceship can be described relative to the positions of the distant stars. A coordinate system based on these stars is then the frame of reference.

An inertial frame of reference is defined as a coordinate system in which the law of inertia is valid. That is, a body at

rest remains at rest unless an unbalanced force produces acceleration in it. Other laws of nature also apply in such a system. If we place a body upon Earth it remains at rest unless an unbalanced force is applied upon it. This observation shows that Earth may be considered as an inertial frame of reference. A body placed in a car moving with a uniformive ocity with respect to Earth also remains at rest, so that car is also an inertial frame of reference. Thus any frame of reference which is moving with uniform velocity relative to an inertial frame is also an inertial frame.

When the moving car is suddenly stopped, the body placed in it, no longer remains at rest. So is the case when the car is suddenly accelerated this uch a situation, the car is not an inertial frame of reference. Thus an accelerated frame is a non-inertial frame of reference. Earth is rotating and revolving and hence strictly speaking, the Earth is not an nertial frame. But it can often be treated as an inertial frame without senous error because of very small acceleration.

#### 19.3 SPECIAL THEORY OF RELATIVITY

The theory of relativity is concerned with the way in which observers who are in a state of relative motion describe physical phenomena. The special theory of relativity treats problems involving mertial or non-accelerating frames of reference. There is another theory called general theory of relativity which treats problems involving frames of reference accelerating with respect to one another. The special theory of relativity is based upon two postulates, which can be stated as follows.

- The laws of physics are the same in all inertial frames.
- The speed of light in free space has the same value for all observers, regardless of their state of motion.

The first postulate is the generalization of the fact that all physical laws are the same in frames of reference moving with uniform velocity with respect to one another if the laws of physics were different for different observers in relative motion, the observer could determine from this difference that which of them were stationary in a space and which were moving. But such a distinction does not exist, so this postulate implies that there is no way to detect absolute uniform motion. The second postulate states an experimental fact that speed of light in free space is the universal constant 'c' ( $c = 3 \times 10^6 \text{ ms}^3$ ). These simple postulates have far-reaching consequences. These



The speed of light emitted by flashlight is a measured by two observers one on the moving track and the other on the road.

include such phenomena as the slowing down of clocks and contraction of lengths in moving reference frames as measured by a stationary observer. Some interesting results of the special theory of relativity can be summarized as follows without going into their mathematical derivations.

March March and A

According to special theory of relativity, time is not absolute quantity. It depends upon the motion of the frame of reference.

Suppose an observer is stationary in an inertial frame. He measures the time interval between two events in this frame. Let it be t<sub>1</sub>. This is known as proper time. If the observer is moving with respect to frame of events with velocity v or if the frame of events is moving with respect to observer with a uniform velocity v the time measured by the observer would not be t<sub>n</sub>, but it would be tigiven by

$$t = \frac{l_0}{v^2} \tag{19.1}$$

$$\sqrt{\frac{1}{c^2}}$$

As the quantity  $\sqrt{1-\frac{V^2}{c^2}}$  is always less than one, so t is greater

than (i.e. time has dilated or stretched due to relative motion of the observer and the frame of reference of events. This astorishing result applies to all timing processes — physical chemical and biological. Even aging process of the human body is slowed by motion at very high speeds.



The distance from Earth to a star measured by an observer in a moving spaceship would seem smaller than the distance measured by an observer on Earth. That is, if you are in motion relative to two points that are a fixed distance apart, the distance between the two points appears shorter than if you were at rest relative to them. This effect is known as length contraction. The length contraction happens only along the direction of motion. No such contraction would be observed perpendicular to the direction of motion. The length of an object or distance between two points measured by an observer who is relatively at rest is called proper length 'L'. If an object and an observer are in relative motion with speed vitten the contracted length 'L' is given by

$$r = r_0 \sqrt{1 - \frac{v^2}{c^2}}$$
 (19.2)

The same of the sa

According to special theory of relativity, mass of an object is a varying quantity and depends upon the speed of the object. An object whose mass when measured at rest is *m*, will have an increased mass *m* when observed to be moving at speed *v*. They are related by

$$m = \frac{m_0}{1 - \frac{v^2}{c^2}}$$
 (193)

The increase in mass indicates the increase in inertia the object has at high speeds. As v approaches c, it requires a larger and larger force to change the speed of the object.

As 
$$v \rightarrow c_1 \frac{v}{c} \rightarrow 1$$
 therefore  $\sqrt{1 - \frac{v^2}{c^2}} \rightarrow 0$ 

Thus

m -- or

An infinite mass would require an infinite force to accelerate it. Because infinite forces are not available, hence, an object cannot be accelerated to the speed of light, c'in free space.

In our everyday life, we deal with extremely small speeds, compared to the speed of light. Even the Earth's orbital speed is only 30 kms. On the other hand, the speed of light in free space is 300,000 kms. This is the reason why Newton's laws are valid in everyday situations. However, when experimenting with atomic particles moving with velocities approaching speed of light, the relativistic effects are very prominent, and experimental results cannot be explained without taking Einstein's equations into account.

Fire of Lorden Relation

According to special theory of relativity mass and energy are different entities but are interconvertible. The total energy *E* and mass *m* of an object are related by the expression

$$E = mc^2 \tag{19.4}$$

where m depends on the speed of the object. At rest, the energy equivalent of an object's mass  $m_{\rm e}$  is called rest mass energy  $E_{\rm e}$ .

$$E = m_c c^2 \tag{19.5}$$

As  $mc^2$  is greater than  $m_ec^2$ , the difference of energy  $(mc - m_ec^2)$  is due to motion as such it represents the kinetic energy of the mass. Hence

$$K.E. = (m - m_0)c^2$$
 ....... (19.6)

From equation 19.4 above, the change in mass m due to change in energy  $\Delta E$  is given by

$$\Delta m = \frac{\Delta E}{c^2}$$

Because of its a very large quantity this implies that small changes in mass require very large changes in energy. In our everyday world energy changes are too small to provide measurable mass changes. However, energy and mass changes in nuclear reactions are found to be exactly in accordance with the above mentioned equations.

# MANAGEM Principality of the Control of the Control

The results of special theory of relativity are put to practical use even in everyday life by a modern system of navigation satellites called NAVSTAR. The location and speed anywhere on Earth can now be determined to an accuracy of about 2 cms. However, if relativity effects are not taken into account speed could not be determined any closer than about 20 cms. Using these results the location of an aircraft after an hour's flight can be predicted to about 50 m as compared to about 760 m determined by without using relativistic effects.

**Example 19 1:** The period of a pendulum is measured to be 3.0 s in the inertial reference frame of the pendulum. What is its period measured by an observer moving at a speed of 0.95 c with respect to the pendulum?

#### Solution:

Using 
$$t = 7$$

$$t = 30s$$

$$t = 96s$$

$$t = 7$$

$$t$$

**Example 19.2:** A bar 1.0 m in length and located along x-axis moves with a speed of 0.75 c with respect to a stationary observer. What is the length of the bar as measured by the stationary observer?

Solution:

Using 
$$t_0 = 1.0 \,\text{m}$$
,  $v = 0.75 \,c$ ,  $t = ?$ 

$$t_0 = 1.0 \,\text{m} \times \sqrt{1 - \frac{v^2}{c^2}}$$

$$t_0 = 1.0 \,\text{m} \times \sqrt{1 - \frac{(0.75 \,c)^2}{c^2}} = 1.0 \,\text{m} \times \sqrt{1 - (0.75)^2} = 0.66 \,\text{m}$$

Example 19.3: Find the mass m of a moving object with speed 0.8 c.

#### Solution:

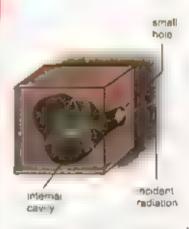
Using 
$$m = \frac{m_o}{\sqrt{1 - \frac{V^2}{c^2}}}$$
 or  $m = \frac{m_o}{\sqrt{1 - \frac{(0.6 \text{ c})^2}{c^2}}} = \frac{m_o}{\sqrt{1 - (0.8)^2}} = 1.67 \text{ m}_o$ 

 $m = 1.67 m_o$ 

# 19.4 BLACK BODY RADIATION

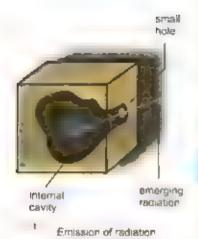
When a body is heated, it emits radiation. The nature of radiation depends upon the temperature. At low temperature, a body emits radiation which is principally of long wavelengths in the invisible infrared region. At high temperature, the proportion of shorter wavelength radiation increases. Furthermore the amount of emitted radiation is different for different wavelengths. It is of interest to see how the energy is distributed among different wavelengths at various temperatures. For example, when platinum wire is heated it appears dull red at about 500 °C, changes to cherry red at 900 °C, becomes orange red at 1100 °C, yellow at 1300 °C, and finally white at about 1800 °C. This shows that as the temperature is increased, the radiation becomes richer in shorter wavelengths.

In order to understand the distribution of radiation emitted from a hot body, we consider a non-reflecting object such as a solid



(a. Absorption of radiation

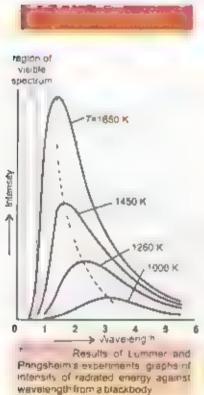
Fig. 19.1

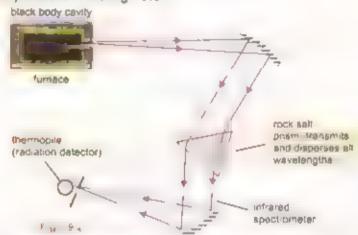


that has a hollow cavity within it. It has a small hole and the radiation can enter or escape only through this hole. The inside is blackened with soot to make it as good an absorber and as bad a reflector as possible. The small hole appears black because the radiation that enters is reflected from the inside walls many times and is partly absorbed at each reflection until none remains. Such a body is termed as black body and has the property to absorbed the radiation entering it. A black body is both an idea, absorber (Fig. 19.1 a) and an ideal radiator (Fig. 19.1 b).

Total Bolisto (Fig. 10 12)

Lummer and Pringsheim measured the intensity of emitted energy with wavelength radiated from a black body at different temperatures by the apparatus shown in Fig. 19.2. The amount of radiation emitted with different wavelengths is shown in the form of energy distribution curves for each temperature in the Fig. 19.3.





These curves reveal the following interesting facts.

At a given temperature, the energy is not uniformly distributed in the radiation spectrum of the body

At a given temperature T the emitted energy has maximum value for a certain wavelength  $\lambda_{min}$  and the product  $\lambda_{min} \times T$  remains constant

$$r = x T = Constant$$
 (197)

The value of the constant known as Wien's constant is about 2.9 x 10° m K. This equation means that as T

increases, λ, shifts to shorter wavelength.

- For all wavelengths, an increase in temperature causes an increase in energy emission. The radiation intensity increases with increase in wavelengths and at a particular wavelength λ<sub>m</sub>, it has a maximum value. With further increase in wavelength, the intensity decreases.
- The area under each curve represents the total energy (E) radiated per second per square metre over all wavelengths at a particular temperature. It is found that area is directly proportional to the fourth power of keivin temperature T. Thus

$$E \times T^+$$
 or  $E \circ T^+$  (198)

where o is called Stefen's constant. Its value is 5.67 x 10<sup>-1</sup> Wm<sup>-1</sup>K<sup>-1</sup> and the above relation is known as Stefen-Botzmanniaw.

Electromagnetic wave theory of radiation cannot explain the energy distribution along the intensity-wavelengths curves. The successful attempts to explain the shape of energy distribution curves gave rise to a new and non-classical rew of electromagnetic radiation. In 1900 Max Planck founded a mathematical model resulting in an equation that describes the shape of observed curves exactly. He suggested that energy is radiated or absorbed in discrete packets, called quanta rather than as a continuous wave. Each quantum is associated with radiation of a single frequency. The energy E of each quantum is proportional to its frequency f, and

$$E = hf$$
 . (19,9)

where his Planck's constant its value is 6.63 x 10° Js. This fundamental constant is as important in physics as the constant c, the speed of light in vacuum.

Max Planck received the Nobel Prize in physics in 1918 for his discovery of energy quanta

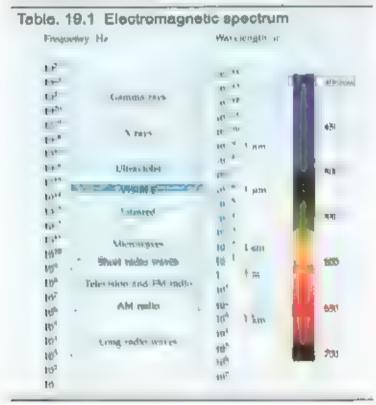
# he Pha

Planck suggested that as matter is not continuous but consists of a arge number of trily particles so is the radiation energy from a source. He assumed that granular nature of

radiation from hot bodies was due to some property of the atoms producing it. Einstein extended his idea and postulated that packets or tiny bundles of energy are integral part of all electromagnetic radiation and that they could not be subdivided. These indivisible tiny bundles of energy he called photons. The beam of light with wavelength  $\lambda$  consists of stream of photons travelling at speed cland carnes energy his from the theory of relativity momentum  $\rho$  of the photon is related to energy as

Thus 
$$\rho c = hf$$
 or  $\rho = \frac{hf}{c} = \frac{h}{\lambda}$ . (19.11)

The table 19.1 relates the quantalem thed in different regions of the electromagnetic spectrum with energy. At the high end, y-radiation with energy ~ 1 MeV is easily detected as quantal by a radiation detector and counter. At the other end, the energy of photon of radio waves is only about 10 ° eV. So millions of photons are needed to detect a signal and hence wave properties of radio waves predominate. The quantalare



so close together in energy value that radio waves are detected as continuous radiation.

The emission or absorption of energy in steps may be extended to include any system such as a mass oscillating on a spring. However, the energy steps are far too small to be detected and so any granular nature is invisible. Quantum effects are only important when observing atomic sized objects, where his a significant factor in any detectable energy change.

**Example 19.4:** Assuming you radiate as does a blackbody at your body temperature about 37 °C, at what wavelength do you emit the most energy?

#### Solution:

$$T = 37 \, ^{\circ}\text{C} = 310 \, \text{K}$$

$$\text{Wien's constant} = 2.9 \times 10^{-3} \, \text{mK}$$

$$\lambda_{\text{max}} = ?$$

$$\text{Using} \quad \lambda_{\text{max}} \times T = \text{Constant}$$

$$\lambda_{\text{max}} = \frac{2.9 \times 10^{-3} \, \text{mK}}{310 \, \text{K}} = 9.35 \times 10^{-6} \, \text{m} = 9.35 \, \mu\text{m}$$

The radiation lies in the invisible infrared region and is independent of skin colour.

Example 19.5: What is the energy of a photon in a beam of infrared radiation of wavelength 1240 nm?

#### Solution:

$$\lambda = 1240 \text{ nm} \qquad E = ?$$
Using 
$$E = hf = \frac{hc}{\lambda}$$

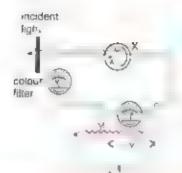
$$E = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^{8} \text{ ms}^{-1}}{1240 \times 10^{-8} \text{ m}} \approx 1.6 \times 10^{-18} \text{ J}$$
or 
$$E = 1.0 \text{ eV}$$

# 19.5 INTERACTION OF ELECTROMAGNETIC RADIATION WITH MATTER

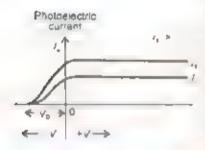
Electromagnetic radiation or photons interact with matter in three distinct ways depending mainly on their energy. The three processes are



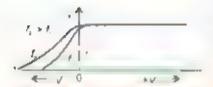
- (1) Compton effect
- Pair production



Experimental arrangement to observe photoelectric effect



Characteristic circles of photocurrent vs applied vortage for two lights ies of monuchromatic light.



Characteristic curves of photocurrent vs. applied voltage for light of different frequencies.

The emission of electrons from a metal surface when exposed to light of suitable frequency is called the photoelectric effect. The emitted electrons are known as photoelectrons.

The photoelectric effect is demonstrated by the apparatus shown in Fig. 19.4. An evacuated glass tube X contains two electrodes. The electrode A connected to the positive terminal of the battery is known as anode. The electrode C connected to negative terminal is known as cathode. When monochromatic light is allowed to shine on cathode, if begins to emit electrons. These photoe ectrons are attracted by the positive anode and the resulting current is measured by an ammeter. The current stops when light is cut off, which proves, that the current flows because of incident, light. This current is hence called photoe ecling current. The maximum energy of the photoelectrons can be determined by reversing the connection of the battery in the circuit : e , now the anode A sinegative and cathode C is at positive potential. In this condition the photoelectrons are repered by the anode and the photoelectric current decreases. If this potential is made more and more negative, at a certain value, called stopping potential V the current becomes zero. Even the electrons of maximum energy are not able to reach collector plate. The maximum energy of photoelectrons is thus

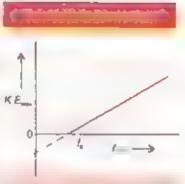
$$\frac{1}{2}mv_{max}^2 = V_0 e$$
 (19.11)

where m is mass v is velocity and e is the charge on electron if the experiment is repeated with light beam of higher intensity, the amount of current increases but the current stops for the same value of  $V_o$ . The Fig 19.5 shows two curves of photoelectric current as a function of potentia. V where  $I_z \ge I_1$ , if, however, the intensity is kept constant and experiment is performed with different frequencies of incident light, we obtain the curves shown in Fig 19.6. The current is same but stopping potentia is different for each frequency of incident light, which indicates the proportional ty of maximum kinetic energy with frequency of light I.

The important results of the experiments are

- The electrons are emitted with different energies. The maximum energy of photoelectrons depends on the particular metal surface and the frequency of incident light.
- There is a minimum frequency below which no electrons are emitted, however intense the light may be. This threshold frequency f<sub>a</sub> varies from metal to metal
- Electrons are emitted instantaneously, the intensity of light determines only their number.

These results could not be explained on the basis of electromagnetic wave theory of light. According to this theory increasing the intensity of incident light should increase the K.E. of emitted electrons which contradicts the experimental result. The classical theory cannot also explain the threshold frequency of light.



A graph of the maximum kinetic energy of photoeractrons vs. light frequency. Below a celtain frequency fall no photoemission occurs.

# Constitution of the last

Einstein extended the idea of quantization of energy proposed by Max Planck that light is emitted or absorbed in quanta known as photons. The energy of each photon of frequency fas given by quantum theory is

A photon could be absorbed by a single electron in the metal surface. The electron needs a certain minimum energy called the work function. Of to escape from the metal surface. If the energy of incident photon is sufficient, the electron is ejected instantaneously from the metal surface. A part of the photon energy (work function) is used by the electron to break away from the metal and the rest appears as the kinetic energy of the electron. That is,

Incident photon energy - Work function = Max, K, E, of photoelectron

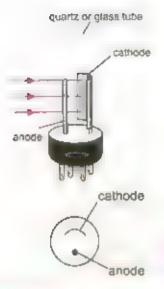
or 
$$h/-\Phi = \frac{1}{2}mv_{max}^2$$
 (19 12)

This is known as Einstein's photoelectric equation.

When  $KE_{mp}$  of the photoelectron is zero, the frequency f is equal to threshold frequency  $f_m$  hence the Eq. 19-12 becomes

$$hf_a - \Phi = 0$$
 or  $\Phi = hf_a$  ............................... (19.13)

Hence, we can also write Einstein's photoelectric equation as



F 5 17 \* Simple photo-emissive cell



F 11.5 Sound track on a film which values the intensity of ligh reaching the photo cell

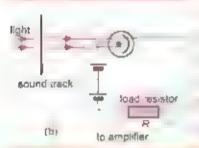


Fig. 1.4 Photocall detection circuit for sound track of movies.

It is to be noted that all the emitted electrons do not possess the maximum kinetic energy some electrons come straight out of the metal surface and some lose energy in atomic collisions before coming out. The equation 19 14 holds good only for those electrons which come out with full surplus energy

Albert Einstein was awarded Nobel Prize in physics in 1921 for his explanation of photoelectric effect.

Note that the phenomenon of photoelectric effect cannot be explained if we assume that light consists of waves and energy is uniformly distributed over its wavefront. It can only be explained by assuming light consists of corpuscles of energy known as photon. Thus it shows the corpuscular nature of light.

A photocel is based on photoelectric effect. A simple photocel is shown in Fig. 19.7. It consists of an evacuated glass bulb with a thin anode rod and a cathode of an appropriate metal surface. The material of the cathode is selected to suit to the frequency range of incident radiation over which the cell is operated. For example sodium or potassium cathode emits electrons for visible light, cesium coated oxidized silver emits electrons for infrared light and some other metals respond to ultraviolet radiation. When photo-emissive surface is exposed to appropriate light (Fig. 19.8 a) electrons are emitted and a current flows in the external circuit which increases with the increase in light intensity. The current stops when the light beam is interrupted. The cell has wide range of applications. Some of these are to operate.

- Security systems
- Counting systems
- 3 Automatic door systems
- 4 Automatic street lighting
- 5 Exposure meter for photography
- Sound track of movies (Fig 19 8 b)

Example 19.6: A sod um surface is illuminated with light of wavelength 300 nm. The work function of sodium metal.

#### is 2.46 eV

- (a) Find the maximum K.E. of the ejected electron.
- (b) Determine the cut off wavelength for sodium.

## Solution:

$$\lambda = 300 \, \text{nm}, \quad \Phi = 2.46 \, \text{eV}$$

or 
$$E = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ ms}^{-1}}{300 \times 10^{-9} \text{ m}} \approx 6.63 \times 10^{-19} \text{ J}$$

Now  $KE_{max}$  hf  $\Phi = 4.14 \,\text{eV} + 2.46 \,\text{eV} + 1.68 \,\text{eV}$ 

Using

or 
$$\lambda_0 = \frac{hc}{dt} = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ ms}^{-1}}{3.94 \times 10^{-9} \text{ J}} = 5.05 \times 10^{-7} \text{ m}$$

$$\lambda_0 = 505 \text{ nm}$$

The cut off wavelength is in the green region of the visible spectrum

Arthur Holly Compton at Washington University in 1923 studied the scattering of X-rays by loosely bound electrons. from a graphite target (Fig 199 a). He measured the wavelength of X-rays scattered at an angel 8 with the original direction. He found that wavelength A, of the scattered X-rays. is larger than the wavelength \(\lambda\) of the incident X-rays. This is known as Compton effect. The increase in wavelength of scattered X-rays could not be explained on the basis of classical wave theory Compton suggested that X-rays consist of photons and in the process of scattering the photons suffer collision with electrons like billiard balls (Fig 19.9 b & c) In this collision, a part of incident photon energy and momentum is transferred to an electron. Applying energy and momentum conservation laws to the process, he derived an expression for the change in wavelength  $\Delta\lambda$ known as Compton shift for scattering angle 9 as

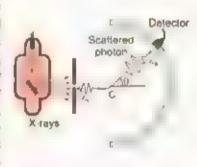
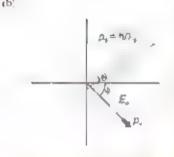


Fig. 10 9 (a) Compton's scattering experiment



Electron and co-Buth are scattered

$$\Delta \lambda = \frac{h}{m_0 c} \left( 1 - \cos \theta \right) \dots (19.15)$$

where  $m_i$  is the rest mass of the electron. The factor  $\frac{h}{m_0c}$  has

dimensions of length and is called Compton wavelength and has the numerical value.

$$\frac{h}{m_0 c} = \frac{6.63 \times 10^{-34} \text{ Js}}{9.1 \times 10^{-31} \text{ kg} \times 3 \times 10^8 \text{ ms}^{-1}} = 2.43 \times 10^{-12} \text{ m}$$

If the scattered X-ray photons are observed at  $\theta = 90^\circ$  the Compton shift  $\Delta r$  equals the Compton wavelength. The Eq 19.15 was found to be in complete agreement with Compton's experimental result, which again is a striking confirmation of particle like interaction of electromagnetic waves with matter.

Arthur Holly Compton was awarded Nobe. Prize in physics in 1927 for his discovery of the effect named after him.

**Example 19 7:** A 50 keV photon is Compton scattered by a quasi-free electron. If the scattered photon comes off at 45° what is its wavelength?

#### Solution:

$$E = 50 \text{ keV} = 50 \times 10^{3} \times 16 \times 10^{-18} \text{ J}$$
Using 
$$E = hf = \frac{hc}{\lambda} \qquad \text{or} \qquad \frac{hc}{E}$$

$$\lambda = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^{8} \text{ ms}^{-1}}{50 \times 10^{3} \times 1.6 \times 10^{-19} \text{ J}} = 0.0248 \text{ nm}$$
Now 
$$\lambda = \lambda = \frac{h}{mc} (1 - \cos 45)$$

$$\lambda = \frac{h}{mc} (1 - \cos 45)$$

$$\lambda = \frac{h}{mc} (1 - \cos 45)$$

$$-0.2429 \times 10^{19} \text{ ms}^{-1} (1 - 0.707)$$

$$-0.2429 \times 10^{19} \text{ ms}^{-1} (1 - 0.707)$$

$$-0.2429 \times 10^{19} \text{ ms}^{-1} (1 - 0.707)$$

$$\lambda = 0.0248 \text{ nm} + 0.0007 \text{ nm}$$

$$\lambda = 0.0248 \text{ nm} + 0.0007 \text{ nm} = 0.0255 \text{ nm}$$

n the previous sections you have studied that a low energy photon interacting with a metal is usually completely absorbed with the emission of electron (Photoelectric effect) and a high energy photon such as that of X-rays is scattered by an atomic electron transferring a part of its energy to the electron (Compton effect). A third kind of interaction of very high energy photon such as that of y-rays with matter is pair production in which photon energy is changed into an electron-positron pair. A positron is a particle having mass and charge equal to that of electron but the charge being of opposite nature le positive. The creation of two particles with equal and opposite charges is essential for charge conservation in the universe. The positron is also known as antiparticle of electron or anti-electron. The interaction usually takes place in the electric field in the vicinity of a heavy nucleus as shown in the Fig. 19.10 so that there is a particle to take up recoil energy and momentum is conserved

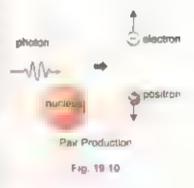
In the process radiant energy is converted into matter in accordance with Einstein's equation E=mc, and hence is a so known as materialization of energy. For an electron or positron, the rest mass energy = mc = 0.51. MeV. Thus to create the two particles 2 x 0.51. MeV or 1.02 MeV energy is required. For photons of energy greater than 1.02 MeV, the probability of pair production occurrence increases as the energy increases and the surplus energy is carried off by the two particles in the form of kinetic energy. The process can be represented by the equation

$$hf = 2m_e c^2 + K.E.(e^-) + K.E.(e^-)$$
 (19.16)

#### 19.6 ANNIHILATION OF MATTER

t is converse of pair production when a positron comes close to an electron they annihilate or destroy each other. The matter of two particles changes into electromagnetic energy producing two photons in the y-rays range.

The two photons are produced travelling in opposite directions (Fig. 19.11) so that momentum is conserved. Each



photon has energy 0.51 MeV equivalent to rest mass energy of a particle

The existence of positron was predicted by Dirac in 1928 and it was discovered in the cosmic radiation in 1932 by Carl Anderson. It gradually became clear that every particle has a corresponding antiparticle with the same mass and charge (if it is a charged particle) but of opposite sign. Particles and antiparticles also differ in the signs of other quantum numbers that we have not yet discussed. A particle and its antiparticle cannot exist together at one place. Whenever they meet, they annihilate each other. That is, the particles disappear, their combined rest energies appear in other forms. Proton and antiproton annihilation has also been observed at Lawrence Berkeley Laboratory.

# 19.7 WAVE NATURE OF PARTICLES

It has been observed that light displays a dual nature. It acts as a wave and it acts as a particle. Assuming symmetry in nature, the French physicist. Louis de Broglie proposed in 1924 that particles should also possess wave like properties. As momentum p of photon is given by equation 19.11.

$$p = \frac{h}{4}$$

de Broglie suggested that momentum of a material particle of mass m moving with velocity v should be given by the same expression. Thus

$$\rho = \frac{h}{\lambda} = mv$$

$$h = \frac{h}{\rho} = mv \qquad (19.17)$$

where  $\lambda$  is the wavelength associated with particle waves. Hence an electron can be considered to be a particle and it can also be considered to be a wave. The equation 19.17 is called de Broglie relation.

An object of large mass and ordinary speed has such a small wavelength that its wave effects such as interference and diffraction are negligible. For example, a rifle bullet of mass 20 g and flying with speed 330 ms, will have a wavelength A given by

$$\lambda = \frac{h}{mv} = \frac{6.63 \times 10^{-34} \text{ Js}}{2 \times 10^{-2} \text{ kg} \times 330 \text{ ms}^{-1}} = 1 \times 10^{-34} \text{ m}$$

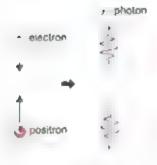


Fig. 19 15



or

Light is, in short the most refined form of matter (Louis de Broglie 1892-1987)

This wavelength is so small that it is not measurable or detectable by any of its effects.

On the other hand for an electron moving with a speed of 1 x 10" ms

$$\lambda = \frac{6.63 \times 10^{-34} \text{ Js}}{9.1 \times 10^{-31} \text{ kg} \times 1 \times 10^6 \text{ ms}^{-1}} = 7 \times 10^{-10} \text{ m}$$

This wavelength is in the X-rays range. Thus, diffraction effects for electrons are measurable whereas diffraction or interference effects for bullets are not.

# Davisous and Gormon Esperiment

A convincing evidence of the wave nature of electrons was provided by Clinton J. Davisson and Laster H. Germer. They showed that electrons are diffracted from metal crystals in exactly the same manner as X-rays or any other wave. The apparatus used by them is shown in Fig. 19.12, in which electrons from heated filament are accelerated by an adjustable applied voltage. V. The electron beam of energy. Ve is made incident on a nickel crystal. The beam diffracted from crystal surface enters a detector and is recorded as a current /. The gain in K.E. of the electron as it is accelerated by a potential. Vin the electron guin is

given by 
$$\frac{1}{2}mv^2 = Ve$$
or 
$$mv^2 = 2Ve : m^2v^2 = 2mVe$$
or 
$$mv = \sqrt{2mVe}$$

From de Broglie equation

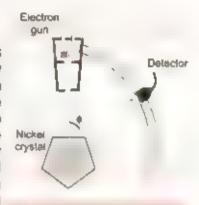
Thus

In one of the experiments, the accelerating voltage V was 54 volts, hence

$$\lambda = \frac{h}{\sqrt{2 \, mVe}} = \frac{6.63 \times 10^{-34} \text{ Js}}{\sqrt{2 \times 9.1 \times 10^{-31} \text{ kg} \times 54 \text{ JC}^{-1} \times 1.6 \times 10^{-19} \text{ C}}}$$

$$\lambda = 1.66 \times 10^{-10} \text{ m}$$

This beam of electrons diffracted from crystal surface was obtained for a grancing angle of 65° According to Bragg's



F g 19 12 Experimental arrangement of Davisson and Germer for electron diffraction

equation

 $2 d \sin \theta = m\lambda$ 

For 1st order diffraction m = 1

For nickel d= 0.91 x 10<sup>10</sup> m

Thus  $2 \times 0.91 \times 10^{-10} \text{ m} \times \sin 66^{\circ} = \lambda$ 

which gives  $\lambda = 1.65 \times 10^{-19} \text{ m}$ 

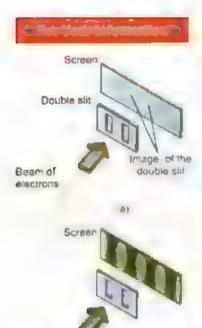
Thus experimentally observed wavelength is in excellent agreement with theoretically predicted wavelength

Diffraction patterns have also been observed with protons neutrons hydrogen atoms and helium atoms thereby giving substantial evidence for the wave nature of particles

For his work on the dual nature of particles, Prince Louis Victor de Brogne received the 1929 Nobel Prize in physics Curton Joseph Davisson and George Pagel Thomson shared the Nobel Prize in 1937 for their experimental confirmation of the wave nature of particles

Water and Commission

Interference and diffraction of light confirm its wave nature while photoe ectac effect proves the particle nature of light Similarly the experiments of Davisson and Germer and G.P. Thomson reveal wave like nature of electrons and in the experiment of J. J. Thomson to find elm we had to assume particle like nature of the electron. In the same way we are forced to assume both wavelike and particle like properties for all matter electrons protons neutrons molecules etc. and also light, X-rays, /-rays etc. have to be included in this. In other words, matter and radiation have a dual 'waveparticle' nature and this new concept is known as wave particle duality. Niels Bohr pointed out in stating his principle. of complementarity that both wave and particle aspects are required for the complete description of both radiation and matter. Both aspects are always present and either may be revealed by an experiment. However, both aspects cannot be revealed simultaneously in a single experiment, which aspect is revealed is determined by the nature of the experiment being done. If you put a diffraction grating in the path of a light beam you revea it as a wave if you allow the light beam to hit a metal surface, you need to regard the beam as a stream of particles to explain your observations There is no simple experiment that you can carry out with the



(a) If electrons behaved as 1's lefe particles with no wave properties they would nass to home or the other of the 'n single as a life screen as a 'g' and produce and single as a pattern of bright a last less small to light is used and interference occurs between the single according from each site.

b.

Beam of

electrons

beam that will require you to interpret it as a wave and as a particle at the same time. Light behaves as a stream of photons when it interacts with matter and behaves as a wave in traveling from a source to the place where it is detected. In effect, all micro-particles (electrons, protons, photons, atoms etc.) propagate as if they were waves and exchange energies as if they were particles—that is the wave particle duality.

**Example 19.8:** A particle of mass 5.0 mg moves with speed of 8.0 ms<sup>-1</sup>. Calculate its de Broglie wavelength.

# Solution:

$$m = 5.0 \text{ mg} = 5.0 \times 10^{-6} \text{ kg}$$
  
 $v = 8.0 \text{ ms}$   
 $h = 6.63 \times 10^{-34} \text{ Js}$   
Using  $\lambda = \frac{h}{mc} = \frac{6.63 \times 10^{-34} \text{ Js}}{5.0 \times 10^{-6} \text{ kg} \times 8.0 \text{ ms}^{-1}} \approx 1.66 \times 10^{-29} \text{ m}$ 

**Example 19.9:** An electron is accelerated through a Potential Difference of 50 V Calculate its de Brogile wavelength

#### Solution:

$$m = 9.1 \times 10^{-31} \text{ kg}, \qquad V_o = 50 \text{ V},$$

$$\lambda = ?, \qquad e = 1.6 \times 10^{-19} \text{ C}$$

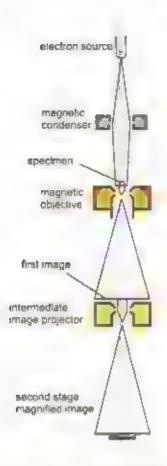
$$\frac{1}{2} m v^2 = V_o e$$

$$p = m v = \sqrt{2} m V_o e$$
then
$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2} m V_o e}$$

$$= \frac{6.63 \times 10^{-34} \text{ Js}}{\sqrt{2 \times 9.1 \times 10^{-31} \text{ kg} \times 50 \text{ JC}^{-1} \times 1.6 \times 10^{-19} \text{ C}}}$$

$$\lambda = 1.74 \times 10^{-10} \text{ m}$$

The fact that energetic particles have extremely short de Broglie wavelengths has been put to practical use in many ultra-modern devices of immense importance such as electron microscope.



Electron microscope ( Block Diagram)

Fig. 19 13



n the subatomic world few things can be predicted with 100% precision

Efectron microscope makes practical use of the wave nature of electrons which is thousands of time shorter than visible light which enables the electron microscope to distinguish details not visible with optical microscope. In an electron microscope, electric and magnetic fields rather than optical tenses are used to focus electrons by means of electromagnetic forces that are exerted on moving charges. The resulting deflections of the electrons beams are similar to the refraction effects produced by glass lenses used to focus light in optical microscope. The electrons are accelerated to high energies by applying voitage from 30 kV to several megavoits. Such high voltages give extremely short wavelength and also give the electron sufficient energy to penetrate specimen of reasonable thickness. A resolution of 0.5 to 1 nm is possible with a 50 kV microscope as compared to best optical resolution of 0.2 µm. A schematic diagram of the electron microscope is shown in the Figure 19.13. The magnetic conducting lens concentrates the beam. from an electron gun on to the specimen. Electrons are scattered out of the beam from the thicker parts of the specimen. The transmitted beam therefore has spatial differences in density that correspond to the features of the specimen. The objective and intermediate lenses produce a real intermediate image and projection lens forms the final image which can be viewed on a fluorescent screen or photographed on special film known as electron micrograph A three dimensional image of remarkable quality can be achieved by modern versions called scanning electron microscopes

# 19.8 UNCERTAINTY PRINCIPLE

Position and momentum of a particle cannot both be measured simultaneously with perfect accuracy. There is always a fundamental uncertainty associated with any measurement. This uncertainty is not associated with the measuring instrument. It is a consequence of the wave particle duality of matter and radiation. This was first proposed by Werner Heisenberg in 1927 and hence is known as Heisenberg. Uncertainty Principle. This fundamental uncertainty is completely negligible for measurements of position and momentum of macroscopic objects but is a predominant fact of life in the atomic domain. For example, a stream of light photons scattering from a flying tennis ball.

hardly affects its path, but one photon striking an electron drastically alters the electron's motion. Since light has also wave properties, we would expect to be able to determine the position of the electron only to within one wavelength of the light being used. Hence, in order to observe the position of an electron, with less uncertainty and also for minimizing diffraction effect, we must use light of short wavelength. But it will alter the motion drastically making momentum measurement less precise. If light of wavelength A. is used to locate a micro particle moving along x-axis, the uncertainty in its position measurement is

$$\Delta x \approx \lambda$$

At most, the photon of light can transfer all its momentum  $\binom{h}{\lambda}$  to the micro particle whose own momentum will then be

uncertain by an amount

$$\Delta p \approx \frac{h}{\lambda}$$

Multiplying these two uncertainties gives

$$\Delta x \Delta p \approx \frac{h}{\Delta} \approx h$$
 (19.19)

The equation 19 19 is the mathematical form of uncertainty principle. It states that the product of the uncertainty  $\Delta x$  in the position of a particle at some instant and the uncertainty  $\Delta p$  in the x-component of its momentum at the same instant approximately equals Planck's constant h

There is another form of uncertainty principle which relates the energy of a particle and the time at which it had the energy if the AE is the uncertainty in our knowledge of the energy of our particle and if the time interval during which

the particle had the energy  $E \pm \frac{\Delta E}{2}$  is  $t_a \pm \frac{\Delta t}{2}$ , then

Thus more accurately we determined the energy of a particle the more uncertain we will be of the time during which it has that energy

According to Heisenberg's more careful calculations, he found that at the very best



You can never accurately describe all aspects of a subatomic particle at once

Werner Karl Heisenberg received Nobel Prize for physics in 1932 for the development of quantum mechanics.

Example 19.10: The life time of an electron in an excited state is about 10<sup>4</sup> s. What is its uncertainty in energy during this time?

#### Solution:

Using uncertainty principle

$$\Delta E \Delta t \approx h$$

$$\Delta E = \frac{h}{\Delta t} = \frac{1.05 \times 10^{-34} \text{ Js}}{10^{-6} \text{ s}}$$

$$\Delta E = 1.05 \times 10^{-26} \text{ J}$$

Example 19.11: An electron is to be confined to a box of the size of the nucleus (1.0 x 10" m). What would the speed of the electron be if it were so confined?

### Solution:

Maximum uncertainty in the location of electron equals the size of the box itself that is  $\Delta x = 1.0 \times 10^{16}$  m. The minimum uncertainty in the velocity of electron is found from Heisenberg uncertainty principle.

$$\Delta p = \frac{h}{\Delta x}$$

or

$$m\Delta V = \frac{h}{\Delta x}$$

$$\Delta V = \frac{h}{m\Delta x} = \frac{1.05 \times 10^{-34} \text{ Js}}{9.1 \times 10^{-34} \text{ kg} \times 1.0 \times 10^{-14} \text{ m}} = 1.15 \times 10^{10} \text{ m/s}$$

For confinement in the box, the speed should be greater than the speed of light. Because this is not possible, we must conclude that an electron can never be found inside the nucleus.



- An inertial frame of reference is defined as a coordinate system in which the law of inertia is valid. A frame of reference that is not accelerating is an inertial frame of reference.
- The special theory of relatively treats problems involving inertial or non-accelerating frames of reference, it is based upon two postulates.
  - ( ) The laws of physics are the same in all inertial frames.
  - The speed of light in free space has the same value for all observers, regardless of their state of motion.
- E = mc is an important result of special theory of relativity.
- A black body is a solid block having a hollow cavity within it. It has small hole and the
  radiation can enter or escape only through this hole.
- Stephen Boltzmann law states that total energy radiated over all wave length at a
  particular temperature is directly proportional to the fourth power of that Kelvin
  temperature
- The emission of electrons from a metal surface when exposed to ultraviolet light is called photoelectric effect. The emitted electrons are known as photoelectrons.
- When X-rays are scattered by loosely bound electrons from a graphite target. It is known as Compton effect.
- The change of very high energy photon into an electron, positron pair is called pair production.
- When a positron comes close to an electron, they annihilate and produce two
  photons in the y-rays range. It is called annihilation of matter.
- Position and momentum of a particle cannot both be measured a multaneously with
  perfect accuracy. There is always a fundamental uncertainty associated with any
  measurement. It is a consequence of the wave particle duality of matter and
  radiation. It is known as Heisenberg uncertainty principle.



- 19.1 What are the measurements on which two observers in relative motion will always agree upon?
- 19.2 Does the dilation means that time really passes more slowly in moving system or that it only seems to pass more slowly?
- 19.3 If you are moving in a spaceship at a very high speed relative to the Earth, would you notice a difference (a) in your pulse rate (b) in the pulse rate of people on Earth?

- 4 If the speed of light were infinite, what would the equations of special theory of relativity reduce to?
- Since mass is a form of energy, can we conclude that a compressed spring has more mass than the same spring when it is not compressed?
- As a solid is heated and begins to glow, why does it first appear red?
- What happens to total radiation from a blackbody if its absolute temperature is doubled?
- 1.45 A beam of red light and a beam of blue light have exactly the same energy. Which beam contains the greater number of photons?
- Which photon, red, green, or blue cames the most (a) energy and (b) momentum?
- Which has the lower energy quanta? Radiowaves or X-rays
- Does the brightness of a beam of light primarily depends on the frequency of photons or on the number of photons?
- When ultraviolet light falls on certain dyes, visible light is emitted. Why does this not happen when infrared light falls on these dyes?
- Will bright light eject more electrons from a metal surface than dimmer light of the same colour?
- Will higher frequency light eject greater number of electrons than low frequency light?
- 15 When light shines on a surface, is momentum transferred to the metal surface?
- Why can red light be used in a photographic dark room when developing films, but a blue or white light cannot?
- 1 17 Photon A has twice the energy of photon B. What is the ratio of the momentum of A to that of B?
- 18 Why don't we observe a Compton effect with visible light?
- Can pair production take place in vacuum? Explain.
- 20 Is it possible to create a single electron from energy? Explain.
- If electrons behaved only like particles, what pattern would you expect on the screen after the electrons passes through the double slit?
- 1 22 If an electron and a proton have the same de Broglie wavelength, which particle has greater speed?
- 15.3 We do not notice the de Brogile wavelength for a pitched chicket ball. Explain why?
  - 9.24 If the following particles have the same energy, which has the shortest wavelength? Electron, alpha particle, neutron, proton.
- 1). 5 When does light behave as a wave? When does it behave as a particle?
- 1 + 16 What advantages an electron microscope has over an optical microscope?
- If measurements show a precise position for an electron, can those measurements show precise momentum also? Exprain

# PROBLEMS

- 19 1 A particle cailed the pion lives on the average only about 2.6 x 10<sup>-8</sup> s when at rest in the laboratory. It then changes to another form. How long would such a particle live when shooting through the space at 0.95 c? [Ans. 8.3 x 10<sup>-8</sup> s]
- 19.2 What is the mass of a 70 kg man in a space rocket traveling at 0.8 c from us as measured from Earth? [Ans. 116.7 kg]
- 19.3 Find the energy of photon in
  - (b) Radiowave of wavelength 100 m
  - (c) Green light of wavelength 550 nm
  - (d) X-ray with wavelength 0.2 nm

[Ans. (a) 1.24 x 10<sup>-6</sup> eV (b) 2.25 eV (c) 6200 eV ]

- 19.4 Yellow light of 577 nm wavelength is incident on a cesium surface. The stopping voitage is found to be 0.25 V. Find.
  - (a) the Maximum K.E. of the photoelectrons
  - (b) the work function of cesturn

[Ans. (a) 4 x 10<sup>-20</sup> J (b) 1.91 eV ]

19.5 X-rays of wavelength 22 pm are scattered from a carbon target. The scattered radiation being viewed at 85° to the incident beam. What is Compton shift?

[Ans. 2 2 x 10" m]

19.6 A 90 keV X-ray photon is fired at a carbon target and Compton scattering occurs. Find the wavelength of the incident photon and the wavelength of the scattered photon for scattering angle of (a) 30° (b) 60°

(Ans. 13.8 pm (a) 14.1 pm (b) 15 pm)

19.7 What is the maximum wavelength of the two photons produced when a positron annihilates an electron? The rest mass energy of each is 0.51 MeV.

[Ans. 2.44 x 10 12 m]

- 19.8 Calculate the wavelength of
  - (a) a 140 g ball moving at 40 ms 3
  - (b) a proton moving at the same speed
  - an electron moving at the same speed

[Ans. (a) 1.18 x 10<sup>-st</sup> m (b) 9.92 nm (c) 1,82 x 10<sup>-s</sup> m]

- 19.9 What is the de Broglie wavelength of an electron whose kinetic energy is 120 eV?

  [Ans. 1.12 x 10<sup>-10</sup> m]
- 19 10 An electron is placed in a box about the size of an atom that is about 1.0 x 10 <sup>10</sup> m. What is the velocity of the electron? [Ans. 7.29 x 10 ms <sup>1</sup>]

# Chapter 20

# ATOMIC SPECTRA

# **Learning Objectives**

At the end of this chapter the students will be able to:

- Know experimental facts of hydrogen spectrum
- Describe Bohr's postulates of hydrogen atom.
- Explain hydrogen atom in terms of energy levels.
- Describe de-Brogile's interpretation of Bohr's orbits.
- Understand excitation and ionization potentials.
- 6 Describe uncertainty regarding position of electron in the atom.
- 7 Understand the production properties and uses of X-rays
- Describe the terms spontaneous emission, stimulated emission, metastable states and population inversion.
- 9 Understand laser principle
- 10 Describe the He-Ne gas laser
- 11 Describe the application of laser including holography

he branch of physics that deals with the investigation of wavelengths and intensities of electromagnetic radiation emitted or absorbed by atoms is called spectroscopy it includes the study of spectra produced by atoms in general there are three types of spectra called (i) continuous spectra, (ii) band spectra, and (iii) discrete or line spectra.

Black body radiation spectrum as described in chapter 19 is an example of continuous spectral molecular spectra are the examples of band spectra while the atomic spectra which we shall investigate in detail in this chapter are examples of discrete or line spectra.

# 20.1 ATOMIC SPECTRA

When an atomic gas or vapour at much less than atmospheric pressure is suitably excited, usually by passing an electric current through it. The emitted radiation has a spectrum, which contains certain specific wavelengths only. An idealized arrangement for observing such atomic spectra is shown in Fig. 20.1. Actual spectrometer uses diffraction grating for better results.

The impression on the screen is in the form of lines if the slit in front of the source S is narrow rectangle. It is for this reason that the spectrum is referred to as line spectrum.

The fact that the spectrum of any element contains wavelengths that exhibit definite regulanties was utilized in the second half of the 19° century in identifying different elements.

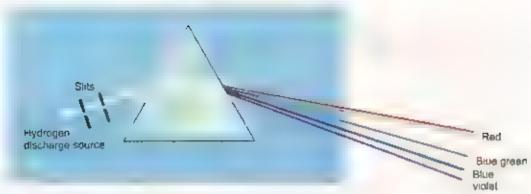


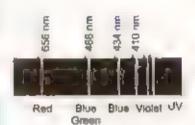
Fig. 20.1 Line spectrum of hydrogen

These regularities were classified into certain groups called the spectral series. The first such series was identified by J J Baimer in 1885 in the spectrum of hydrogen. This series called the Baimer series, is shown in Fig 20.2, and is in the visible region of the electromagnetic spectrum.

The results obtained by Balmer were expressed in 1896 by J R Rydberg in the following mathematical form

$$\frac{1}{\lambda} = R_H \left( \frac{1}{2^2} = \frac{1}{n^2} \right) \dots (20.1)$$

where R<sub>H</sub> is the Rydberg's constant, its value is 1 0974 x 10<sup>2</sup> m. Since then many more series have been discovered and proved heipful in predicting the arrangement of the electrons in different atoms.



Fla. 20.2

The Balmer series contain wavelengths in the visible portion of the hydrogen spectrum. The spectral lines of hydrogen in the ultraviolet and infrared regions fall into several other series. In the ultraviolet region, the Lyman series contains the wavelengths given by the formula.

$$\frac{1}{\lambda} = R_H = \frac{1}{1^2} = \frac{1}{n^2} \qquad (20.2)$$

where

n = 23, 4

in the infrared region, three spectral series have been found whose lines have the wavelengths specified by the formulae.



(a) Continuous spectrum

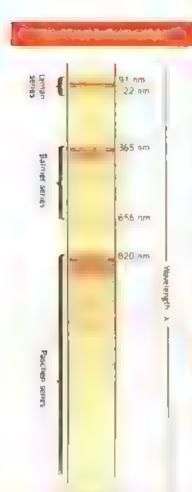


(b) Line spectrum



(c) Band spectrum

#### Paschen series



Line spectrum of atomic hydrogen. Only the Balmer series lies in the visible legion of the electromagnetic spectrum.

$$\frac{1}{A} R_{H} \frac{1}{3^{2}} \frac{1}{n^{2}}, \qquad (20.3)$$
n=4.5.6.

where

Brackett senes

$$\frac{1}{2} \cdot R_{H} = \frac{1}{4^{2}} \cdot \frac{1}{n^{2}}$$
 (20 4)

where

n = 5, 6, 7

Pfund senes

$$\frac{1}{A} = R_{H} \frac{1}{5^{2}} \frac{1}{R^{2}}$$
 (20.5)

where

n = 6, 7, 8,

The existence of these regularities in the hydrogen spectrum together with similar regularities in the spectra of more complex elements proposes a definite test for any theory of atomic structure.

# 20.2 BOHR'S MODEL OF THE HYDROGEN ATOM

In order to explain the empirical results obtained by Rydberg Neils Bohr, in 1913, formulated a mode: of hydrogen atom utilizing classical physics and Planck's quantum theory. This semi-classical theory is based on the following three postulates.

Postulate I: An electron, bound to the nucleus in an atom can move around the nucleus in certain circular orbits without rad ating. These orbits are called the discrete stationary states of the atom.

Postulate II: Only those stationary orbits are allowed for which orbital angular momentum is equal to an integral multiple of  $\frac{\hbar}{2\pi}$  i.e.,

$$mvr = \frac{nh}{2\pi}$$
 (20.6)

where  $n = 1, 2, 3, \dots$  and n is called the principal quantum number, m and v are the mass and velocity of the orbiting electron respectively, and h is Planck's constant.

**Postulate III:** Whenever an electron makes a transition that is, jumps from high energy state *E*, to a lower energy state *E*, a photon of energy h *f* is emitted so that

$$hf = E_x - E_x$$
 ......... (20.7)

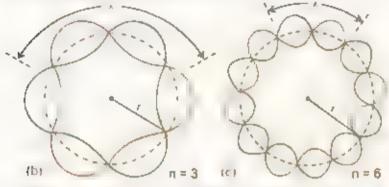
where  $f = c/\lambda$  is the frequency of the radiation emitted

# de-Broglie's Interpretation of Bohr's Orbits

At the time of formulation of Bohr's theory, there was no justification for the first two posturates, while Postulate III had some roots in Planck's thesis. Later on with the development of de Broglie's hypothesis, some justification could be seen in Postulate II as explained below:



Helium was identified in the Surusing spectroscopy before if was discovered on earth



Standing de Broglie waves of electrons around the discumierance of Bohr orbits. Consider a string of length  $\ell$  as shown in Fig. 20.3 (a). If this is put into stationary vibrations, we must have  $\ell = n \lambda$ , where n is an integer. Suppose that the string is bent into circle of radius r as demonstrated for n=3 and n=6 in Fig. 20.3 (b) and (c) so that

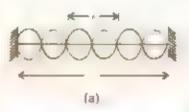


Fig. 20 Stationary wove for n = 3

$$\ell = 2\pi r = r\lambda$$

$$\lambda = \frac{2\pi r}{r} \qquad (20.8)$$

From de Broglie's hypothesis

OΓ

thus

$$\lambda = \frac{h}{\rho} = \frac{h}{mv}$$

$$\frac{h}{mv} = \frac{2\pi r}{h}$$

or  $mvr = \frac{n!}{2!}$ which is Postulate II



Consider a hydrogen atom in which electron moving with velocity  $v_n$  is in stationary circular orbit of radius  $r_n$ . From Eq. (20.6),

$$v_n = \frac{nh}{2\pi m r_n} \tag{20.9}$$

For this electron to stay in the circular orbit, shown in Fig. 20.4, the centripetal force  $F_c = \frac{mv_n^2}{r_n}$  is provided by the Coulomb's force  $F_+ = \frac{ke^2}{r_n^2}$ , where e is the magnitude of charge on electron as well as on the hydrogen nucleus consisting of a single proton. Thus,

$$\frac{m v_n^2}{r_n} = \frac{k \sigma^2}{r_n^2} \qquad (20.10)$$

where constant k is equal to  $\frac{1}{4\pi\epsilon_0}$ 

After substituting for v\_from Eq. 20.9 we have

$$r_{\rm c} = \frac{n^2 n^2}{4\pi^2 \text{ kme}^2} = n^2 r$$
 (20.11)

where 
$$r_{\rm c} = \frac{h^2}{4\pi^2 \, \text{kme}^2} = 0.053 \, \text{nm}$$

This agrees with the experimentally measured values and is called the first Bohr orbit radius of the hydrogen atom. Thus according to Bohr's theory, the radii of different stationary orbits of the electrons in the hydrogen atom are given by

$$r_n = r_1, 4r_1, 9r_1, 16r_2$$

Substituting the value of r, from Eq. 20.11 in Eq. 20.9, the speed of electron in the nth orbit is

$$v_n = \frac{2\pi ke^2}{nh}$$
 (20 12)



Proton

Fg 20 4

Electron

The first Both profit in the hypergan atom has a radius  $r_s = 5.3 \times 10^{10} m$ . The second and third Both profits have radii  $r_a = 4r_1$  and  $r_2 = 9r_2$  respectively.

Let us now calculate the total energy *E*, of the electron in the Bohr orbit, *E*, is the sum of the kinetic energy K E, and the potential energy U, i.e.

E. 
$$KE + U \frac{1}{2}mv + \frac{ke^2}{r_0}$$
 (20 13)

By rearranging Eq. (20.10), we get

$$\frac{1}{2}mv_n^2 = \frac{ke^2}{2r_n}$$
 (20 14)

then

$$\frac{1}{2} m v_n^2 = \frac{ke^2}{2 r_n}$$
 (20 14)  

$$E_r = \frac{ke^2}{2 r_n} \frac{ke^2}{r_n} = \frac{ke^2}{2 r_n}$$
 (20 15)

By substituting the value of r, from Eq. (20-11), we have

$$E_n = \frac{1}{n^2} \left( \frac{2\pi^2 k^2 me^4}{h^2} \right) = \frac{E_e}{n^2}$$
 (20.16)

where

$$E_a = \frac{2\pi^2 \text{ k}^2 me^4}{h^2} = \text{constant} = 13.6 \text{ eV}$$

which is the energy required to completely remove an electron. from the first Bohr orbit. This is called ionization energy. The ion zation energy may be provided to the electron by collision. with an external electron. The minimum potential through which this external electron should be accelerated so that it can supply the requisite ionization energy is known as ionization potential. Thus for n = 1, 2, 3,..... we get the allowed energy levels of a hydrogen atom to be

$$E_n = E_n - \frac{E_0}{4} - \frac{E_0}{9} - \frac{E_0}{16}$$

The experimentally measured value of the binding energy of the electron in the hydrogen atom is in perfect agreement with the value predicted by Bohr theory.

Normally the electron in the hydrogen atom is in the lowest energy state corresponding to n = 1 and this state is called the ground state or normal state. When it is in higher orbit, it is said to be in the excited state. The atom may be exited by collision with externally accelerated electron. The potential through which an electron should be accelerated so that, on collision it can lift the electron in the atom from its ground state to some higher state, is known as excitation potential.

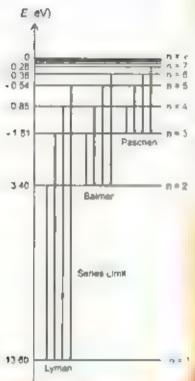
The results derived above for the energy levels along with Postulate III can be used to arrive at the expression for the wavelength of the hydrogen spectrum. Suppose that the electron in the hydrogen atom is in the excited state it with



The orbital electrons have specific amount of energies where as free electrons may have any amount of



Photon must have energy exactly equal to the energy difference between the two shells for excitation of an atom out an electron with K-E greater that the required difference can excite the gas atoms.



F in K Enempy level diagram for the hydrogen allom

energy  $E_a$  and makes a transition to a lower state p with energy  $E_a$ , where  $E_a < E_m$  then

$$E_{n} = \frac{E_{n}}{n^{2}} \quad \text{and} \quad E_{n} = \frac{F_{n}}{p^{2}}$$

$$h f = -E_{n} \cdot \frac{1}{n^{2}} \cdot \frac{1}{p^{2}}$$

Substituting for f = c D, and rearranging

$$\frac{1}{\lambda}$$
  $\frac{E_0}{hc}$   $\frac{1}{p^2}$   $\frac{1}{n^2}$ 

or  $\frac{1}{\lambda} \cdot R_H = \frac{1}{p^2} \cdot \frac{1}{n^2}$  (20 17)

where R<sub>n</sub> is the Rydberg constant given by the equation

$$R_{\rm m} = \frac{E_{\rm o}}{h c} = 1.0974 \times 10 \text{ m}$$
 (20.18)

which agrees well with the latest measured value for hydrogen atom.

Eq. 20.17 reduces to the empirical result derived by Rydberg and given by Eq. 20.1 provided that we substitute p = 2 and  $n = 3, 4, 5, \ldots$ . The different energy levels corresponding to Eq. 20.17 are shown in Fig. 20.5.

Example 20.1: Find the speed of the electron in the first Bohr orbit

#### Solution:

where

hence

The speed found from Eq. (20-12) with n = 1 is

$$v = \frac{2^{-1} \text{ke}^4}{\text{h}} = 2 \times 3.14 \times (9 \times 10^{8} \text{Nm C}) = \frac{(1.6 \times 10^{-19} \text{ C})^2}{6.63 \times 10^{-34} \text{ Js}}$$
  
 $v = 2.19 \times 10^{8} \text{ms}$ 

# 20.3 INNER SHELL TRANSITIONS AND CHARACTERISTIC X-RAYS

The transitions of electrons in the hydrogen or other light elements result in the emission of spectral lines in the infrared, visible or ultraviolet region of electromagnetic spectrum due to small energy differences in the transition levels.

In heavy atoms the electrons are assumed to be arranged in concentric she is labeled as K, L, M, N, O etc., the K shell being closest to the nucleus, the L shell next, and so on (Fig. 20.6). The inner shell electrons are tightly bound and large amount of energy is required for their displacement from their normal energy levels. After excitation, when an atom returns to its normal state photons of larger energy are emitted. Thus transition of niner shell electrons in heavy atoms gives his to the emission of high energy photons or X-rays. These X-rays consist of series of specific wavelengths or frequencies and hence are called characteristic X-rays. The study of characteristic X-rays spectra has played a very important role in the study of atomic structure and the periodic table of elements.

### Production of Kanas

Fig. 20.7 shows an arrangement of producing X-rays. It consists of a high vacuum tube called X-ray tube. When the cathode is heated by the flament Filt emits electrons which are accelerated towards the anode T. If V is the

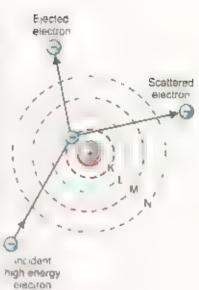
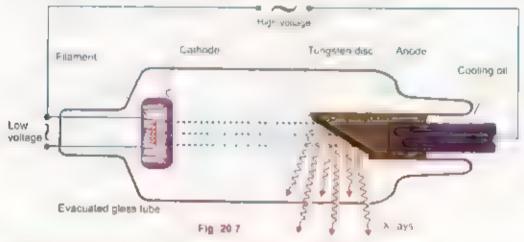


Fig 20 6



potential difference between C and T the kinetic energy K E with which the electron strike the target is given by

Suppose that these fast moving electrons of energy Ve strike a target made of tungsten or any other heavy element. It is possible that in collision, the electrons in the innermost she is such as K or . will be knocked out. Suppose that one of the electrons in the K shell is removed, thereby producing a vacancy or hole in that shell. The electron from the L shell.

jumps to occupy the hole in the K shell, thereby emitting a photon of energy h f, called the K, X-ray given by

$$h f_{k} = E_1 - E_k$$
 (20.20)

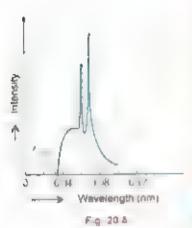
it is also possible that the electron from the M shell might also jump to occupy the hole in the K shell. The photons emitted are K, X-ray with energies.

$$h f_{kd} = E_{kl} - E_{kl}$$
 (20.21)

these photons give rise to K<sub>a</sub> X-ray and so on.

The photons emitted in such transitions ie noer shell transitions are called characteristic X-rays because their energies depend upon the type of target material.

The holes created in the L and M shells are occupied by transitions of electrons from higher states creating more X-rays. The characteristic X-rays appear as discrete tines on a continuous spectrum as shown in Fig. 20.8.



The continuous spectrum is due to an effect known as bremsstrahlung or braking radiation. When the fast moving

bremsstrahlung or braking radiation. When the fast moving electrons bombard, the target, they are suddenly slowed down on impact with the target, we know that an accelerating charge, emits electromagnetic radiation. Hence, these impacting electrons emit radiation as they are strongly decelerated by the target. Since the rate of deceleration is so large, the emitted radiation correspond to short wavelength and so the bremsstrahlung is in the X-ray region in the case when the electrons lose all their kinetic energy in the first coils on the entire kinetic energy appears as a X-ray photon of energy hi<sub>mat</sub> i.e.,

The wavelength / ... in Fig. 20.8 corresponds to frequency f... Other electrons do not lose all their energy in the first collision. They may suffer a number of collisions before coming to rest. This will give use to photons of smaller energy or X-rays of longer wavelength. Thus the continuous spectrum is obtained due to deceleration of impacting electrons.

# Properties and Uses of X-sa

X-rays have many practical applications in medicine and industry Because X-rays can penetrate several cent metres

into a solid matter so they can be used to visualize the interiors of the materials opaque to ordinary light, such as fractured bones or defects in structural steel. The object to be visualized is placed between an X-ray source and a large sheet of photographic film, the darkening of the film is proportional to the radiation exposure. A crack or air bubble allows greater amount of X-rays to pass. This appears as a dark area on the photographic film. Shadow of bones appears lighter than the surrounding flesh. It is due to the fact that bones contain greater proportions of elements with high atomic number and so they absorb greater amount of incident X-rays than flesh. In flesh, light elements like carbon, hydrogen and oxygen predominate. These elements allow greater amount of incident X-rays to pass through them.

# GATI-Scanner

In the recent past, several vastly improved X-ray techniques have been developed. One widely used system is computerized axial tomography, the corresponding instrument is called CAT-Scanner. The X-ray source produces a thin fan-shaped beam that is detected on the opposite side of the subject by an array of several hundred detectors in a line. Each detector measures absorption of X-ray along a thin line through the subject. The entire apparatus is rotated around the subject in the plane of the beam during a few seconds. The changing reactions of the detector are recorded digitally, a computer processes this information and reconstructs a picture of different densities over an entire cross section of the subject. Density differences of the order of one percent can be detected with CAT-Scans Tumors, and other anomalies much too small to be seen with older techniques can be detected.

# Blological Wilesto of it my

X-rays cause damage to living tissue. As X-ray photons are absorbed in tissues, they break molecular bonds and create highly reactive free radicals (such as. H and OH), which in turn can disturb the molecular structure of the proteins and especially the genetic material. Young and rapidly growing cells are particularly susceptible; hence X-rays are useful for selective destruction of cancer cells. On the other hand a cell may be damaged by radiation but survive, continue dividing and produce generation of defective cells. Thus X-rays can cause cancer Even when the organism itself shows no apparent damage, excessive

# C Puis Marie Informatibiliti



An X-ray picture of a hand.

# adinteresting informations



In CAT scanning a "lanned-out" array of X-ray beams is directed through the patient from a number of different counts soon.







(a) This two-dimensional (AT scan of a brain reveals a Tigo into a tumor colored police. Three dimensional and the Standard Reveals are the A available and this tight of the property of the Standard Reveals are the standard Reveals and the standard Reveals are the company of the standard Reveals and the standard Reveals are desired.

radiation exposure can cause changes in their productive system that will affect the organism's offspring

# 20.4 UNCERTAINTY WITHIN THE ATOM

One of the characteristics of dual nature of matter is a fundamental limitation in the accuracy of the simultaneous measurement of the position and momentum of a particle

Heisenberg showed that this is given by the equation

$$\Delta p \Delta x \ge \frac{h}{2\pi}$$

However, these limitations are significant in the realm of atom. One interesting question is whether electrons are present in atomic nuclei. As the typical nuclei are less than 10 <sup>14</sup> m in diameter for an electron to be confined within such a nucleus the uncertainty in its position is of the order of 10 <sup>14</sup> m. The corresponding uncertainty in the electron's momentum is

$$\Delta p \ge \frac{h}{\Delta x}$$

$$\frac{6.63 \times 10^{-34} \text{ Js}}{10^{-14} \text{ m}} = 6.63 \times 10^{-30} \text{ kg ms}^{-1}$$

As  $\Delta p = m \Delta v$ Hence  $\Delta v = \frac{6.63 \times 10^{-20} \text{ kg ms}^{-1}}{9.11 \times 10^{-31} \text{ kg}} \ge 7.3 \times 10^{10} \text{ ms}$ 

Hence for the electron to be confined to a nucleus its speed would have to be greater than 10 ms. Let greater than the speed of Ight. Because this is impossible, we must conclude that an electron can never be found inside of a nucleus. But can an electron reside inside the atom? To find this we again calculate the speed of an electron and if it turns to be less than the speed of light, we have reasonable expectation of finding the electron within the atom but outside the nucleus. The radius of the hydrogen atom is about 5 x 10 m. Applying the uncertainty principle to the momentum of electron in the atom we have.

As  $\Delta p \ge \frac{h}{\Delta x}$ As  $\Delta p = m \Delta v$ Therefore  $\Delta v = \frac{h}{m \Delta x}$ 

For an atom Axis given as 5 x 10 m

$$\Delta V = \frac{6.63 \times 10^{-34} \text{ Js}}{9.11 \times 10^{-31} \text{kg} \times 5 \times 10^{-11} \text{ m}}$$

 $= 1.46 \times 10^7 \, \text{ms}^{-1}$ 

This speed of the electron is less than the speed of light therefore it can exist in the atom but outside the nucleus

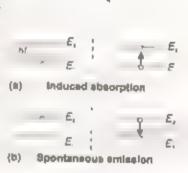
# 20.5 LASER

Laser is the acronym for Light Amplification by Stimulated Emission of Radiation. As the name indicates lasers are used for producing an intense monochromatic and undirectional coherent beam of visible light. To understand the working of a laser terms such as stimulated emission and population inversion must be understood.

# Spontaneous and Otherstand Contactoris

Consider a sample of free atoms some of which are in the ground state with energy E and some in the excited state E, as shown in Fig. 20.9. The photons of energy hf = E - E are incident on this sample. These incident photons can interact with atoms in two different ways. In Fig. 20.9 (a) the incident photon is absorbed by an atom in the ground state E, thereby leaving the atom in the excited state E. This process is called stimulated or induced absorption. Once in the excited state two things can happen to the atom. (i) It may decay by spontaneous emission as shown in Fig. 20.9 (b), in which the atom emits a photon of energy hf = E, E in any arbitrary (b) direction.

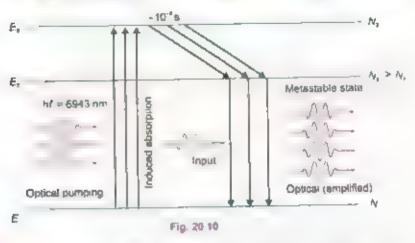
The other alternative for the atom in the excited state E, is to decay by stimulated or induced emission as shown in Fig 20.9 (c). In this case the incident photon of energy (c) in f = E, -E induces the atom to decay by emitting a photon that travels in the direction of the incident photon. For each incident photon, we will have two photons going in the same direction thus we have accomplished two things an amplified as well as a unidirectional coherent beam. From a practical point, this is possible only if there is more stimulated or induced emission than spontaneous emission. This can be achieved as described in the next section.





Induced emission

Let us consider a simple case of a material whose atoms can reside in three different states as shown in Fig. 20.10 state.





(a) Normal population

A normal population of atomic energy state, with more atomic in the lower energy state E, than in the excited state E,...



(b) Population Inversion

A population invention, in which the higher energy state has a greater population than the lower energy state

E which is ground state, the excited state E in which the atoms can reside only for 10 is and the metastable state E in which the atoms can reside for ~10 %, much longer than 10 s A metastable state is an excited state in which an excited electron is unusually stable and from which the electron spontaneously fails to lower state only after relatively longer time. The transition from or to this state are difficult as compared to other excited states. Hence instead of direct excitation to this state, the electrons are excited to higher level for spontaneous fall to metastable state. Also let us assume that the incident photons of energy h f = E - Eraise the atom from the ground state E to the excited state Ebut the excited atoms do not decay back to E. Thus the only alternative for the atoms in the excited state E is to decay spontaneously to state E the atoms reach state E much faster than they leave state E. This eventually leads to the situation that the state E, contains more atoms than state E This situation is known as population inversion

Once the population inversion has been reached the lasing action of a laser is simple to achieve. The atoms in the metastable state  $E_z$  are bombarded by photons of energy  $hf = E_z - E_z$ , resulting in an induced emission, giving an intense, coherent beam in the direction of the incident photon.

The emitted photons must be confined in the assembly long enough to stimulate further emission from other excited atoms. This is achieved by using mirrors at the two ends of the assembly. One end is made totally reflecting, and the other end is partially transparent to allow the laser beam to escape (Fig 20 11). As the photons move back and forth between the reflecting mirrors they continue to stimulate other excited atoms to emit photons. As the process continues the number of photons multiply and the resulting radiation is, therefore much more intense and coherent than light from ordinary sources.

# Completely singred murror

Fig. 20 11

# Muhum - Neon

It is a most common type of lasers used in physics laboratories. Its discharge tube is filled with 85% helium and 15% neon gas. The neon is the lasing or active medium in this tube. By chance, helium and neon have nearly identical metastable states respectively ocated 20.61 eV and 20.66 eV level. The high voltage electric discharge excites. the electrons in some of the helium atoms to the 20 61 eV state. In this laser, population inversion in neon is achieved by direct collisions with same energy electrons of helium atoms. Thus excited heiturn atoms collide with neon atoms. each transferring its own 20 61 eV of energy to an electron in the neon atom along with 0.05 eV of K.E. from the moving atom. As a result, the electrons in neon atoms are raised to the 20.66 eV state in this way a population inversion is sustained in the neon gas relative to an energy level of 18 70 eV Sponlaneous emission from neon atoms initiate aser action and stimulated emission causes electrons in the neon to drop from 20 66 eV to the 18 70 eV level and red laser light of wavelength 632.8 nm corresponding to 1.96 eV energy is generated (Fig. 20.12).

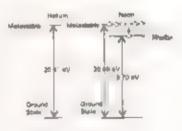


Fig. 20 12

# Here's in the Medicine and Industry

- Laser beams are used as surgical tool for "welding" detached retinas
- The narrow intense beam of laser can be used to destroy tissue in a localized area. Tiny organelles with a living cell have been destroyed by using laser to study how the absence of that organelle affects the behavior of the cell
- Finely focused beam of laser has been used to destroy cancerous and pre-cancerous cell





The helium-neon laser beam is being used to diagnose diseases of the eye. The use of aser technology is this field of ophthalmology is wilespread.

- The heat of the laser sea's off capitaines and lymph vessels to prevent spread of the disease
- The intense heat produced in small area by a laser beam is also used for welding and machining metals and for drilling tiny holes in hard meterials
- The precise straightness of a laser beam is also useful to surveyors for lining up equipment especially in maccessible locations
- It is potential energy source for inducing fusion reactions
- It can be used for telecommunication along optical fores
- 9 Laser beam can be used to generate threedimensional images of objects in a process called holography



- When an atomic gas or vapours at less than atmospheric pressure is suitably
  excited usually by passing electric current through it the emitted radiation has a
  spectrum which contains certain specific wavelenghts only.
- Postulates of Bohr's model of hydrogen atom are

4

An electron bound to the nucleus in an atom can move around the nucleus in certain circular orbits without radiating. These orbits are call the discrete stationary states of the atom.

- Only those stationary states are allowed for which orbital angular momentum is equal to an integral multiple of hi.e.,  $mvr = \frac{nh}{2\pi}$
- Whenever an electron makes a transition e jumps from high energy state E, to a lower energy state E, a photon of energy h is emitted so that hI E E.
- The transition of electrons in the hydrogen or other light elements result in the
  emission of spectral lines in the infrared visible or ultraviolet region of
  electromagnet dispectrum due to small energy differences in the transition levels.
- The X rays emitted in inner shell transitions are called characteristic X-rays, because their energy depends upon the type of target material
- The X-rays that are emitted in all directions and with a continuous range of frequencies are known as continuous X-rays.
- Laser is the acronym for Light Amplification by Stimulated Emission of Radiation

The incident photon absorbed by an atom in the ground state E -thereby leaving the atom in the excited state E is called stimulated or induced absorption

Spontaneous or induced emission is that in which the atom emits a photon of energy  $hf = E_1 + E_2$  in any arbitrary direction.

Stimulated or induced emission is that in which the incident photon of energy  $h f = E_2 - E$  induces the atom to decay by emitting a photon that travels in the direction of the notident photon. For each incident photon, we will have two photons going in the same direction giving use to an amplified as well as a unidirectional coherent beam.

# QUESTIONS

- 20.1 Bohr's theory of hydrogen atomis based upon several assumptions. Do any of these assumptions contradict classical physics?
- 20.2 What is mean! by all ne spectrum? Explain how line spectrum can be used for the identification of elements?
- 20.3 Can the electron in the ground state of hydrogen absorb a photon of energy 13.6 eV and greater than 13.6 eV?
- 20.4 How can the spectrum of hydrogen contain so many lines when hydrogen contains one electron?
- 20.5 Is energy conserved when an atom emits a photon of I ght?
- 20.6 Explain why a glowing gasig vesionly certain wavelengths of light and why that gas is capable of absorbing the same wavelengths? Give a reason why it is transparent to other wavelengths?
- 20.7 What do we mean when we say that the atom is excited?
- 20.8 Can X-rays be reflerted refraction diffracted and polarized just like any other waves? Explain
- 20.9 What are the advantages of lasers over or unary right?
- 20.10 Explain why laser action could not occur without population inversion between atomic levels?

# PROBLEMS

20.1 A hydrogen atoms is in its ground state (n = 1). Using Behr's theory, calculate (a) the radius of the orbit (b) the Linear momentum of the electron (c) the angular momentum of the electron (d) the kinetic energy (e) the potential energy and (f) the total energy.

[Ans: (a) 0 529 x 10 °m (b) 1 99 x 10 " kg ms '(c) 1 05 x 10 " kg m s (d) 13.6 eV (e) - 27.2 eV (f) -13.6 eV)

- 20.2 What are the energies in eV of quanta of wavelength? > 400, 500 and 700 nm (Ans. 3.10 eV, 2.49 eV, 1.77 eV)
- 20.3 An electron jumps from a level E = -3.5 x 10 \*\* J to E, = 1.20 x 10 \*\* J. What is the wavelength of the emitted light? (Ans: 234 nm)
- Find the wavelength of the spectral line corresponding to the transition in hydrogen from n = 6 state to n = 3 state?

(Asn: 1094 nm)

- 20.5 Compute the shortest wavelength radiation in the Baimer senes? What value of n must be used? (Ans: 364.5 nm, n = ∞)
- A 6 Calculate the longest wavelength of radiation for the Paschen series (Ans: 1875 nm)
- Electrons in an X-ray tube are accelerated through a potential difference of 3000 V If these electrons were slowed down in a target, what will be the minimum wavelength of X-rays produced?

  (Ans. 4.14 x 10 ° m)
- 20.8 The wavelength of K X-ray from copper is 1.377 x 10 in. What is the energy difference between the two levels from which this transition results?
  (Ans: 9.03 keV)
- Atungsten target is struck by electrons that have been an electated from rest through 40 kV potential difference. Find the shortest wavelength of the bremsstrahlung radiation emitted.

  (Ans. 0.31 x 10 m.)
- 20.10 The orbital electron of a hydrogen atom moves with a speed of 5.456 x 10 ms (a) Find the value of the quantum number in associated with this electron
  - (b) Calculate the radius of this orbit.
  - (c) Find the energy of the electron in this orbit

(Ans: n = 4,  $r_s = 0.846$  nm;  $E_s = -0.85$  eV).

# Chapter 21

# **NUCLEAR PHYSICS**

# **Learning Objectives**

At the end of this chapter the students will be able to:

- Understand the qualitative treatment of Rutherford's scattering experiment and the evidence it provides for the existence and small size of nucleus.
- 2 Distinguish between nucleon number (mass number) and atomic number
- Understand that an element can exist in various isotopic forms each with a different number of neutrons
- 4 Understand the use of mass spectrograph to demonstrate the existence of isotopes and to measure their relative abundance
- 5 Understand mass defect and calculate binding energy using Einstein's equation
- ibustrate graphically the variation of binding energy per nucleon with the mass number
- 7 Appreciate the sponteneous and random nature of nuclear decay
- Explain the meaning of half-life.
- 9 Recognize and use decay law.
- 10 Understand and describe the interaction of nuclear radiation with matter
- Understand the use of Wilson cloud chamber, Ge ger Mulier counter and solid state detectors to detect the radiations
- 12 Appreciate that atomic number and mass number conserve in nuclear process
- 13 Describe energy and mass conservation in simple reactions and in radioactive decay.
- 14. Understand and describe the phenomena of nuclear fission and nuclear fusion.
- Explain the working principle of nuclear reactor.
- Be aware of various types of nuclear reactors.
- 17 Show an awareness about nuclear radiation exposure and biological effects of radiation
- 18 Describe in simple terms the use of radiations for medical diagnosis and therapy
- 19 Understand qualitatively the importance of limiting exposure to ion 2 ng rad at on
- 20 Outline the use of tracer technique to obtain diagnostic information about internal structures
- 21 Describe examples of the use of radioactive tracers in diagnosis
- 22. Describe basic forces of nature
- 23 Describe the modern view of the building blocks of matter based on hadrons, leptons and quarks.

Soon after the discovery of electron and proton in an atom the quest started to find the way in which these charged particles are present in an atom. From his experiments Ernest Rutherford developed a nuclear mode of the atom his mode of the atom consisted of a small dense positively charged nucleus with negative electrons orbiting about it in 1920 Rutherford suggested that there is probably another particle within the nucleus ineutral one to which he gave the name neutron. James Chadwick discovered neutron in 1932.

# Negative electron

Paricips scattering experiments to discuss the participal concluded that most of the participal ties at a some size of the size of the participal ties at a some size of the siz

nucleus

#### 21.1 ATOMIC NUCLEUS

At the centre of each and every atom there is an infinites mally small nucleus. The entire positive charge of the atom and about 99.9 percent of its mass is concentrated in the nucleus. The tin ness of the nucleus can be imagined by companing that the radius of the atom is 10° times the radius of the nucleus.

A nucleus consists of nucleons comprising of protons and neutrons. A proton has a positive charge equal to 1.6 x 10 °C and its mass is 1.673 x 10 °Kg. A neutron has no charge on it, but its mass is 1.675 x 10 °Kg. The mass of a neutron is a most equal to mass of proton. To indicate the mass of atomic particles instead of kilogram unified mass scale (u) is generally used. By definition 10 is exactly one twelveth the mass of carbon, atom. 10 = 1.6606 x 10 °Kg) In this unit the mass of a proton is 1.007276 u and that of a neutron is 1.008665 u while that of an electron is 0.00055 u.

The charge on a proton is equal in magnitude to the charge on an electron. The charge on the proton is positive while that of an electron is negative. As an atom on the whole is electrically neutral, therefore, we can conclude that the number of protons inside the nucleus is equal to the number of electrons outside the nucleus. The number of protons inside a nucleus is called the atomic number or the charge number of an atom. It is denoted by Z. Thus the total charge of any nucleus is Zellhere eliminates charge on one proton.

The combined number of all the protons and neutrons in a nucleus is known as its mass number and is denoted by A

The number of neutrons N present in a nucleus is given by

$$N - (A \cdot Z) \tag{21.1}$$

We now consider different elements of the periodic table. Hydrogen atom is simplest of all the atoms. Its nucleus is composed of only one proton that is for hydrogen A = 1. Z = 1 That is why hydrogen is represented by the symbol .H Next in the periodic table after the hydrogen element is the helium element. Its nucleus contains two protons and two neutrons. This means for helium A = 4 and Z = 2, and hence helium is represented as 'He. We now take the example of uranium - a heavy element of the periodic table. The charge number Z of uranium is 92 while its mass number A is 235. This is represented as 235 J It has 92 protons while the number of neutrons N is given by the equation N = A - Z = 235 - 92 = 143. In this way the number of protons and neutrons in atoms of all the elements of the periodic table can be determined. It has been observed that the number of neutrons and protons in the initial light elements of the periodic table is almost equal but in the later heavy elements the number of neutrons is greater than the number of protons in the nucleus.

#### 21.2 ISOTOPES

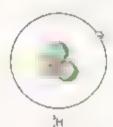
Isotopes are such nuclei of an element that have the same charge number Z but have different mass number A, that is in the nucleus of such an element the number of protons is the same, but the number of neutrons is different, Helium, for example has two isotopes. These are symbolically represented as 3He and 1He. As the charge number of henum is 2, therefore, there are two protons in the helium nucleus. The neutron number of the first sotope is according to Eq. 21.1 is  $3 \cdot 2 = 1$  and that in the second isotope. He, the number of neutron is 4 - 2 = 2. Hydrogen has three isotopes represented by "H "H H Its first isotope is called ordinary hydrogen or protium. There is only one proton in its nucleus. The second isotope of hydrogen is called deutenum. It has one proton and one nautron in its nucleus. Its nucleus is called deuteron. The third isotope of hydrogen has two neutrons and one proton in its nucleus and it is called tritium. The isotopes of hydrogen are shown in Figs. 21.1 (a.b.c.).

The chemical properties of ail the isotopes of an element are alike as the chemical properties of an element depend only upon the number of electrons around the nucleus, that is upon the charge number Z which for all the isotopes of an element sithe same. It is therefore not possible to separate the isotopes of an element by chemical methods. Physical methods are found to be successful. for this purpose. A





,b (Deutenum,



(c) (Tribum) Fig. 21 1



Both Kenon and caesium each have in satoyes



Some atomic masses

Particie	Mass (u)		
8	0.00055		
n	1 008655		
н	1 007276		
*H	2 314102		
*H	3 01605		
*He	3 0 603		
'Ha	+ 002603		
" <u>L</u> 1	7 016004		
"Be	10 013534		
14/4	14 0031		
10	18 9991		

device with the help of which not only the isotopes of any element can be separated from one another but their masses can also be determined quite accurately is called mass spectrograph.

# And the second second second second

A simple mass spectrograph is shown in Fig. 21.2 (a) The atoms or molecules of the element under investigation, in vapour form, are ionized in the ions source S. As a result of ionization one electron is removed from the particle lieaving with a net positive charge +e. The positive ions, escaping the slit. S. are accelerated through a potential difference. V applied between the two slits S. and S<sub>2</sub>.

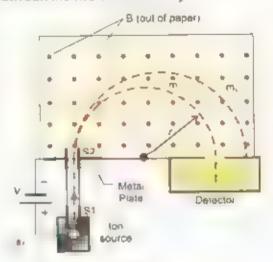


Fig. 21.2

The ions pass through the slit  $S_z$  in the form of a narrow beam. The K.E. of singly charged ion at the slit  $S_z$  will be given by

$$\frac{1}{2}mv^2 = Ve$$
 ...... (21.2)

The ions are then subjected to a perpendicular and uniform magnetic field B in a vacuum chamber, where they are deflected in semicircular paths towards a detector. The detector records the number of one arriving per second. The centripetal force applied by the magnetic field is given by

$$Bev = \frac{mv^2}{r}$$

$$m = \frac{Ber}{v}$$
(21.3)

OΓ

Substituting the values of v from Eq. 21.2, we get

$$m = \left(\frac{\theta r^2}{2V}\right) B^2 \qquad \dots \tag{21.4}$$

The above equation shows that the mass of each ion reaching the detector is proportional to B'. By adjusting the value of B and keeping the term in the parentheses constant, ions of different masses are allowed to enter the detector A graph of the detector output as a function of B' then gives an indication of what masses are present and the abundance of each mass.

Fig. 21.2 (b) shows a record obtained for naturally occurring neon gas showing three isotopes whose atomic mass numbers are 20.21 and 22. The larger is the peak, the more abundant is the isotope. Thus most abundant isotope of neor is neon-20.

# 21.3 MASS DEFECT AND BINDING ENERGY

It is usually assumed that the whole is always equal to the sum of its parts. This is not so in the nucleus. The results of experiments on the masses of different nucleus show that the mass of the nucleus is always less than the total mass of all the protons and neutrons making up the nucleus. In the nucleus the missing mass is called the mass defect migreen by

$$\Delta m = Z m_o + (A - Z) m_o - m_{matter}$$
 ......... (21.5)

As Z is the total number of protons in the nucleus and  $m_p$  is the mass of a proton, then  $Zm_p$  is the total mass of all the protons. As shown in Eq. 2.1.1 (A - Z) is the total number of neutrons and as  $m_p$  is the mass of a single neutron, (A - Z)  $m_p$  is the total mass of all the neutrons. The term  $m_{new}$  is the experimentally measured mass of the entire nucleus. Hence, Eq. 21.5 represents the difference in mass between the sum of the masses of its constituents and the mass of the nucleus itself.

The missing mass is converted to energy in the formation of the nucleus. This energy is found from Einstein's mass energy relation

$$E = (\Delta m) c^2 \qquad \dots (21.6)$$

and is called the binding energy (B E ) of the nucleus. From equations 21.5 and 21.6, the binding energy of a nucleus is

$$B E_{r} = (\Delta m) c^{2} = Z m_{b} c^{2} + (A - Z) m c^{2} - m c^{2} \dots$$
 (21.7)

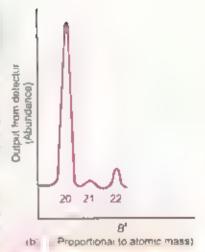


Fig 21.2 The mass spectrum of naturally occurring mean showing three isotopes whose atomic mass becare 20.21 and 22. The larger the peak, the more abundant the various.

Let us consider the example of the deuteron nucleus to make the concept of mass defect and binding energy more clear

**Example 21.1:** Find the mass defect and binding energy of the deuteron nucleus. The experimental mass of deuteron is 3 3435 x 10 1 kg.

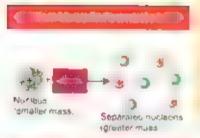
#### Solution:

Using equation 21.5, we get the mass defect of deuteron as

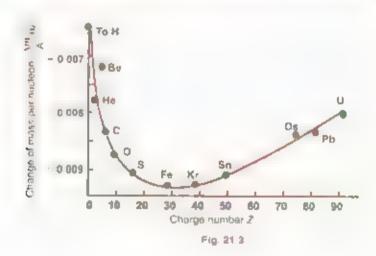
$$m = m + m_r - m_p$$

The B E of deuteron as found from Eq. 21.6 s.  $\Delta m.c$ .  $\Delta m.c' = 3.9754 \times 10^{3} \, \text{kg} \times (3 \times 10^{3} \, \text{ms}) = B.E = 3.5729 \times 10^{3} \, \text{J}$ . To express the result in eV units divide the B.E. obtained in joules by 1.6 x 10 . J. Thus

Therefore the bound constituents have less energy than when they are free. That is the B.E. comes from the mass that is lost in the process of formation. Conversely the binding energy is the amount of energy that must be supplied to a nucleus if the nucleus is to be broken up into protons and neutrons. Experiments have revealed that such mass defects exist in other elements as well. Shown in Fig. 21.3 is a graph between the mass defect per nucleon and charge



Freegy must be as police to him his micro-s apart into its constituted protor's and residences



number Z is obtained by finding the difference of mass between the total mass of all the protons and neutrons that form the nucleus and the experimental mass of the nucleus and dividing this difference by mass number A i.e.

Mass defect per nucleon

$$\frac{\Delta m}{A} = \frac{m_{\text{nucleum}} - [Zm_p + (A - Z)m_n]}{A}$$

where  $\Delta m$  is the mass defect. From the definition of mass defect it is quite obvious that for hydrogen, mass defect is zero. The mass defect is made clear with Einstein's equation  $E = \Delta mc$ . This equation shows that if for any reason a mass  $\Delta m$  is lost, them it is converted into energy

Let us now calculate the BE of helium. For 2He

$$\Delta m = 2 m_u + 2 m_{e^+} m_{ee}$$
  
= 2 01519 u + 2 01796 u - 4 00281 u = 0 03034 u

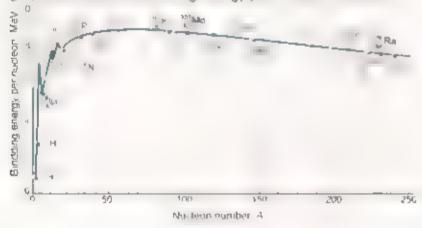
since 1 u=1 66 x 10 27 kg

$$\Delta m = 0.03034 \text{ u.x.} 1.66 \text{ x.} 10^{27} \text{ kgu}^{1} = 5.03 \text{ x.} 10^{28} \text{kg}$$
Thus
$$B E = 1 \text{ kmc} = 5.03 \text{ x.} 10^{-6} \text{kg.} \text{ y.x.} 10^{-6} \text{m/s.}^{2}$$

= 
$$4.5 \times 10^{-12} J = \frac{4.5 \times 10^{-12} J}{1.6 \times 10^{-10} J (eV)^{-1}} = 2.82 \times 10^7 eV = 28.2 MeV$$

This means that when two protons and two neutrons fuse together to make helium nucleus, if an amount of 28.2 MeV energy is given to the helium nucleus then it breaks up into two protons and two neutrons. From this, we conclude that

In this way we can calculate binding energy of every element. Shown in Fig. 21.4 is a graph between binding energy per nucleon and the mass number of different elements. This graph shows that the binding energy per nucleon increases.



Ph 21.4

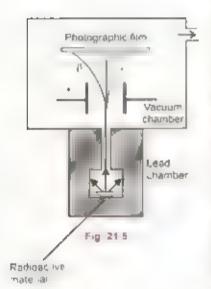
with the mass number till it reaches a maximum value of 8.8 MeV at mass number 58 and then it gradually decreases to a value of 7.6 MeV at mass number 238. The binding energy per nucleon is maximum for iron. This shows that of all the elements iron is the most stable element. Later in this chapter it will be shown with the help of graph of Fig. 21.4 that when heavy element breaks into lighter elements or the lighter elements are fused to form heavier element then a large amount of energy can be obtained.

# 21.4 RADIOACTIVITY

It has been observed that those elements whose charge number Z is greater than 82 are unstable. Some invisible radiations, that can affect the photographic plates emanate out of these elements. Such elements are called radioactive and the phenomenon is called radioactivity. The radiations coming out of the radioactive element are called a pha  $(\alpha)$  beta  $(\beta)$  and gamma  $(\alpha)$  radiation. Radio. Taily was discovered by Henri Becquerel in 1896. He found that an one containing uranium (Z=92) emits an invisible radiation that penetrates through a black paper wrapping a photographic plate and affects the plate. After Becquerel's discovery Marie Curie and Pierre Curie discovered two new radioactive elements that they called polonium and radium.

The analysis of the radiations emanating out of a radioactive material can be carried out by a simple experiment. The radioactive material is placed at the centre of a block of lead by drilling a hole in the block. Radioactive rad ations enter a vacuum chamber after emerging out of this hole. After passing between the two parallel plates the rad at onsistince a photographic plate. These lad at ons, instead of impinging at one point fail at three different points due to the potential difference between the plates (Fig. 21.5).

From this experiment I can be concluded that all radiations from the radioactive material are not alike. The radiation that bends towards the negative plate is made up of positively charged particles. These are called  $\alpha$ -particles. Those radiations that bend towall is the positive plate are composed of negatively charged particles. These are called  $\beta$ -particles. Those radiations that go straight without bending have no



charge on them. These are called y-rays.

Further experiments reveal that α-particles are helium nuclei. The charge on them is +2e while their mass is 4u (atomic mass unit) that is every α-particle has two protons and two neutrons in it. β-particles are in fact fast moving electrons which come out of the nucleus of a radioactive element γ-rays like X-rays, are electromagnetic waves which issue out of the nucleus of a radioactive element. The wavelength of these rays is much shorter, compared with the wavelength of X-rays.

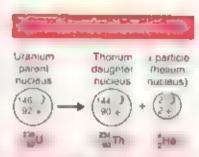
Radioactivity is purely a nuclear phenomenon. This is not affected by any physical or chemical reaction. Whenever any particle / radiation is emitted out of any radioactive element, it is always accompanied by some changes in the nucleus of the element. Therefore, this element changes into a new element. This phenomenon is called radioactive decay. The element formed due to this change is called daughter element. The original element is called the parent element. During the nuclear changes the laws of conservation of mass, energy, momentum and charge remain applicable.

We know that three types of radiations  $\alpha$ -particle [i-particle and  $\gamma$ -rays are emitted by the naturally occurring radioactive elements. When  $\alpha$ -particle is emitted out of any nucleus then due to law of conservation of matter, the mass number of the nucleus decreases by 4, and due to law of conservation of charge the charge of the nucleus decreases by a magnitude of  $2\sigma$  is the charge number of the nucleus decreases by 2. It is due to the fact that the mass number and charge number of the emitted particle  $\alpha$  is 4 and 2 respectively. The emission of the  $\alpha$ -particle is represented by the following equation

Here X represents the parent and Y the daughter element

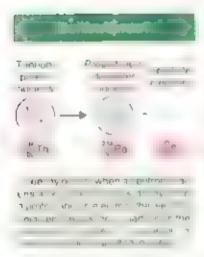
To explain the emission of  $\alpha$ -particles we take the example of radium <sup>226</sup><sub>88</sub>Ra. The emission of an  $\alpha$ -particle from radium 226, results in the formation of radion gas <sup>224</sup><sub>88</sub>Rn. This change is represented by the following equation

It may be remembered that the sum of the mass numbers and the charge numbers on both sides of the



decay occurs when an unstable paren nucleus emits an a pai inte ons the process it surveited into a different or laughter nucleus.





equation are equal. When a β-particle is emitted out of any nucleus, then its mass number does not undergo any change but its charge number increases by one. The emission of a β-particle from any element X is represented by the following equation.

Negative β-particle is an electron and its emission from the nucleus becomes an incomprehensible enign a, as there is no electron present in the nucleus. However, the emission of electron from the nucleus can be thought of as a neutron emitting an electron and becoming a proton, although the modern explanation is not that simple

This means that the B-particle is formed at the time of emission. That is why at the time of emission of a B-particle the charge number of the nucleus increases by one but no change in its mass number takes place as the mass of electron is exceedingly small as compared to the mass of a proton or a neutron. The transformation of an electron a the moment of its emission is given below by an equation.

It has been observed that the intermediate of the entire on of the action.

The following equation recresents the eaction.

The following equation recresents the eaction.

When a y-radiation issues out of nucleus then neither the charge number Z not the mass number A of the nucleus undergoes any change. It is due to the fact that a y-radiation is simply a photon that has neither any charge nor any mass. Its emission from the nucleus has some resemblance with the emission of a photon of light from an atom. We know that when any electron of an atom absorbs energy it jumps from the ground state to a higher energy state and the atom becomes excited. When the electron of his excited at a same way the research of the same way the research of the same way the research of the same way unstable, state

The emission of y-radiation from a nucleus is generally represented by this equation

excited state.

Here  $\frac{A}{Z}X^{*}$  represents an excited nucleus while  $\frac{A}{Z}X$  shows ground state of the nucleus

#### 21 5 HALFLIFE

We have seen that whenever an α or β-particle is emitted from a rad pactive element. It is transformed into some other element. This rad pactive decay process is quite random and is not subjected to any symmetry. This means that we cannot foretell about any particular atom as to when will it decay. It could decay immediately or it may remain unchanged for the max or year This we cannot have any one at the life of any particular atom of a radioactive element.

Let us take the example of a city with a population of one million and we know that on the average ten person die every day. Even with this knowledge we cannot say with certainty that which particular person will die on which particular day We can only say that on the whole ten person will die. The o to the edulation such predictions. Like the population of a city, it is not possible to talk about an atom of a radioactive element. For more accurate result we always talk about large groups of atoms and laws of statistics are applied upon them. Let us suppose that we bring a group of 100,000 atoms under consideration and wait till such time that half of these i.e. Sa in a chi prin serape el The time sia lad the half-life T, of this element. If the half-life of the said element be one day, then after one day only 25,000 atoms will remain behind and after two days 12 500 atoms will remain behind. That is with the passage of every one day, the number of atoms remaining behind becomes half of the number aready present. This example provides us the definition of half-life of a radioactive element i.e.

The half life To of a radioactive element is that period in which half of the atoms decay

Besides getting the definition of half-life we can deduce two other conclusions from this example. These are, firstly no radioactive element can completely decay. It is due to the life in this way an infinite time is required for all the atoms to decay.

Secondly, the number of atoms decaying in a particular period is proportional to the number of atoms present in the beginning of the period. If the number of atoms to start with is large then a large number of atoms will decay in this period and if the number of atoms present in the beginning is small then less atoms will decay.

We can represent these results with an equation if at any particular time the number of radioactive atoms be N, then in an interval  $\Delta t$  the number of decaying atom,  $\Delta N$  is proportionate the time interval  $\Delta t$  and the number of atoms N, i.e.,

$$\Delta N \propto -N \Delta t$$

or 
$$\Delta N = -\lambda N \Delta t$$
 ........ (21.8)

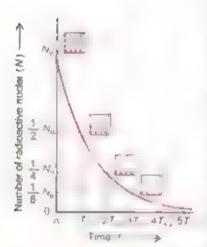
where  $\lambda$  is the constant of proportionality and is called decay constant. Eq. 21.8 shows that if the decay constant of any element is large then in a particular interval more of its atoms will decay and if the constant  $\lambda$  is small then in that very interval less number of atoms will decay. From Eq. 21.8 we can define decay constant  $\lambda$  as given below

here  $\Delta N / N$  is the fraction of the decaying atoms. Thus decay constant of any element is equal to the fraction of the decaying atoms per unit time. The unit of the decay constant is s. The negative sign in the Eq. 21.8 indicates the decrease in the number of atoms N.

The decay ability of any rad oactive element can be shown by a graphic method also

We know that every radioactive element decay at a particular rate with time. If we draw a graph between number of atoms in the sample of the radioactive element present at different times and the time then a curve as shown in Fig. 21.6 will be obtained. This graph shows that in the beginning the number of atoms present in the sample of the radioactive element was N<sub>a</sub>, with the passage of time the number of these atoms decreased due to their decay. This graph is called decay curve.

After a period of one half-irfe N. / 2 number of atoms of this radioactive element are left behind. If we wait further for another half-period then half of the remaining N<sub>o</sub> / 2 atoms decay, and  $1/2 \times N_o/2 = (1/2)^3 N_o$  atoms remain behind. After



the in a The half life 7 of a famous vertex as the true in which under the famous of the discrete discrete discrete discrete and the control of the control

the expiry of further period of a half-life. The following  $(1/2)^2 N_o$  atoms decay. The number of around that remain undecayed is  $1/2 \times (1/2)^2 N_o \approx (1/2)^2 N_o$ . We can conclude from this example that if we have N number of any radioactive element then after a period of n half-lives the number of atoms left behind is  $(1/2)^2 N_o$ .

it has been found that the estimate of decay of every radioactive element is according to the graph of Fig.21.6 but the half-life of every radioactive element is different. For example the half-life of uranium 236 is 4.5 x 10, years while the half-life of radium 226 is 1620 years. The half-life of some radio active elements is very small, for example, the half-life of radon gas is 3.8 days and that of uranium-239 is 23.5 minutes.

From the above discussion it is found that the estimate of any radioactive element can be made from its half-life or by determining its decay constant r. It can be proved with the help of calculus that the following relations exist between the decay constant  $\lambda$  and the half-life  $T_{\rm rad}$ 

Eq. 21.9 shows that if the decay constant / of any radioactive element is known, its half-life can be found.

Any stable element, besides the naturally occurring radioactive element can be made radioactive. For this very high energy particles are bombarded on the stable element. This bombardment excites the nucle and the nuclei after becoming unstable become radioactive element. Such radioactive elements are called artificial radioactive elements.

Example 21.2: Iodine 131 is an artificial radioactive isotope. It is used for the treatment of human thyroid gland its half-life is 8 days in the drug store of a hospital 20 mg of iodine 131 is present it was reneived from the laboratory 48 days ago. Find the quantity of iodine-131 in the hospital after this period.

#### Solution:

As the half life of lodine is 8 days, therefore in 8 days half of the lodine decays. Given below in the table is the amount of odine present after every 8 days.

Interval in days	Quantity of lodine	Interval in days	Quantity of lodine
0		32	1 25 mg
8	10 mg	40	0 625 mg 1
16	5 mg	48	0 3125 mg
24	2.5 mg		]

Thus 48 days after the receipt, the amount of iodine 131 left behind is only 0 3125 mg.

# 21.6 INTERACTION OF RADIATION WITH MATTER

An a-particle travels a well defined distance in a medium before coming to rest. This distance is called the range of the particle. As the particle passes through a solid it guid or gas. It loses energy due to excitation and ionization of atoms and molecules in the matter. The ionization may be due to direct elastic collisions or through electricistatic affraction functions the main interaction with matter to detect the particle or to measure its energy. The range depends on the

- i. charge, mass and energy of the particle and
- fi. the density of the medium and ionization potentials of the atoms of the medium

Since apparticle is about 7000 times more massive than an electron so it does not suffer any appreciable deflection from its straight path provided it does not approach too close y to the nucleus of the atom. Thus apparticle continues producing intense ionization along its straight path in it loses a lits energy and comes almost to restrict their captures two electrons from the medium and becomes a neutral helium atom.

β-particles also lose energy by producing ion zation. However its ionizing ability is about 100 times less than that of α-particles. As a result its range is about 100 times more than α-particles ip-particles are more easily deflected by cooks ons than heavy α-particles. Thus the path of i-particles in matter is not straight but shows much straighing or scattering. The range of 3-particles is measured by the effective depth of penetration into the medium not by the length of ematic path. The more dense the material through which the particle moves, the shorter its range will be

α and β-particles both radiate energy as X-ray photons when they are slowed by the electric field of the charged particles in a solid materia.

Photons of y-rays, being uncharged, cause very little ionization. Photons are removed from a beam by either scattering or absorption in the medium. They interact with matter in three distinct ways, depending mainly on their energy.

- At low energies (less than about 0.5 MeV), the dominant process that removes photons from a beam is the photoelectric effect.
- (ii) At intermediate energies, the dominant process is Compton scattering
- (iii) At higher energies (more than 1.02 MeV), the dominant process is pair production

In air y-rays intensity fails off as the inverse square of the distance from the source, in much the same manner as light from a lamp in solids the intensity decreases exponent ally with increasing depth of penetration into the material. The intensity of a beam after passing through a distance x in the medium is reduced to intensity / given by the relation /=1,e<sup>-rt</sup>

where  $\mu$  is the linear absorption coefficient of the medium. This coefficient depends on the energy of the photon as well as on the properties of the medium.

Charged particles (a or line) and in-radiation produce fluorescence or grow on striking some substance like zinc sulphide sod um lodide or barium plat nocyanide coated screens.

"Fluorescence is the property of absorbing radiant energy of high frequency and reemitting energy of low frequency in the visible region of electromagnetic spectrum".

Neutrons being neutral particles are extremely penetrating particles. To be stupped or slowed a neutron must undergo a direct collision with a nucleus or some other particle that has a mass comparable to that of the neutron. Materials such as water or plastic, which contain more low-mass nuclei per unit volume, are used to stop neutrons. Neutrons produce a little indirect sonization when they interact with materials containing hydrogen atoms and knock out protons.

Table 21 1	The summar	of the nature of a	in & radiation
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Characteristics	a particles	particles	γ–rays
1 Nature	Helium nuclei of charge 2e	Electrons or positrons from the nucleus of charge ±e	E M waves from excited nuclei with no charge
2 Typica sources	Radon-222	Strontium-94	Cobalt-60
3 on zation (lon pairs mm in air)	About 10*	About 10	About 1
4 Range n air	Several centimetres	Several metres	Obeys inverse square law
5 Absorbed by	A paper	1.5 mm of Alisheet	1 10 cm of ead sheet
6 Energy spectrum	Emitted with the same energy	Vanable energy	Variable energy
7 Speed	~ 10 <sup>7</sup> ms <sup>1</sup>	~1 x 10 <sup>8</sup> ms <sup>-1</sup>	-3 x 10 <sup>8</sup> ms 1

#### 21.7 RADIATION DETECTORS

Nuclear rad at one cannot be detected by our senses hence, we use some observable detecting methods employing the interaction of radiation with matter. Most detectors of radiation make use of the fact that ionization is produced along the path of the particle. These detectors include Wilson cloud chamber. Genger counter and solid state detectors.



It is a device which shows the visible path of an ionizing particle. It makes use of the fact that supersaturated vapours. condense preferentially on ions. If an ion zing particle passes. through a region in which cloud droplets are about to form, the droplets wir form first along the particle's path, showing the path as a trail of droplets. The apparatus consists of a cylindrical glass chamber closed at the upper end by a glass. window and at the lower end by a movable piston (Fig. 21.7). A black felt pad soaked in alcohol is piaced on a metal piate inside the chamber. The air soon becomes saturated with alcohol vapours. A rapid expansion is produced by pulling quickly the piston of the bicycle pump having the leather washer reversed so that it removes air. The sudden cooling resulted from adiabatic expansion helps to form supersaturated vapours. As radiation passes through the chamber ions are produced along the path. The tiny dropiets

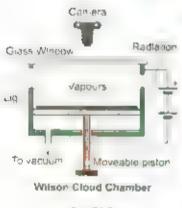


Fig. 21.7

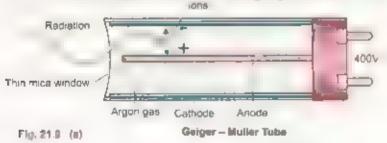
of moisture condense about these ions and form vapour tracks showing the path of the radiation. These are the atomic versions of the ice crystals left in the sky by a jet plane when suitable conditions exist. The fog tracks are interminated with a lamp and may be seen or photographed through the glass window.

The α particles leave thick, straight and continuous tracks due to intense ionization produced by them as shown in Fig. 21.8 (a), β-particles form thin and discontinuous tracks extending in erratic manner showing frequent deflections (Fig. 21.8 b) and γ-rays leave no definite tracks along their path (Fig. 21.8 c). The length of the cloud tracks has been found proportional to the energy of the incident particle. A high potential difference of the order of 1 kV between the top and bottom of the chamber provides an electric field which clears away at the unwanted ions from the chamber to make it ready for use. The tracks seen are therefore, those of rays that pass the chamber as the expansion occurs.

The chamber may be placed in a strong magnetic field which will bend the paths providing information about the charge, mass and energy of the radiating particle. In this way, it has helped in the discovery of many new particles.



Ge ger-Muller tube is a well-known radiation detector (Fig. 21.9 a). The discharge in the tube results from the ionization produced by the incident radiation. It consists of a stiff central wire acting as an anode in a hollow metal cylinder acting as a cathode filled with a suitable mixture of gas at about 0.1 atmospheric pressure. One end of the tube has a thin mica window to allow the entry of α or β-particles and other end is sealed by non-conducting material and carries the connecting pins for the two electrodes. A high potential difference (about 400 V for neon-bromine filled tubes) but slightly less than that



235



(a) a- Particle



(b) B-Particle



Fig. 11 in Cloud chamber tracks of radiations



(b) G.M. Tube with scalar unit Fig. 21.9

necessary to produce discharge through the gas is maintained between the electrodes. When radiation enters the tube, ionization is produced. The free electrons are attracted towards the positively charged central wire. As they are accelerated towards the wire by a strong electric field, they collide with other molecules of the gas and knock out more electrons which in turn do the same and produce a cascade of electrons that move towards the central wire. This makes a short pulse of electric current to pass through an external resistor, it is amplified and registered electronically. The counter, which also provides the power, is called a scaler.

The cascade of electrons produced by the entry of an ionizing particle is counted as a single pulse of approximately of the same size whatever the energy or path of the particle maybe. It cannot, thus, discriminate between the energies of the incident particle as output pulses are same. The entire electron pulse takes less than 1µ s. However, positive ions, being very massive than the electrons, take several hundred times as long to reach the outer cathode. During this time, called the dead time (10°s) of the counter further incoming particles cannot be counted. When positive ions strike the cathode, secondary electrons are emitted from the surface. These electrons would be accelerated to give further spurious counts. This is prevented by mixing a small amount of quenching gas with the principal gas.

The guenching gas must have an ionization potential lower than that of mert or principal gas. Thus, the ions of guerching. gas reach the cathode before principal gas ions. When they reach near the cathode, they capture electrons and become neutral molecules. Following neutralization, the excess energy of the quenching molecules is dissipated in dissociation of the molecules rather than in the release of electrons from the cathode. For example, bromine gas is added to neon gas. The bromine molecules absorb energy from the ions or secondary electrons and dissociate into bromine atoms. The atoms then readily recombine into molecules again for the next pulse. The gas quenching is called self quenching. Although all commercial Geiger tubes are self quenched, it is common practice to use electronic quenching in addition. For this purpose, a large negative voltage is applied to the anode immediately after recording

the output pulse. This reduces the electric field bledwithe critical value for ion lation by the sion, the height velocitage remains until all the positive ions are collected at cathode thus preventing secondary pulses.

Geiger counter can be used to determine the range or punction, power of onlying particles. The reduction in the count rate by inserting metal plates of varying thickness between the source and the tube helps to estimate the penetration power of the incident radiation.

Gerger ourser's not suitable for fast counting it is because of its relatively long "dead time" of the order of more than a millisecond which timits the counting rate to a few hundred counts per second particles are not dent on the tube at a faster rate, not all of them will be counted since some will arrive it nog the dead time. Solid slate detectors are fast end, indicate and accounted.

# Schiel Chate Between I

A solid state detector is a specially designed p-n Junction (Fig. 21.10) operating under a reversed bias in which e actron-hole pairs are produced by the incident radiation to ca seacurrent prostotick with a track macreal The detector is made from a p-type silicon or germanium. An ntype thin layer is produced by doping the top surface with donor type impurity. The top and bottom surfaces are coated with aith neayer of gold to make good conducting contact with external circuit. The combined thickness of n-type and gold layer absorbs so less energy of the incident particle that the junction may be assumed to be situated at the front surface. This is known as the surface barrier type detector. A reverse bias is applied through the two conducting avers of god. This entiriges the charge free region around the junction called deciletion region. Normally no current flows through the circus. When an incident particle penetrates through the depletion region, it produces electron hole pairs. These mobile charge carriers move towards the respective sides due to upplied electric field. This gives rise to a current in the external circuit due to which a pulse of voltage is generated across the resistance R. This pulse is amplified and registered by a scaler unit. The size of the pulse is found proport anal to the energy absorbed of the noident particle. The energy needed to produce an electronhole pair is about 3 eV to 4 eV which makes the device useful for detecting low energy particles. The collection time of electrons and holes is much less than gas filled counters and hence a solid state detector can count very fast. It is much smaller in size than any other detector and operates at low voltage. The above mentioned type detector is used for detecting a or it particles but a specially designed device

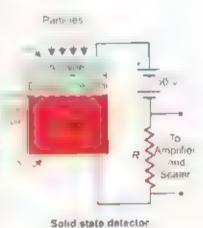


Fig. 21 10

# 21.8 NUCLEAR REACTIONS

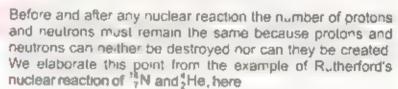
While studying radioactivity, we have seen that an  $\alpha$  particle is emitted from radium-226 and radon-222 is obtained. This nuclear change is represented by the following equation

Such an equation represents a nuclear reaction. Above mentioned nuclear reaction takes place on its own accord. However, it was Rutherford who, first of ail expressed his opinion that besides natural radioactive decay processes other nuclear reactions can also occur. A particle x is bombarded on any nucleus X and this process yield a nucleus Y and a light object y as given below.

$$X+x \rightarrow Y+y$$

Rutherford performed an experiment on the nuclear reaction in 1918. He bombarded α-particles on nitrogen. He observed that as a result of this reaction, oxygen is obtained and a proton is emitted. That is

This reaction indicated that when  $\alpha$ -particle enters the nucleus of  ${}^{\dagger}N$ , then an excitation is produced in it. And as a result of it.  ${}^{\dagger}O$  and a proton are produced. Since the experiment of Rutherford innumerable nuclear reactions have been observed. For nuclear reactions to take place, the fulfillment of certain conditions is a most.

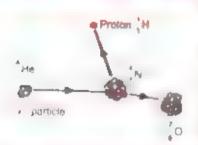


$$^{14}_{7}\text{N} + {^4_{2}\text{He}} \longrightarrow {^{17}_{8}\text{O}} + {^1_{1}\text{H}}$$

Number of protons = 7 + 2 = 8 + 1Number of neutrons = 7 + 2 = 9 + 0

Anuclear reaction can take place only when the total energy of the reactants including the rest mass energy is equal to the total energy of the products. For its explanations we again take the example of the nuclear reaction of Rutherford involving  ${}^4N$  and  ${}^4He$ . In this reaction the mass of the reactants is





An upha proton nuclear reaction

Mass of <sup>1</sup>/<sub>2</sub>N = 14.0031 u Mass of <sup>4</sup>/<sub>2</sub>He = 4.0026 u

Total mass of the reactants ≈ 18 0057 u In the same way the mass of the products is

> Mass of  ${}_{B}^{17}O = 16.9991 \text{ u}$ Mass of  ${}_{C}^{1}H = 1.0078 \text{ u}$

Total mass of the products after the reaction = 18,0069 u

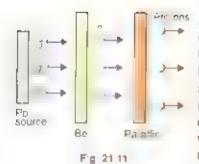
This shows that the total mass after the reaction is greater than the total mass before the reaction by 0 0012 u. We know that a 1u mass = 931 MeV energy, therefore, a mass difference of 0.0012u is equivalent to an energy of 931 MeV x 0 0012 u = 1.13 MeV. Hence this reaction is possible only when an additional mass of 0 0012 u is added into the reactants or the minimum kinetic energy of the aparticle s 1.13 MeV such as obtained from  $^2$  Po. The energy of these  $\alpha$ -particles is equal to 7.7 MeV which is greater than 1.13 MeV. Had these  $\alpha$ -particles been obtained from a source that give out  $\alpha$ -particles whose energy was less than 1.13 MeV then this reaction would not have taken place.

From the conditions described above we can tell whether any nuclear reaction is possible or not. There is an interesting aspect in a nuclear reaction that it can take place in the opposite direction also. We know that  ${}_{8}O$  is obtained by the interaction  ${}_{8}^{4}N$  with an  $\alpha$ -particle of appropriate energy. If we accelerate protons, with the help of a machine like cyclotron, and increase their velocity and then bombard these high velocity protons on  ${}_{8}^{4}O$ . Rutherford's nuclear reaction of  ${}_{8}^{4}N$  and  $\alpha$ -particle, will proceed in the backward direction as

$${}^{17}_{8}O + {}^{1}_{1}H \longrightarrow {}^{14}_{7}N + {}^{4}_{2}He$$

By bombarding different elements with  $\alpha$ -particles, protons and neutrons many nuclear reactions have been produced. Now we describe one such nuclear reaction with the help of which James Chadwick discovered neutron in 1932. When  ${}^8_a$ Be was bombarded with  $\alpha$ -particles emitted out of  ${}^{210}_{84}$ Po then as a result of a nuclear reaction  ${}^{12}_6$ C and a neutron were obtained. This reaction is shown below with an equation.

As neutron carries no charge, therefore, it presented a great amount of difficulty for its identification. Anyhow



when neutrons were passed through a block of paraffin, fast moving protons were ejected out and these were easily identified. It may be remembered that a large amount of hydrogen is present in paraffin and the nuclei of hydrogen. atoms are protons. The emission of protons is the consequence of elastic colusions between the neutrons and the protons. This indicates that the mass of neutron is equal. to the mass of the proton. It may be remembered that when an object of certain mass will derive it another object of equamass at rest, then as a result of elastic coll sion, the moving object comes to rest and the stationary object begins to move with the velocity of the colliding object. The discovery of neutron has brought in a revolution in nuclear reactions, as the neutrons carry no charge so they can easily enter the nucleus. Fig. 21.11 shows the arrangement of Chadwick's experiment for the discovery of neutron.

# 21.9 NUCLEAR FISSION

Ofto Hahn and Fritz Strassmann of Germany white working upon the nuclear reactions made a startling discovery. They observed that when slow moving neutrons are bombarded on \$\frac{1}{2}\$U then as a result of the nuclear reaction \$\frac{1}{2}\$. Kr and an average of three neutrons are obtained. It may be remembered that the mass of bold hkry; on and bar um is essitian that of the mass of uranium. This nuclear reaction was different from hither to studied other nuclear reactions, in two ways. First as a result of the breakage of the uranium nucleus, two nuclei of almost equal size are obtained, whereas in the other nuclear reactions the difference between the masses of the reactions and the products was not large. Secondly a very large amount of energy is given out in this reaction.

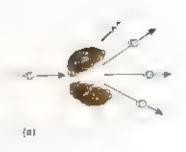
"Such a reaction in which a heavy nucleus like that of uranium splits up into two nuclei of roughly equal size along with the emission of energy during the reaction is called fission reaction"

Fission reaction of \_\_u can be represented by the equation

$$^{235}_{92}U + ^{1}_{0}n \longrightarrow ^{141}_{50}Ba + ^{92}_{36}Kr + 3^{1}_{0}n + Q$$

here Q is the energy given out in this reaction. By comparing the total energy on the left side of the equation with total energy on the right side we find that in the fission of one uranium nucleus about 200 MeV

energy signer out. It may be kept in mind that there is no difference between the sum of the mass and the charge numbers on both sides of the equation. Fission reaction is shown in Fig. 21.12 (a) and (b). Fission reaction can be easily explained with the help of graph of Fig. 21.4. This graph shows that the binding energy per nucleon is greatest for the middle elements of the periodic table and this binding energy per nucleon is a little less for the light or very heavy elements i.e., the nucleons in the light or very heavy elements are not so rigidly bound. For example the light of genergy per nucleon for uranium is



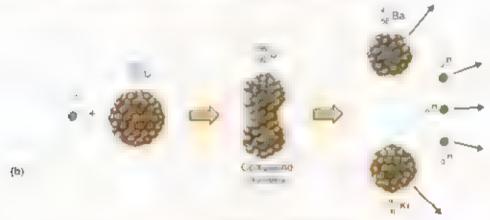


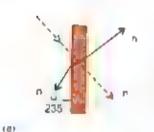
Fig. 21-12 Process of Flasion reaction

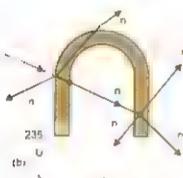
about 7.7 MeV and the products of the fission reaction of uranium namely banum and krypton, have binding energy of about 8.5 MeV per nucleon. Thus when a uranium nucleus breaks up as a result of fission reaction, into banum and krypton, then an energy at the rate of (8.5-7.6) = 0.9 MeV per nucleon is given out. This means that an energy 235 x 0.9 = 211.5 MeV is given out in the fission of one uranium nucleus.

The fission process of transom does not always produce the same fragments (Balikr). In fact any of the two nuclei present in the upper horizontal part of binding energy could be produced. Two possible fission reactions of uranium are given below as an example.

$$^{235}_{92}U + ^{1}_{0}n \longrightarrow ^{132}_{50}Sn + ^{101}_{42}Mo + 3 ^{1}_{0}n + Q$$







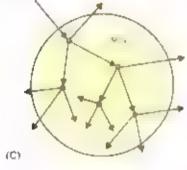


Fig 21 14

# 235 U + 1n ---- 140 Xe + 34 St + 2 1n + Q

Hence in the uranium fission reaction several products may be produced. All of these products (fragments) are radioactive Fission reaction is not confined to uranium alone, it is possible in many other heavy elements. However it has been observed that fission takes place very easily with the slow neutrons in uranium-235 and plutonium-239, and mostly these two are used for fission purposes.

# This is the Reaction

We have observed that during fiss on reaction, a nucleus of uranium-235 absorbs a neutron and breaks into two nucle of almost equal masses besides emitting two or three neutrons. By properly using these neutrons fission reaction can be produced in more uranium atoms such that a fission reaction can continuously maintain itself. This process is called fission chain reaction. Suppose that we have a definite amount of 235 u and a slow neutron or ginating from any source produces fission reaction in one atom of uranium. Out of this reaction about three neutrons produce fission in some more atoms of uranium. In this way this process rapidly proceeds and in an infinites mai small time a large amount of energy along with huge explosion is produced Fig.21.13 is the representation of fission chain reaction.

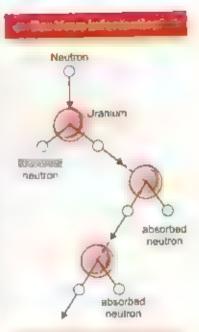
It is possible to produce such conditions in which only one neutron, out of all the neutrons created in one fission reaction, becomes the cause of further Ession reaction. The other neutrons either escape out or are absorbed in any other medium except uranium. In this case the fission chain reaction proceeds with its initial speed. To understand these conditions carefully look at Fig 21.14. In Fig 21.14 (a) a fission reaction in a thin sheet of 21°U is shown to be in progress. The resulting neutrons scatter in the air and so they cannot produce any fission chain reaction. Fig. 21.14 (b) shows some favourable conditions for chain reaction. Some of the neutrons produced in the first fission reaction produce only one more fission reaction but here also no chain reaction is produced in Fig. 21.14 (c) a sphere of U is shown. If the sphere is sufficiently big, then most of the neutrons produced by the fission reaction get absorbed in ... U before they escape out of the sphere and produce chain reaction. Such a

mass of uranium in which one neutron out of all the neutrons produced in one fission reaction produces further fission is called critical mass. The volume of this mass of uranium is called critical volume

If the mass of uranium is much greater than the critical mass, then the chain reaction proceeds at a rapid speed and a huge explosion is produced. Atom bomb works at this principle. If the mass of uranium is less than the critical mass, the chain reaction does not proceed. If the mass of uranium is equal to the critical mass, the chain reaction proceeds at its initial speed and in this way we get a source of energy. Energy, in an atomic reactor, is obtained according to this principle. The chain reaction is not allowed to run wild, as in an atomic bomb but is controlled by a series of rods, usually made of cadmium, that are inserted into the reactor. Cadmium is an element that is capable of absorbing a large number of neutrons without becoming unstable or radioactive. Hence, when the cadmium control rods are inserted into the reactor, they absorb neutrons to cut down on the number of neutrons that are available for the fission process. In this way the fission reaction is controlled



In a nuclear power station the reactor plays the same part as does furnace in a thermal power station. In a furnace, coal or oil is burnt to produce heat, while in a reactor fission reaction produces heat. When fission takes place in the atom of uranium or any other heavy atom, then an energy at the rate of 200 MeV per nucleus is produced. This energy appears in the form of kinetic energy of the fission fragments. These fast moving fragments besides colliding with one another also collide with the uranium atoms. In this way, their is netic energy gets transformed in heat energy. This heat is used to produce steam which in turn rotates the turbine. Turbine rotates the generator which produces electricity. A sketch of a nuclear power station is shown in Fig. 21.15.



In a controlled chain reaction only one relation on average from each fast on event causes another notes a result on a result of a result of a controlled rate.

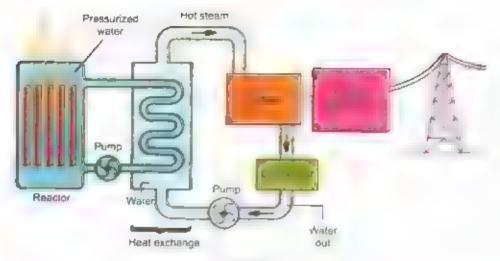


Fig. 21 15

#### Areactor usually has four important parts. These are:

The most important and vital part of a reactor is called core. Here the fuel is kept in the shape of cylindrical tubes. Reactor fuels are of various types. Uranium was used as fuel in the elementary reactors. In this fuel the quantity of <sup>218</sup><sub>92</sub>U its increased from 2 to 4 percent. It may be remembered that the quantity of <sup>230</sup><sub>92</sub>U in the naturally occurring uranium is only 0.7 percent. Now-a-days plutonium-239 and uranium-233 are also being used as fuel

The fuel rods are placed in a substance of small atomic weight, such as water, heavy water, carbon or hydrocarbon etc. These substances are called moderators. The function of these moderators is to slow down the speed of the neutrons produced during the fission process and to direct them towards the fuel. Heavy water, it may be remembered, is made of <sup>2</sup><sub>3</sub>H , a heavy isotope of hydrogen instead of <sup>3</sup><sub>3</sub>H. The neutrons produced in the fission reaction are very fast and energetic and are not suitable for producing fission in reactor fuel like <sup>235</sup>U or <sup>236</sup>Pu etc. For this purpose slow neutrons are more useful. To achieve this moderators are used.

Besides moderator there is an arrangement for the control of number of neutrons, so that of all the

neutrons produced in fission, only one neutron produces further fission reaction. The purpose is achieved either by cadmium or by boron because they have the property of absorbing fast neutrons. The control rods made of cadmium or boron are moved in or out of the reactor core to control the neutrons that can initiate further fission reaction. In this way the speed of the chain reaction is kept under control. In case of emergency or for repair purposes control rods are allowed to fall back into the reactor and thus stop the chain reaction and shut down the reactor.

Heat is produced due to chain reaction taking place in the core of the reactor. The temperature of the core, therefore, rises to about 500 °C. To produce steam from this heat, it is transported to heat exchanger with the help of water, heavy water or any other liquid under high pressure. In the heat exchanger this heat is used to produce high temperature steam from ordinary water. The steam is then used to run the turbine which in turn rotates the generator to produce electricity. The temperature of the steam coming out of the turbine is about 300 °C. This is further cooled to convert it into water again. To cool this steam, water from some river or sea is, generally, used. In Karachi nuclear power plant (KANUP), heavy water is being used as a moderator and for the transportation of heat also from the reactor core to heat exchanger. heavy water is used. To cool steam coming out of the turbine, sea water is being used.

The nuclear fuel once used for charging the reactor can keep on operation continuously for a few months. There after the fissile material begins to decrease. Now the used fuel is removed and fresh fuel is fed instead in the used up fuel intensely radioactive substances remain. The half-life of these radioactive remnant materials is many thousand years. The radiations and the particles emitted out of this nuclear waste is very injurious and harmful to the living things unfortunately there is no proper arrangement of the disposal of the nuclear waste. This cannot be dumped into oceans or laft. In any place, where they will contaminate the environment, such as through the soil or the air. They must not be allowed to get into the drinking water. The best place so far found to store these wastes is in the bottom of old sait.

mines, which are very dry and are thousands of metres below the surface of the Earth. Here they can remain and decay without polluting the environment.

# voes of Reactor

There are two main types of nuclear reactors. These are

(i) Thermal reactors

(ii) Fast reactors

The thermal reactors are called "thermal" because the neutrons must be slowed down to "thermal energies" to produce further fission. They use natura uranium or slightly enriched uranium as fuel. Enriched uranium contains a greater percentage of U-235 than natural uranium does. There are several designs of thermal reactors. Pressurized water reactors (PWR) are the most widely used reactors in the world. In this type of reactors, the water is prevented from boiling, being kept under high pressure. This hot water is used to boil another circuit of water which produces steam for turbine rotation of electricity generators.

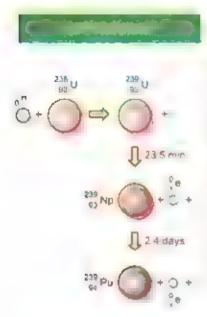
Fast reactors are designed to make use of U-238, which is about 99% content of natural uranium. Each U-238 nucleus absorbs a fast neutron and changes to plutonium-239

Plutonium can be fissioned by fast neutrons hence moderator is not needed in fast reactors. The core of fast reactors consists of a mixture of plutonium and uranium dioxide surrounded by a blanket of uranium-238.

Neutrons that escape from the core interact with uran um-238 in the blanket, producing thereby plufonium-239. Thus more protonium fue is bred in this way and natural uranium is used more effectively.

#### 21.10 FUSION REACTION

We know that the energy given out per nucleon per fission of heavy element like that of uranium is 0.9 MeV it is due to the fact that the binding energy per nucleon of the fission fragments is greater than uranium in fact energy is obtained from any nuclear reaction in which the binding energy per nucleon of the products increases is there any other reaction besides the fission reaction from which energy could be obtained? In order to answer this question we must ponder



An induced nuclear reaction of which  $\frac{23h}{6}$ , us transmuted into the rans rankum element protonium of  $\frac{239}{64}$ .

over Fig 21.4 again. This graph shows that the binding energy per nucleon increases upto A = 50. Hence when two light nucle merge together to form a heavy nucleus whose mass number A is less than 50, then energy is given out. In section on "Mass Defect and Binding Energy" we have observed that when two protons and two neutrons merge to form a healumnucleus, then about 28 MeV energy is given out.

"Such a nuclear reaction in which two light nuclei merge to form a heavy nucleus is called fusion reaction".

During a fusion reaction some mass is lost and its equivalent energy is given out. In a fusion reaction, more energy per nucleon can be obtained as compared to the fission reaction. But unfortunately it is comparatively more difficult to produce fusion. Two positively charged light nuclei must be brought very close to one another. To do so work has to be done against the electrostatic force of repulsion between the positively charged nuclei. Thus a very large amount of energy is required to produce fusion reaction. It is true that a greater amount of energy can be obtained during a fusion reaction compared to that produced during a fission reaction, but in order to start this reaction a very large amount of energy is spent. On the contrary no difficulty is faced to start the fission reaction because neutron has no charge on it and thesito face no repulsive force while reaching the nucleus.

Let us now take the example of a fusion reaction when two deuterons are merged to form a helium nucleus. 24 MeV energy is released during this process i.e.,

But there is a very little chance of the formation of <sup>4</sup><sub>2</sub>He nucleus by the merger of two deuterons. The probability of occurring such a reaction is great where one proton or one neutron is produced as given below:

$${}^{2}_{H} + {}^{2}_{H} \longrightarrow {}^{3}_{H} + {}^{3}_{H} + 4.0 \text{ MeV}$$
or
$${}^{2}_{H} + {}^{3}_{H} \longrightarrow {}^{3}_{H} + {}^{4}_{n} + 3.3 \text{ MeV}$$

in both of these reactions about 1.0 MeV energy per nucleon is produced which is equal to the energy produced during fission if "Hand "H are forced to fuse then 17.6 MeV energy is obtained) e.

We know that for fusion of two light nuclei the work has to be

# ( De You Know)

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done to overcome the repulsive force which exists between them. For this the two nuclei are hurled towards one another at a very high speed. One method to do so is to give these nuclei a very large velocity with the help of an accelerator. This method has been used in the research study of nuclear fusion of <sup>2</sup>H and <sup>3</sup>H. But this method of nuclear fusion for getting energy cannot be used on a large scale.

There is another method to produce fusion reaction all is based upon the principle that the speed of atoms of a substance increases with the increase in the temperature of that substance. To start a fusion reaction the temperature at which the required speed of the Light, nucleican be obtained is about 10 million degrees celsius. At such extraordinarly high temperature the reaction that takes place is called thermonic ear reaction. Ordinarly such a high temperature cannot be achieved. However during the explosion of am atom bomb this temperature can be had for a very short time.

Until now the fusion reaction is taking place only in a hydrogen bomb. That extraordinary high temperature is obtained during the expression of an atom no no due to this high temperature the fusion reaction between H and 'H sots in In this way a very large amount of ellergy is given out with the explosion.

A very large amount of energy can be had from a fusion reaction, but till now this reaction has not been brought under control like a fission reaction and so is not being used to produce electricity. Efforts are infulls with a find and it is hoped that in near future some method would be found to control this reaction as well.

# Nation Thought of the the Dall (

amount of helium and a slight amount of other heavy elements. A tremendous amount of energy keeps saving out of it continuously at all times. The temperature of its core is about 20 million degrees celsius and its surface temperature is about 6000 degrees celsius. Its energy is due to fus on reaction, called p-p reaction. During this process two hydrogen nuclei or two protons fuse to from devieron. This reaction takes place as

With the fusion reaction of deuteron with proton (He an isotope of helium is formed i.e.,

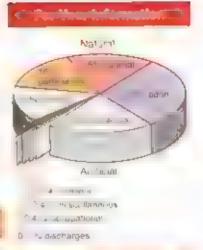
In the last stage the two nucles of 3He react in the following manner

In this reaction six protons take part and finally a helium nucleus and two protons are formed. That is, the result of different stages of this reaction is that four protons have formed one helium nucleus. It has been estimated that in this p-pichain reaction, 25.7 MeV energy is given out i.e., 6.4 MeV per nucleon energy is obtained which is much greater than the energy given out per nucleon (1 MeV) during a fission reaction.

# 21.11 RADIATION EXPOSURE

When a Garger tube is used in any experiment, it records radiation even when a radioactive source is nowhere near it. This is caused by radiation called background radiation it is partividue to cosmic radiation which comes to us from outer space and partly from naturally occurring radioactive substance in the Earth's crust. The cosmic radiation consists of high energy charged particles and electromagnetic radiation. The almosphere acts as a shield to absorb some of these radiations as well as ultraviolet rays. In recent past, the depletion of ozone layer in the upper atmosphere has been detected which particularly filters ultraviolet rays reaching us This may result in increased eye and skin diseases. The depletion of oxone layer is suspected to be caused due to excessive release of some chemicals in the atmosphere such as chioroflourocarbons, CFC) used in refrigeration, aerosospray and plastic foam industry its use is now being replaced by environmentally friendly chemicals. Many building materials contain small amounts of radioactive isotopes Rad pactive raden gas enters buildings from the ground. It gets trapped inside the building which makes radiation levels much higher from radon inside than outside, A good ventilation can reduce radon level inside the building. All types of food also contain a little radioactive substance. The most common are potassium-40 and carbon-14 isotopes.

Some radiation in the environment is added by human activities. Medical practices, mostly diagnostic X-ray probably contribute the major port on to it. It is an unfortunate fact that many X-ray exposures such as routine chest X-ray



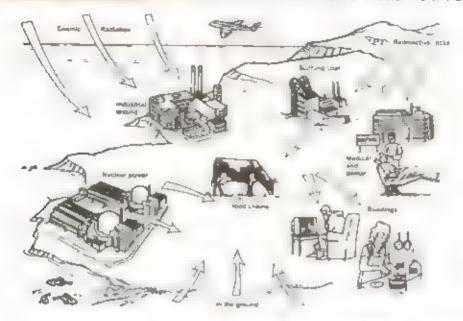
Pio chart showing proportion of rails in oir respectively average passon.



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Sources of natural radiation

and denta X ray are made for no strong reason and may do more harm than good. Every X-rays exposure should have a definite justification that outweighs the risk. The other sources include radioactive waste from nuclear facilities,



hospitals research and industrial establishments colour television luminous watches and tobacco leaves. A smoker not only inhales toxic smoke but also hazardous radiation. Low level background radiation from natural sources is normally considered to be harmless. However, higher levels of exposure are certainly damaging. We cannot avoid exposure to radiation. However, the best advice is to avoid unnecessary exposure to any kind of ionizing radiation.

# 21.12 BIOLOGICAL EFFECTS OF RADIATION

Table 27.2
Relative Biological Effectiveness (RBE)
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To study the effects of radiation, we need to define some of the units of radiation. The strength of the radiation source is indicated by its activity measured in becquere. (Bq). One becquerer is one disintegration per second. A arger unit is curre (Ci) which equals 3.7 x 10 disintegrations per second. The effect of radiation on a body absorbing it relates to a quantity called absorbed dose *D* defined as the energy *E* absorbed from onizing radiation per unit mass *m* of the absorbing body.

 $D = \frac{E}{m} \qquad (21.10)$ 

its SI unit is gray (Gy) defined as one joule per kilogram.

1 Gy = 1 Jkg 1

An old unit is rad, an acronym for radiation absorbed dose.

$$1 \text{ rad} = 0.01 \text{ Gy}$$

Equal doses of different radiations do not produce same biological effect. For the same absorbed dose, α-particles are 20 times more damaging than X-rays. The effect arso depends on the part of the body absorbing the radiation. For example, neutrons are particularly more damaging to eyes than other parts of the body. To allow this the absorbed dose is multiplied by a quality factor known as relative biological effect veness or RBE (Table 21.2). The equivalent dose *D*, of any absorbed radiation is defined as the product of absorbed dose and RBE of the kind of radiation being absorbed.

$$D_{\bullet} = D \times RBE$$
 ........... (21.11)

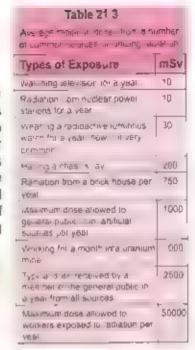
The SI unit of equivalent dose is sievert (Sv).

An old unit, the rem is equal to 0.01 Sv.

The background radiation to which we are exposed, on the average is 2 mSv per year. Doses of 3 Sv will cause radiation burns to the skin. For workers in the nuclear facilities or mines, a weekly dose of 1 mSv is normally considered safe (Table 21.3).

The damage from α-particles is small unless the source enters the body α and β-particles can cause redness and sores on the skin. Some other low level radiation effects are oss of hair ulceration, stiffening of the lungs, and a drop in the white blood ceas which is followed by a sickness pattern of diarrheal vomiting and fever known as radiation sickness (Fig. 21.16). High levels of radiation may disrupt the blood cells seriously leading to diseases such as anaemia and leukaemia. Chromosome abnormalities or mutation may cause delayed genetic effects such as cancer, eye cataracts and abnormalities in the future generations. These may develop many years after exposure to harmful radiation.

Example 21.3: How much energy is absorbed by a man of mass 80 kg who receives a lethal whole body equivalent dose of 400 rem in the form of low energy neutrons for which RBE factor is 10?



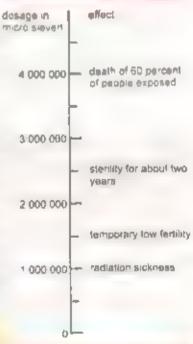


Fig. 21 15 The effects of exposure to high levels of ionizing radiation



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#### Solution

RBE factor - 10

 $D_s = 400 \text{ rem} = 400 \times 0.01 \text{ Sv} = 4 \text{ Sv}$  D = 100 s

Using Eq. 214

Since 1 Gy is 1 J kg $^{\prime}$ , hence total energy absorbed by the whole body = mD =  $80 \times 0.4$  Gy = 32 J

It is a very small amount of thermal energy. Obviously, the damage done by ronzing radia, on has nothing to do with thermal a lengy. The narmful effects arise due to disruption of the normal functions of the tissues in which it is absorbed

# 21 13 BIOLOGICAL AND MEDICAL USES OF RADIATION

Radio solopes of many elements can be made easily by bombardment with neutrons and other particles. As such solopes have become available and are inexpensive their use in medicine, agriculture, scientific research and industries has expanded tremendously.

Radio sotopes are used to find out what happens in many nomplex chemical reactions and how they proceed Similarly in brough, they have helped in investigating into chemical reactions that take place in plants and animals. By mixing a small amount of radioactive isotope with fertilizer, we can easily measure how much fertilizer is taken up by a plant using rad at un detector. From such measurements, farmers know the proper amount of fertilizer to use. Through the use of rad at on-induced mutations, improved varieties of certain crops such as rice, whickpea, wheat and cotton have been developed. They have improved plant structure. The plants have shown more resistance to diseases and pest, and give better yield and grain quality. Rad ation is also used to treat cancers. Radioactive tracers, and imaging devices have helped in the inderstanding and diagnosis of many diseases.



A rad oactive solope behaves in just the same way as the normal isolope inside a living organism. But the location and concentration of a radioactive isolope can be determined easily by measuring the radiation it emits. Thus, a radioactive

isotope acts as an indicator or tracer that makes it possible to follow the course of a chemical or biological process. The technique is to substitute radioactive atoms for stable atoms. of the same kind in a substance and then to follow the 'tagged' atoms with the help of radiation detector in the process. Tracers are widely used in medicine to detect malignant tumors and in agriculture to study the uptake of a fertilizer by a plant. For example, if a plant is given radioactive. carbon-14, it will use it in exactly the same way as it always. uses stable carbon-12. But the carbon-14 releases β-rad ations and thus by measuring radioactivity in different parts of the plant, the path taken by the carbon atoms can be known. This technique has betped to understand more e aborately the complex process of photosynthesis. The tracer technique was also used to identify faults in the underground pipes of the fountain system of the historical Shallmar gardens of Lahore by the scientists of Pakistan Atomic Energy Commission

## Madical Madical Annie

Tracers are widely used in medicine to study the process of digestion and the way chemical substances move about in the body.

Some chemicals such as hydrogen and sodium present in water and food are distributed uniformly throughout the body. Certain other chemicals are selectively absorbed by certain organs. Radio-odine for example, is absorbed mostly by the thyroid gland phosphorus by bones and cobait by over likely can serve as tracers. Small quantity of low activity radio-sotope mixed with stable sotope is administered by nijection or otherwise to a patient and its location in diseased bissue can be ascertained by means of radiation detectors. For example, radioactive localle can be used to check that a person's thyroid gland is working property. A diseased or hyperactive gland absorbs more than twice the amount of normal thyroid gland. A similar method can be used to study the circulation of blood using radioactive isotope sod umit/4.

Experiments on cancerous cells have shown that those cells that multiply rapidly absorb more radiation and are more easily destroyed then normal cells by ionizing radiation. Radiotherapy with rays from cobalt 50 is often used in the treatment of cancer. The γ-rays are carefully focussed on to the malignant tissue. Strict safety precautions are necessary.

Table 21 4

lsotope	Haff-fife		Example
		Mev 9 Do	use
	F + F <sub>1</sub>	47 Th	Frank Ro
un <sup>a</sup> Fre	% J days	25 6	Iron r Pasing
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for both patient and attendant medical staff. Radioactive podine-131 is used to combat cancer of the thyroid gland. Since rodine tends to collect in the thyroid gland, radioactive isotopes lodge where they can destroy the malignant cells. In some cases encapsulated "seeds" are implanted in the malignant tissue for local and short ranged treatment. For skin cancers, phosphorus-32 or strontium-90 may be used instead. These produce β-radiation. The dose of radiation has to be carefully controlled otherwise the radiation could do more damage than help. Patients undergoing radiation treatment often feel. If because the radiation also damages the healthy cells.



Fig. 21 17

The y-rays radiographs are used in medical diagnosis such as internal imaging of the brain to determine precisely the size and location of a tumor or other parts of the body. Cracks or cavities in castings or pipes can also be detected by scanning. Any sudden increase in count rate indicates a cavity within the object.

The gamma camera is designed to detect /-radiations from sites in the body where a /-emitting isotope is located. An image as shown in Fig. 21.17, consisting of many dots of the remitting sources in the patient body is formed. The camera can also be used to obtain a sequence of images to observe an organ such as a kidney in action.

#### 21.14 BASIC FORCES OF NATURE

The man has always desired to comprehend the complexity of nature in terms of as few elementary concepts as possible. Among his quest in Feynman's words has been the one for "wheels within wheels" the task of Natural Philosophy being to discover the inner most wheels if any such exist. A second quest has concentrated itself with the fundamental forces, which make the wheels go round and enmesh with one another.

Although we have been familiar with the basic forces and about some of the basic building blocks of the matter but here we are going to study the modern concepts about both of these. We know that the basic forces are

- 1. Gravitational force
- 2 Magnetic force
- 3 Electric force
- 4. Weak nuclear force
- 5 Strong nuclear force

The electric and magnetic forces were unfied to get an electromagnetic force by Faraday and Maxwell, who were able to prove that a current is induced in a coil whenever the magnetic flux passing through the coil is changed, leaving behind four fundamental forces, the strong nuclear force, the electromagnetic force, the weak nuclear force and the gray tational force. These four fundamental forces of nature have seemed for some time ou teld ifferent from one another. Despite its different effective strength the strong nuclear force is effective only within sub-nuclear distances and therefore, confines the neutrons and protons within the nucleus. The electromagnetic force is long-range and causes. all chemical reactions it binds together atoms molecules, crystals, trees, buildings and you. This force acting on a m croscopic eve is responsible for a variety of apparently different macroscopic forces such as friction, cohesion and adhesion. The weak nuclear force is short range, like the strong nuclear force and is responsible for spontaneous breaking up of the radioactive elements, it is a sort of repulsive force of very short range (10 "m). It is usually masked by the effect of the strong and electromagnetic forces inside the nuclei. The gravitational force, like the electromagnetic force is again long range, extending upto and beyond the remotest stars and galaxies. It keeps you the atmosphere and the seas fixed to the surface of the planet it. gives rise to the ocean tides and keeps the planets moving in their orbits around the Sun.

These widely disparate properties of the four basic forces have not stopped the scientists from finding a common cause. for them al

One hundred years after the unification of electric and magnetic forces into electromagnetic force, in 1979, the physics nobel prize was conferred on Giashow Weinberg and Abdus Sam for the unification of electromagnetic and weak forces.

It is further expected that a strong nuclear force will eventually unite with electroweak force to make up a single entity resulting in the grand unified electro-nuclear force

#### BUILDING BLOCKS OF MATTER

Subatomic particles are divided into three groups.

1. Photons 2. Leptons Hadrons

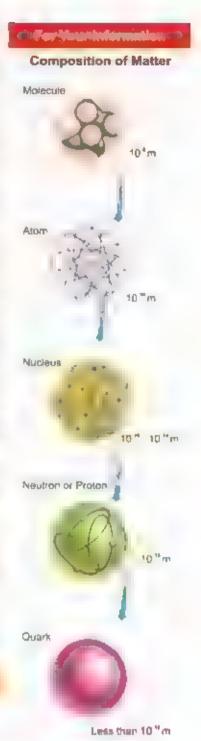


Table 21 5 Quarks and Antiquarks

Name	Symbol	Charge
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Ant quarks

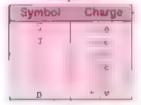






Fig. 21 18

Elementary particles are the casic building blocks of matter All photons and leptons are elementary particles. Hadrons are not elementary particles but are composed of elementary particles called quarks. Scientists now believe that all matter belongs to either the quark group or the lepton group.



Hadrons are particles that expenence the strong nuclear force in addition to protons neutrons and mesons are hadrons. The particles equal in mass or greater than protons are called baryons and those lighter than protons are called mesons.



Leptons are particles that do not experience strong nuclear force. Electron, muons and neutrinos are septons.



According to quark theory initiated by M. Gell-Mann and G. Zweig, the quarks are proposed as the basic building blocks of the mesons and baryons. A pair of quark and antiquark makes a meson and 3 quarks make a baryon. It is proposed that there are six quarks like (1 up (2, down (3) strange (4 charm 5) builton and 6) top. The charges on these quarks are fractional as shown in Table 21.5.

Aproton is assumed to be made up of two up quarks and one down quark as shown in Fig. 21.18 a. The neutron is assumed to be made of one up quark and two down quarks as shown in Fig. 21.18 (b). Currently like hundred of hadrons can be accounted for in terms of six quarks and their antiquarks. It is believed that quarks carried this carried that quarks carried their existence has been indirectly verified.



 The combined number of at the protons and neutrons in a nucleus is known as mass number and is denoted by A

- The protons and neutrons present in the nucleus are called nucleons.
- The number of performs premitting and tack
   denoted by N
- The number of protor's inside a mideus or their indicate interest one outside and a number of their indicate in a natural manual submitted by a submitted by a
- Isotopes are such rauter of an element that have it elsante marge number Z, but have different mass number A.
- The mass of the nucleus is always less than the total mass of the protons and
  neutron that make up the nucleus. The difference of the two masses is called mass
  defect. The missing mass is converted to energy in the formation of the nucleus and
  is called the binding energy.
- The energy of radiations of an analytic relationship of a single har set Z greater than 82 is called radioactivity
- The change of an element into a new element due to emission of radiations is called radioactive decay. The original element is called parent element and the element formed due to this decay is called daughter element.
- Half-life of a radioactive element is that period in which half of the atoms of the parent element decay into daughter element.
- Such a reaction in which a heavy nucleus like uranium splits up into two nuclei of equal size along with the emission of energy during reaction is called fission reaction.
- Such a nuclear reaction in which two light nuclei merge to form a heavy nucleus along with the emission of energy is called fusion reaction.
- The strength of the radiation source is indicated by its activity measured in becquerel One becquerel (Bq) is one disintegration per second. Alarger unit is curie.
   (Ci) which equals 3.7 x 10<sup>10</sup> disintegrations per second.
- The effect of radiation on a body absorbing it relates to a quantity called absorbed dose D defined as the energy E absorbed from ion zing radiation per unit mass molthe absorbing body
- The basic forces are
  - i. Gravitational force li. Electromagnetic force
  - iii. Weak nuclear force iv. The strong force
- Subatomic particles are divided into following three groups:
  - i. Photons ii. Leptons iii. Hadrons

Elementary particles are the basic building blocks of matter.

### QUESTIONS

- 21.1 What are isotopes? What do they have in common and what are their differences?
- 21.2 Why are heavy nuclei unstable?
- 21.3 If a nucleus has a half-ife of 1 year does this mean that it will be completely decayed after 2 years? Explain
- 21.4 What traction of a radicactive sample decays, after two half-lives have elapsed?
- 21.5 The raise in the intention of the Farth is about 5 brown years out how can you explain why we still can find this element in nature?
- 21.6 Describe a brief account of interaction of various types of radiations with matter
- 21.7 Explain how u and p-particles may ionize an atom without directly hitting the electrons? What is the difference in the action of the two particles for producing ionization?
- 21.8 Aparticle which produces more ionization is less penetrating. Why?
- 21.9 What information is revealed by the length and shape of the tracks of an incident particle in Wilson cloud chamber?
- 21.10 Why must a Geiger Muller tube for detecting α-particles have a very thin end window? Why does a Geiger Muller tube for detecting γ-rays not need a window at all?
- 21.11 Describe the principle of operation of a solid state detector of ionizing radiation in terms of generation and detection of charge carriers.
- 21.12 What do we mean by the term critical mass?
- 21.13 Discuss the advantages and disadvantages of nuclear power compared to the use of fossil fuel generated power
- 21.14 What factors make a fusion reaction difficult to achieve?
- 21.15 Discuss the advantages and disadvantages of fission power from the point of safety pollution and resources.
- 21.16 What do you understand by "background radiation"? State two sources of this radiation.
- 21.17 f someone accidently swallows an α-source and a β-source which would be the more dangerous to him? Explain why?
- 21 18 Which radiation dose would deposit more energy to the body (a) 10 mGy to the hand, or (b) 1 mGy dose to the entire body.
- 21.19 What is a radioactive tracer? Describe one application each in medicine, agriculture and industry.
- 21.20 How can radioactivity help in the treatment of cancer?

### PROBLEMS

- 21.1 Find the mass defect and the binding energy for totium if the atomic mass of tritium is 3 016049 u. (Ans: 0 00857 u, 7 97 MeV)
- 21.2 The half-life of 11 Sr is 9.70 hours. Find its decay constant. Ans. 1.99 x 10 s)
- 21.3 The element <sup>234</sup><sub>9</sub>,Pa is unstable and decays by β-emission with a half ide 6.66 hours state the nuclear reaction and the daughter nucle .Ans <sup>44</sup><sub>24</sub> U)
- 21.4 Find the energy associated with the following reaction (Massin' H. 1 (0784 u)

What does negative sign indicate?

Ans: 1 12 MeV)

21.5 Determine the energy associated with the following reaction (mass of C=14.0077u)

$$^{14}_{6}C \longrightarrow ^{14}_{7}N + ^{0}_{1}e$$
 (Ans: 3.77 MeV)

- 21.6 If 233 decays twice by u-emission, what is the resulting isotope? Ans -25 Rn.)
- 21,7 Calculate the energy (in MeV) released in the following fusion reaction

- 21.8 A sheet of lead 5.0 mm thick reduces the intensity of a beam of line rays by a factor 0.4 Find half value thickness of lead sheet which will reduce the intensity to half of its initial value.

  (Ans: 3.79 mm)
- 21.9 Radiation from a point source obeys the inverse since at a source of 1.0 m from Geiger counter is 360 counts per minute, what will be its count rate at 3.0 m from the source? (Ans: 40 counts per min.)
- 21.10 A 75 kg person receives a whote body radiation dose of 24 m-rac, delivered by u-particles for which RBE factor is 12. Calculate (a) the absorbed energy in joules, and (b) the equivalent dose in rem. (Ans. (a) 18 mJ (b) 0.29 rem]

Note: Consult the table on page 222, where required, for atomic masses.

# GLOSSARY

,	- Alternating Current	Current produced by a voltage source whose polarity
		keeps on reversing with time
,	Amorphous	Those solids in which arrangement of atoms or
		molecules are not regular
-	Amplifier	A device that increases the output of electrical signal
		fed as input
-	Atomic Number	The number of protons in the nucleus
-	Sinding Energy	The work done on the nucleus to separate it into its
		constituent neutrons and protons
*	Black Body	A body that absorbs all the radiations incident upon it
*	Bulk Modulus	Ratio of applied stress to volumetric strain
-	Capacitor	A device that can store charge
•	Cathode ray Oscilloscope	High speed graph plotting device
-	Compton effect	An increase in the wavelength of X-rays when
		scattered by bound electrons
-	Crystalline Solids	Substances having regular arrangement of atoms or
		money tobs
,	Current	A device which converts mechanical energy into
	Generator	electrical energy
-	Digital System	It deals with only those quantiles which have only two
		discrete values
-	Elastic limit	The limit beyond which the sample becomes
		permanently deformed
-	Electric Current	Rate of flow of electric charge
-	Electric Field Intensity	Electric field force per unit charge at a point

-	Electric Flux	Number of electric field lines passing through certain
		surface element
*	Electric Potential	Amount of work done in bringing a unit positive charge
		from infinity to a point
-	Electrolysis	Conduction of electricity due to chemical reaction in
		kquids
,	Electromagnetic	Waves which do not require any medium for their
	Waves	propagation
-	Electromotive	A measure of the energy supplied by a source of
	Force	efecting current per unit charge
1	Electron volt	Unit of energy equals to 1.6×10 <sup>-19</sup> J
-	Electroplating	Electric metallic coating
-	Forward Blas	Bias voltage which when applied to a pin junction
		produce large current flow
*	Frequency	Number of cycles per unit time
-	Fusion	Such nuclear reaction in which two light nuclei merge
	, 40,011	passet indicate the real section of the real section of the
	, 45,011	to form a heavy nucle is with the emission of energy
,	Half life	
-		to form a heavy nucle is with the emission of energy
,		to form a heavy nucle is with the emission of energy. It is the period in which half of the radioactive element.
	Half life	to form a heavy nucle is with the emission of energy it is the period in which half of the radioactive element atoms decay.
	Half life Holography	to form a heavy nucle is with the emission of energy it is the period in which half of the radioactive element atoms decay.  A method of recording three dimensional image.
	Half life Holography	to form a heavy nucle is with the emission of energy.  It is the period in which half of the radioactive element atoms decay.  A method of recording three dimensional image.  Combined effect of resistances and reactances in an
1 11 1	Half life Holography Impedance	to form a heavy nucle is with the emission of energy.  It is the period in which half of the radioactive element atoms decay.  A method of recording three dimensional image.  Combined effect of resistances and reactances in an A.C. circuit.
	Half life Holography Impedance	to form a heavy nucle is with the emission of energy. It is the period in which half of the radioactive element atoms decay.  A method of recording three dimensional image.  Combined effect of resistances and reactances in an A.C. circuit.  The phenomenon in which changing current in a coil.
	Half life Holography Impedance Inductance Inertial frame of	to form a heavy nucle is with the emission of energy. It is the period in which half of the radioactive element atoms decay.  A method of recording three dimensional image.  Combined effect of resistances and reactances in an A.C. circuit.  The phenomenon in which changing current in a coil produces an emi in itself.
	Half life Holography Impedance Inductance Inertial frame of reference	It is the period in which half of the radioactive element atoms decay  A method of recording three dimensional image  Combined effect of resistances and reactances in an A C circuit  The phenomenon in which changing current in a coil produces an emi in itself  Coordinate system in which the law of mertia is valid

-	Laser	Light amplification by stimulated emission of radiation
	Logic Gate	Electronic circuits which implements various logic
		operations
*	Magnetic Induction	Magnetization of a substance by an external magnetic
		field
-	Mass Defect	It is the difference between the mass of the separated
		nucleons and the combined mass of the nucleus
ja	Mass Number	Total number of protons and neutrons in a nucleus
p	Modulation	The process of combining the low frequency signal
		with a high frequency radio wave
-	Mutual Inductance	A phenomenon in which a changing current in one coil
		produces emf in other coil
-	NAVASTAR	Navigation system based on Einstein theory of
		relativity
-	Nuclear Energy	Energy denved from nuclear reactions either by fission
		or by fusion
*	Nuclear fission	Disintegration of atomic nucleus into two or more
		fragments with the emission of huge amount of energy
	Nuclear Reactor	A device in which controlled nuclear fission reaction
		takes place
,	Nucleons	Protons and neutron in the nucleus,
	Pair Production	Production of electron-position pair from a photon
-	Photo voltaic cell	A device that detects or measures electromagnetic
	<b>D</b> 1	radiation by generating a potential at a junction
-	Photodiode	A device used to detect light falling on it
	Photoelectric	Emission of electrons from metallic surface when
	Effect	exposed to electromagnetic radiations
	Plastic deformation	A permanent deformation of a solid object to an
		applied stress

-	Polymeric Solids	The solid materials with a structure that is intermediate
		between ordered and disordered structure
-	Rectification	Conversion of alternating current into direct current
-	Resistivity	Tendency of material to oppose the flow of current
-	Reverse Bias	Bias voltage which when applied to a p - n junction
		produces a very small or no current flow
-	Spectrograph	An instrument for producing photographic record of
		spectrum
-	Spectroscopy	The investigation of wavelength and intensities of
		electromagnetic radiations emitted or absorbed by the
		atoms
-	Strain	The change produced in the size or shape of the body
		by applying a stress
-	Stress	Force per unit area
-	Super Conductors	Those material whose resistivity becomes zero below
		a critical temperature
-	Thermistor	Heat sensitive resistor
7	Time Period	That interval during which the voltage source changes
		its polarity once
7	Transformer	A device which converts high A.C. voltage to low A. C.
		voltage or low A.C. voltage to high A. C. voltage
*	Transistor	Semi conducting material to which at least three
		efectrical contacts are made
7	Ultimate tensile stress	The maximum stress that a material can withstand
•	Young's Modulus	Ratio of the tensile stress applied to the material to the
		resulting tensile strain

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# INDEX

A		Capacitance	22
A.C. generator	97-99	Capacitor	22
Absorbed dose	250	CAT Scanar	211
Alpha particles	226	Characteristic X-rays	209-210
Alternating current	111	Choke	128
Ammeter	74	Collector	159
Amorphous solid	136	Comparator	166-167
Ampere's law	61-62	Compressional stress	138
Amplitude modulation	131	Compressive strain	138
	168	Compton effect	190-191
AND gate	168	Compton shift	190-191
AND Operation	192-193	Compton wavelength	190-191
Annihilation of matter	220	Conductance	38
Atomic nucleus	220	Conduction band	143
Atomic number	76	Conductors	143-144
Avometer	10	Conventional current	32
В	000	Core	244
Balmer series	203	Coresivity	150
Baryons	256	Cosmic radiation	249
Base	159	Coulomb's law	2
Basic forces	254-255	Critical mass	242-243
Becqueral	250	Critical temperature	146
Beta particles	226	Crystalline solid.	136
Binding energy	223	Curie	250
Black body	183	Current gain	160
Black body radiation	182-183	D	
Bohr's atomic model	204-205	D.C. generator	100-101
Bohr's orbit	205	D.C. motor	102
Boolean variable	168	Daughter element	230
Brackett series	204	Dead beat galvanometer	74
Bragg's equation	194-195	de-Broglie relation	193
Bremsstrahlung	210	Decay constant	230
Brittle substances	140	Depeletion region	154
Building block of matter	255-256	Deparetion region	221
*Bulk modulus	139	Deutenum	221
C.R.O.	68-70	Diamagnetic substances	148

24	G	
		164-165
		71-74
	Gamma rays	226-227
140	Geiger Muller counter	235-237
12.12		178
43-44		251
		12
		256
	Half life	229
	Half wave rectification	156
	He-Ne laser	215
	Henery	92-94
	Holography	216
	Hooke's law	140
	Hydrogen emission spectrum	
	Hysteresis	150
	Hysteresis loop	148-150
		150
	1	,00
	Impedance	120
		82-84
		82-84
		177
	Insulators	143-144
144	Intrinsic semiconductor	144
		207
	Ionization potential	207
87	Territoria	221
246	K	66.1
	Kirchhoff's first law	46
	187 . 1	47
		M-3
143		212
	( autor )	213
	1	155
	Lawrence to an	179
157	Lantana	38
	LBURDE	256
	148 242 233 143 155 177 131-132	77-78 167-168 167-168 167-168 168-149 140 Gamma rays 140 Geiger Multer counter General theory of relativity 43-44 Gray 188 Guass's law 140 H 32 Hadrons Half life 9-10 Haif wave rectification He-Ne laser Henery 15 Holography 149 Hooke's law 185 Hydrogen emission spectrum Hysteresis loop Hysteresis loss 197 Hysteresis loss 197 Hysteresis loss 197 Hysteresis loss 159 I mertial frame of reference Induced current Induced e.m.f. Inertial frame of reference Insulators Intrinsic semiconductor Ionization energy Ionization potential Isotopes K 148 Kirchhoff's first law Kirchhoff's first law Kirchhoff's second law L Laser Leakage current Length contraction Lenz's law

Linear absorption co-efficient	233	Operational amplifier	162-163
Lyman senes	203	OR gate	168
M		OR operation	168
Magnetic dipole	148	P	
Magnetic flux	60	p - n junction	154
Magnetic flux density	60-61	Pair production	192
Mass defect	223	Parent element	227
Mass spectrograph	222-223	Paschen series	204
Mass variation	180	Pfund series	204
Measurement of e/m	66-67	Photo diode	158
Mesons	256	Photo electron	187
Millikan's method	20-21	Photo electron	187
Moderator	244	Photo voltaic cell	158
Modulation	131	Photocell	189
Modulus of elasticity	139	Photoelectric effect	187-189
Motional e.m.f.	84	Photon	185
Mutual inductance	90-91	Plancks constant	184
N	55.51	Plastic deformation	140
NAND gate	169	Plasticity	140
NAND operation	169	Polymenic solids	136-137
NAVASTAR Navigation system	180	Population inversion	214
NAVASTAR Navigation system	180	Positron	192
Night switch	171	Potentiometer	51-52
Non-intertial frame of reference	178	Principle quantum number	204
NOR gate	169	Proportional limit	140
NOR operation	169	Protium	221
NOT gate	169	Q	
NOT operation	169	Quantized energy	206
n-p-n transistor	159	Quantized radii	206
Nuclear fission	240	Quarks	256
Nuclear power station	243-245	R	
Nuclear reaction	238-239	Radiation absorbed dose	251
Nuclear reactor	243-246	Radiation detector	234-237
Nuclear transmutation	227-228	Radiation exposure	249-250
Nucleon number	220	Radiation sickness	251
0		Radioactive decay	227
Ohm	37	Radioactive elements	226
Ohm meter	76-77	Radioactivity	226
Ohm's law	36	Radiography	254
Open loop gain	163	Rectification	156

Relative biological effectiveness	251	T	
Relative motion	177	Tensile strain	138
Rem	251	Tensile stress	138
Resistivity	38	Thermal reactor	246
Resonance	125	Thermistor	42
Retantivity	150	Threshold frequency	188
Rheostat	41	Time dilation	179
Right hand rule	57	Tracer techniques	
Rutherford atomic model	220	Transformer	252-253
Rydberg constant	203, 208	Transistor	103-106
5	200, 200	Tritium	159
Saturation	150	U	221
Self inductance	93	_	110
Self quenching	236	Ultimate lensile strength	140
Semiconductors	143	Uncertainty principle Unified mass	197-199
Sensors	170-171	Uses of laser	220
Shear modulus	139	V	215-216
Shear strain	139	•	
Shear stress	138	Voltage gain	161-162
Sievert	251	Voltmeter 3	75
Solid state detector	237	W	138-139
Special theory of relativity	178-181		
	203	Wave particle duality	195-196
	202	Weber	60
	104	Wheatstone bridge	50-51
	104	Wilson cloud chamber Work function	234-235
	184		188
A	184	X	
Wild I was a second of the sec	213	Xerography	8-9
and the second s	213	XNOR gate	170
	187	XNOR operation	170
and the second s	138	XOR gate	169-170
and the second s	138	XOR operation	169
According to the contract of t	140	X-rays	209-211
	146-147	Y	
		Young's modulus	139